

# CPM-Nets: Cross Partial Multi-View Networks

Changqing Zhang, Zongbo Han, Yajie Cui, Huazhu Fu,  
Joey Tianyi Zhou, Qinghua Hu

Tianjin University, Tianjin, China

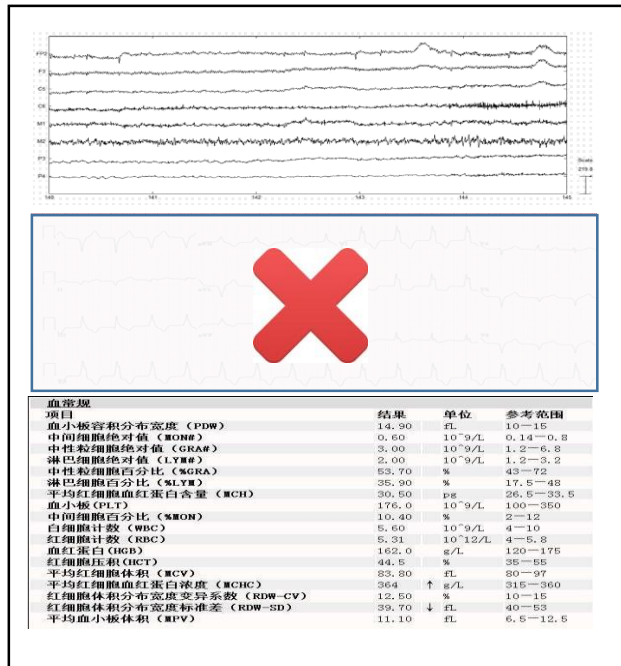
Inception Institute of Artificial Intelligence, Abu Dhabi, UAE

Institute of High Performance Computing, A\*STAR, Singapore

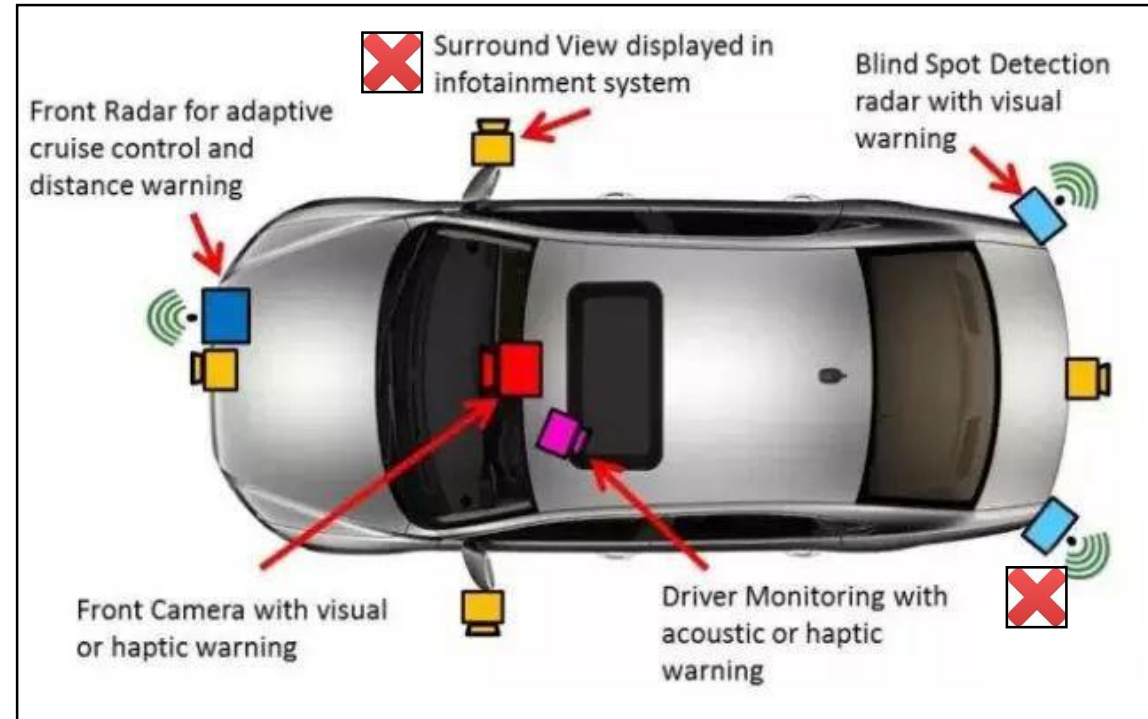
# CPM-Nets: CPM-Nets: Cross Partial Multi-View Networks

## Multi-View Classification & Theory

### Multi-modal medical data



### Multi-sensor driving



# Challenges of Classification on Partial Multi-View Data

- ❑ For complex view-missing, how to avoid manually preprocessing (e.g., completion/discarding/grouping)?
  - Large number of views, and view-missing patterns;
  - The view-missing pattern of test sample is novel;
- ❑ How to guarantee the sufficiency in using partial multiple views?
- ❑ How to scale for large-scale & small-sample-size cases?

