

EcoFormer: Energy-Saving Attention with Linear Complexity

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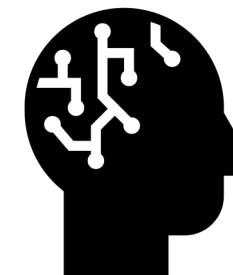
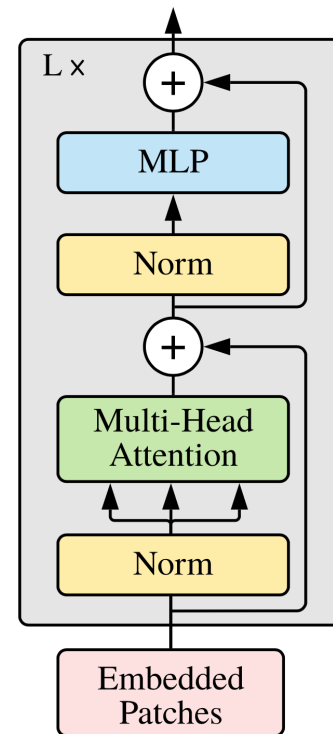
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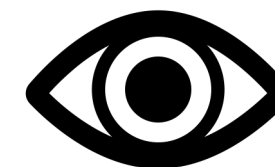
Background: Transformers



Transformer Encoder



Natural Language Processing



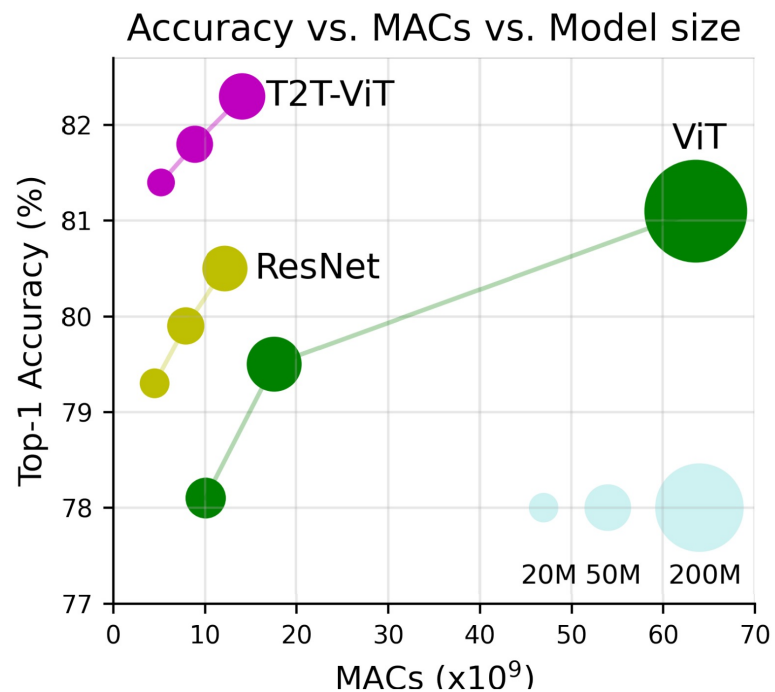
Computer Vision

Transformers treat input as a sequence of patches and processes with a Transformer encoder.

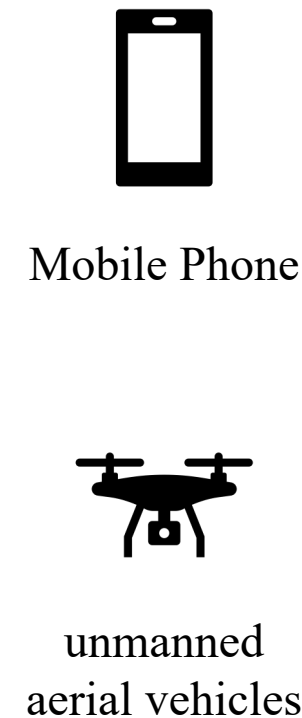
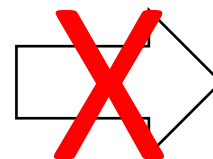
Dosovitskiy et al. An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale. ICLR 2021.

Liu et al. EcoFormer - NeurIPS 2022

Background: Transformers



Deploy

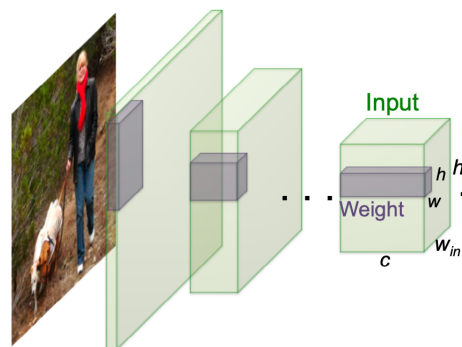


The efficiency bottlenecks greatly hamper the massive deployment to resource-constrained edge devices.

Background: Binary Quantization

Table. Energy cost for different operations (on 45nm CMOS technology).

Operation	16-bit FP Add	16-bit FP Mult	32-bit FP Add	32-bit FP Mult
Energy (pJ)	0.4	1.1	0.9	3.7
Area (μm^2)	1,360	1,640	4,184	7,700



	Network Variations	Operations used in Convolution	Memory Saving (Inference)	Computation Saving (Inference)	Accuracy on ImageNet (AlexNet)												
Standard Convolution	<p>Real-Value Inputs</p> <table border="1"> <tr><td>0.11</td><td>-0.21</td><td>-0.34</td></tr> <tr><td>-0.25</td><td>0.61</td><td>0.52</td></tr> </table> <p>Real-Value Weights</p> <table border="1"> <tr><td>0.12</td><td>-1.2</td><td>0.41</td></tr> <tr><td>-0.2</td><td>0.5</td><td>0.68</td></tr> </table>	0.11	-0.21	-0.34	-0.25	0.61	0.52	0.12	-1.2	0.41	-0.2	0.5	0.68	+ , - , ×	1x	1x	%56.7
0.11	-0.21	-0.34															
-0.25	0.61	0.52															
0.12	-1.2	0.41															
-0.2	0.5	0.68															
Binary Weight	<p>Real-Value Inputs</p> <table border="1"> <tr><td>0.11</td><td>-0.21</td><td>-0.34</td></tr> <tr><td>-0.25</td><td>0.61</td><td>0.52</td></tr> </table> <p>Binary Weights</p> <table border="1"> <tr><td>1</td><td>-1</td><td>1</td></tr> <tr><td>-1</td><td>1</td><td>1</td></tr> </table>	0.11	-0.21	-0.34	-0.25	0.61	0.52	1	-1	1	-1	1	1	+ , -	~32x	~2x	%56.8
0.11	-0.21	-0.34															
-0.25	0.61	0.52															
1	-1	1															
-1	1	1															
BinaryWeight Binary Input (XNOR-Net)	<p>Binary Inputs</p> <table border="1"> <tr><td>1</td><td>-1</td><td>-1</td></tr> <tr><td>-1</td><td>1</td><td>1</td></tr> </table> <p>Binary Weights</p> <table border="1"> <tr><td>1</td><td>-1</td><td>1</td></tr> <tr><td>-1</td><td>1</td><td>1</td></tr> </table>	1	-1	-1	-1	1	1	1	-1	1	-1	1	1	XNOR , bitcount	~32x	~58x	%44.2
1	-1	-1															
-1	1	1															
1	-1	1															
-1	1	1															

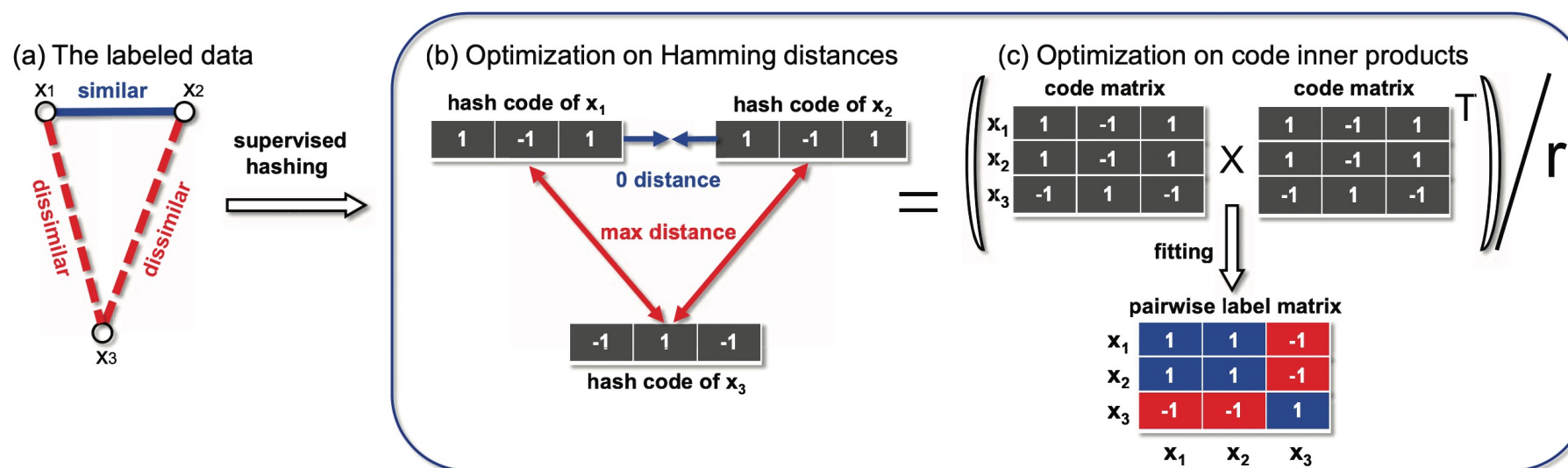
Binarize weights enable to replace the multiply-accumulate operations with energy-efficient accumulations.