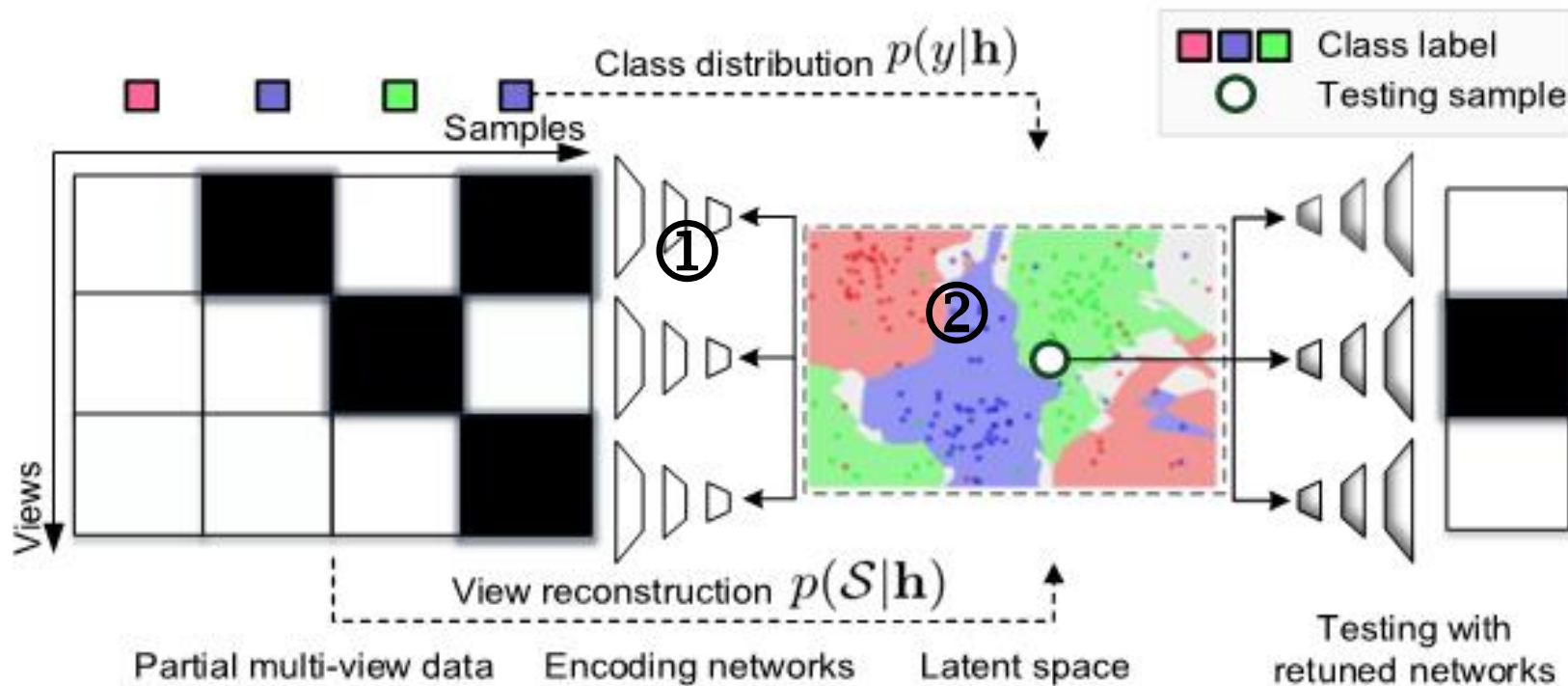
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# Our Algorithm for Classification on Partial Multi-View Data

1. **Flexibility:** Samples with arbitrary view-missing patterns;
2. **Complete-Representation:** Compact with full information;
3. **Structured-Representation:** Simplify classifier for interpretability;

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# Framework of CPM-Nets



① **Backward- Encoding:**  
completeness & flexibility

② **Structured Representation:** simple classifier & interpretability

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# Framework of CPM-Nets

All (partial) available views are encoded into  $\mathbf{h}$

Clustering-like loss: structured representation & nonparametric classifier

**Complete Representation**

**Structured Representation**

$$\min_{\{\mathbf{h}_n\}_{n=1}^N, \Theta_r} \frac{1}{N} \sum_{n=1}^N \ell_r(\mathcal{S}_n, \mathbf{h}_n; \Theta_r) + \lambda \ell_c(y_n, y, \mathbf{h}_n)$$

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# Theoretical Analysis

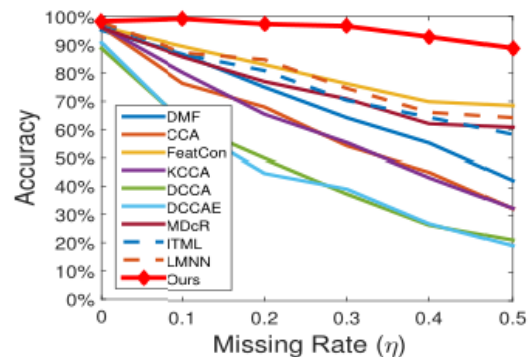
**Proposition 2.1** (*Versatility for the Multi-View Representation from Eq. (5)*) *There exists a solution (with respect to latent representation  $\mathbf{h}$ ) to Eq. (5) which holds the versatility.*