- (a) Rastegari et al. XNOR-Net: ImageNet Classification Using Binary Convolutional Neural Networks. ECCV 2016.
- (b) Han et al. EIE: Efficient Inference Engine on Compressed Deep Neural Network. ISCA 2016.
- (c) Mark Horowitz. 1.1 computing's energy problem (and what we can do about it). ISSCC 2014.
- (d) Lian et al. High-performance FPGA-based CNN accelerator with block-floating-point arithmetic. VLSI 2019.

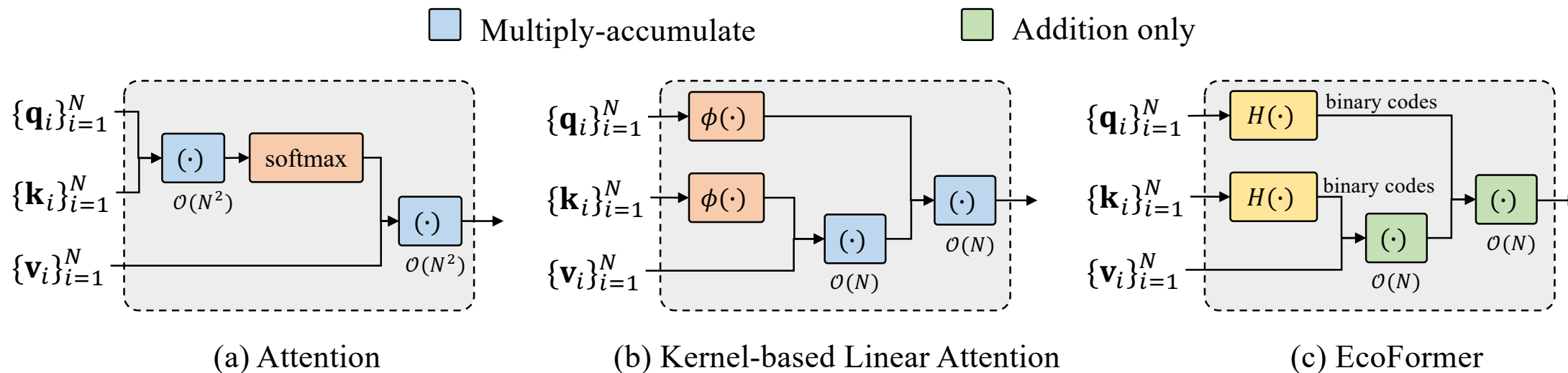
Background: Limitation of Binary Quantization

Limitation: Binary quantization can not well preserve the similarity relations among tokens in attention.

Solution: Learn kernelized hashing to map the queries and keys into low-dimensional binary codes while preserving the similarity relations in Hamming space.



EcoFormer



- ❑ Utilize kernel-based linear attention reduces the time complexity from $\mathcal{O}(N^2)$ to $\mathcal{O}(N)$.
- ❑ Use self-supervised kernelized hashing to map the queries and keys to compact binary codes.
- ❑ Replace most of the energy-hungry floating-point multiplications with energy-efficient additions.

EcoFormer

Hash function: $h(\mathbf{Q}) = \text{sign} \left(\sum_{j=1}^m (\kappa(\mathbf{q}_{(j)}, \mathbf{Q}) - \mu_j) a_j \right) = \text{sign}(\mathbf{g}(\mathbf{Q})\mathbf{a})$

$$H(\mathbf{Q}) = [h_1(\mathbf{Q}), \dots, h_b(\mathbf{Q})] = \begin{bmatrix} h_1(\mathbf{q}_1), \dots, h_b(\mathbf{q}_1) \\ \dots\dots\dots \\ h_1(\mathbf{q}_N), \dots, h_b(\mathbf{q}_N) \end{bmatrix} = \text{sign}(\mathbf{g}(\mathbf{Q})\mathbf{A})$$

Objective for hash function learning:

$$\min_{\mathbf{A}} \left\| H(\mathbf{Q})H(\mathbf{Q})^\top - b\mathbf{Y} \right\|_F^2 = \min_{\mathbf{A}} \left\| \sum_{r=1}^b h_r(\mathbf{Q})h_r(\mathbf{Q})^\top - b\mathbf{Y} \right\|_F^2$$

where $\mathbf{Y}_{ij} = \begin{cases} 1, & (\mathbf{q}_i, \mathbf{q}_j) \in \mathcal{S} \quad \text{Similar pairs of tokens} \\ -1, & (\mathbf{q}_i, \mathbf{q}_j) \in \mathcal{U} \quad \text{Dissimilar pairs of tokens} \\ 0, & \text{otherwise.} \end{cases}$

Results on ImageNet-1k

Table. Main results on ImageNet-1K.

Model	Method	#Mul. (B)	#Add. (B)	Energy (B pJ)	Throughput (images/s)	Top-1 Acc. (%)
PVTv2-B0 [62]	MSA	2.02	1.99	9.25	850	70.77
	Ours	0.54	0.56	2.49	1379	70.44
PVTv2-B1	MSA	5.02	5.00	23.07	621	78.83
	Ours	2.03	2.09	9.39	874	78.38
PVTv2-B2	MSA	8.64	8.60	39.71	404	81.82
	Ours	3.85	3.97	17.82	483	81.28
PVTv2-B3	MSA	11.86	11.82	54.56	310	82.26
	Ours	6.54	6.72	30.25	325	81.96
PVTv2-B4	MSA	15.97	15.93	73.43	247	82.42
	Ours	9.57	9.82	44.25	249	81.90
Twins-SVT-S [10]	MSA	5.96	5.91	27.36	426	81.66
	Ours	2.72	2.81	12.59	576	80.22

- Our EcoFormer achieves **lower computational complexity**, **less energy consumption** and **higher throughput** with comparable performance.

Results on LRA

Table. Comparisons of different methods on Long Range Arena (LRA).

Method	#Mul. (B)	#Add. (B)	Energy (B pJ)	Text (4K)	Retrieval (4K)	Average
Transformer	4.63	4.57	21.25	64.87	79.62	72.25
Performer [9]	0.83	0.84	3.83	64.82	79.08	71.95
Linformer [60]	0.81	0.81	3.74	57.03	78.11	67.57
Reformer [29]	0.54	0.54	2.49	65.19	79.46	72.33
Combiner* [50]	0.51	0.51	2.34	64.36	56.10	60.23
EcoFormer	0.25	0.29	1.17	64.79	78.67	71.73

□ Our EcoFormer saves around **94.6%** multiplications, **93.7%** additions and **94.5%** on-chip energy consumption compared with standard multi-head self-attention.

(a) Choromanski et al. Rethinking attention with performers. ICLR 2021.

(b) Wang et al. Linformer: Self-attention with linear complexity. ArXiv 2020.

(c) Kitaev et al. Reformer: The efficient transformer. ICLR 2020.

(d) Ren et al. Combiner: Full attention transformer with sparse computation cost.. NeurIPS 2021.

Quantization vs. hashing

Table. Performance comparisons with different binarization methods on CIFAR-100.

Model	Method	#Mul. (B)	#Add. (B)	Energy (B pJ)	Top-1 Acc. (%)
PVTv2-B0	FP-EcoFormer	0.94	0.94	4.33	70.78
	Bi-EcoFormer	0.63	0.83	3.09	70.06
	EcoFormer	0.54	0.56	2.49	71.23
Twins-SVT-S	FP-EcoFormer	5.96	5.91	27.36	80.04
	Bi-EcoFormer	3.01	3.59	14.38	80.04
	EcoFormer	2.72	2.81	12.58	80.31

- ❑ Our EcoFormer with lower energy cost **consistently outperforms** Bi-EcoFormer on different frameworks.
- ❑ Our proposed self-supervised hash functions **preserve the pairwise similarity** of attention.

Thanks for Watching

Please refer to our paper and code for more details

Paper



Code