**Proof 2.1** *The proof for proposition 2.1 is as follow. Ideally, according to Eq. (5), there exists  $\mathbf{x}^{(v)} = f_v(\mathbf{h}; \Theta_r^{(v)})$ , where  $f_v(\cdot)$  is the mapping from  $\mathbf{h}$  to  $\mathbf{x}^{(v)}$ . Hence,  $\forall \varphi(\cdot)$  with  $y^{(v)} = \varphi(\mathbf{x}^{(v)})$ , there exists a mapping  $\psi(\cdot)$  satisfying  $y^{(v)} = \psi(\mathbf{h})$  by defining  $\psi(\cdot) = \varphi(f_v(\cdot))$ . This proves the versatility of the latent representation  $\mathbf{h}$  based on multi-view observations  $\{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(V)}\}$ .*

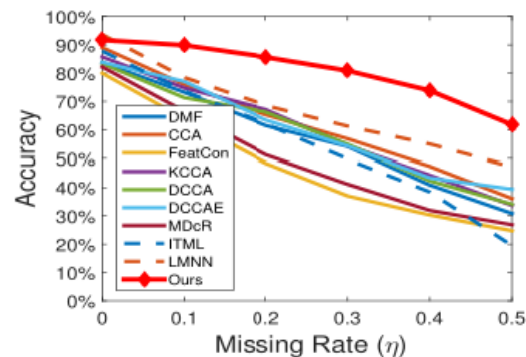
*In practical case, it is usually difficult to guarantee the exact versatility for latent representation, then the goal is to minimize the error  $e_y = \sum_{v=1}^V \|\psi(\mathbf{h}) - \varphi(\mathbf{x}^{(v)})\|^2$  (i.e.,  $\sum_{v=1}^V \|\varphi(f_v(\mathbf{h}; \Theta_r^{(v)})) - \varphi(\mathbf{x}^{(v)})\|^2$ ) which is inversely proportional to the degree of versatility. Fortunately, it is easy to show that  $Ke_r$  with  $e_r = \sum_{v=1}^V \|f_v(\mathbf{h}; \Theta_r^{(v)}) - \mathbf{x}^{(v)}\|^2$  from Eq. (5) is the upper bound of  $e_y$  if  $\varphi(\cdot)$  is Lipschitz continuous with  $K$  being the Lipschitz constant.  $\square$*

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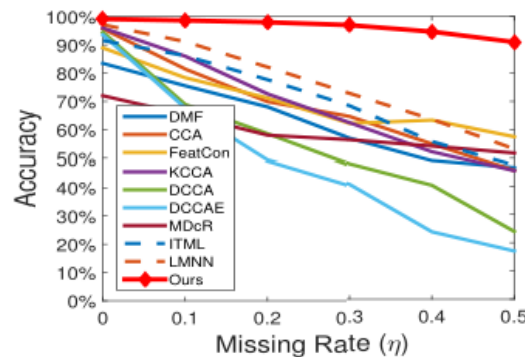
# Comparison under Different Missing Rate



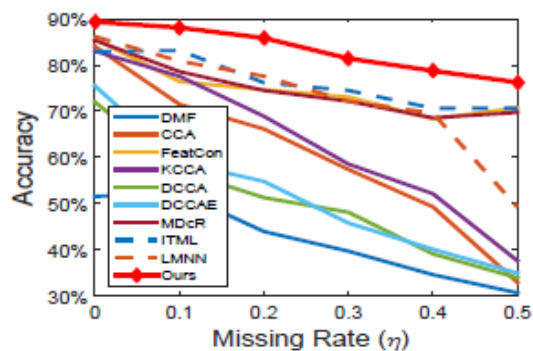
(a) ORL



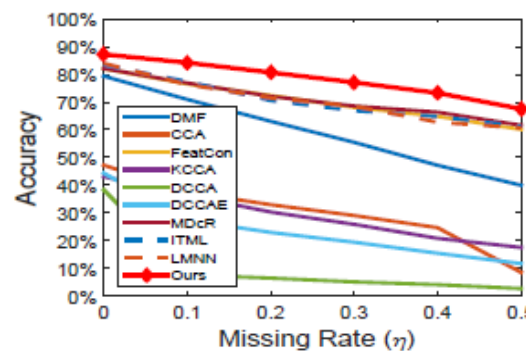
(b) PIE



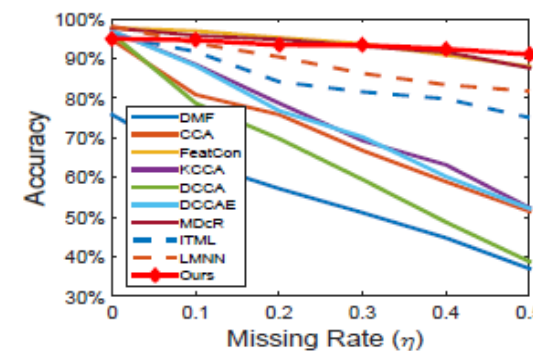
(c) YaleB



(d) CUB



(e) Animal



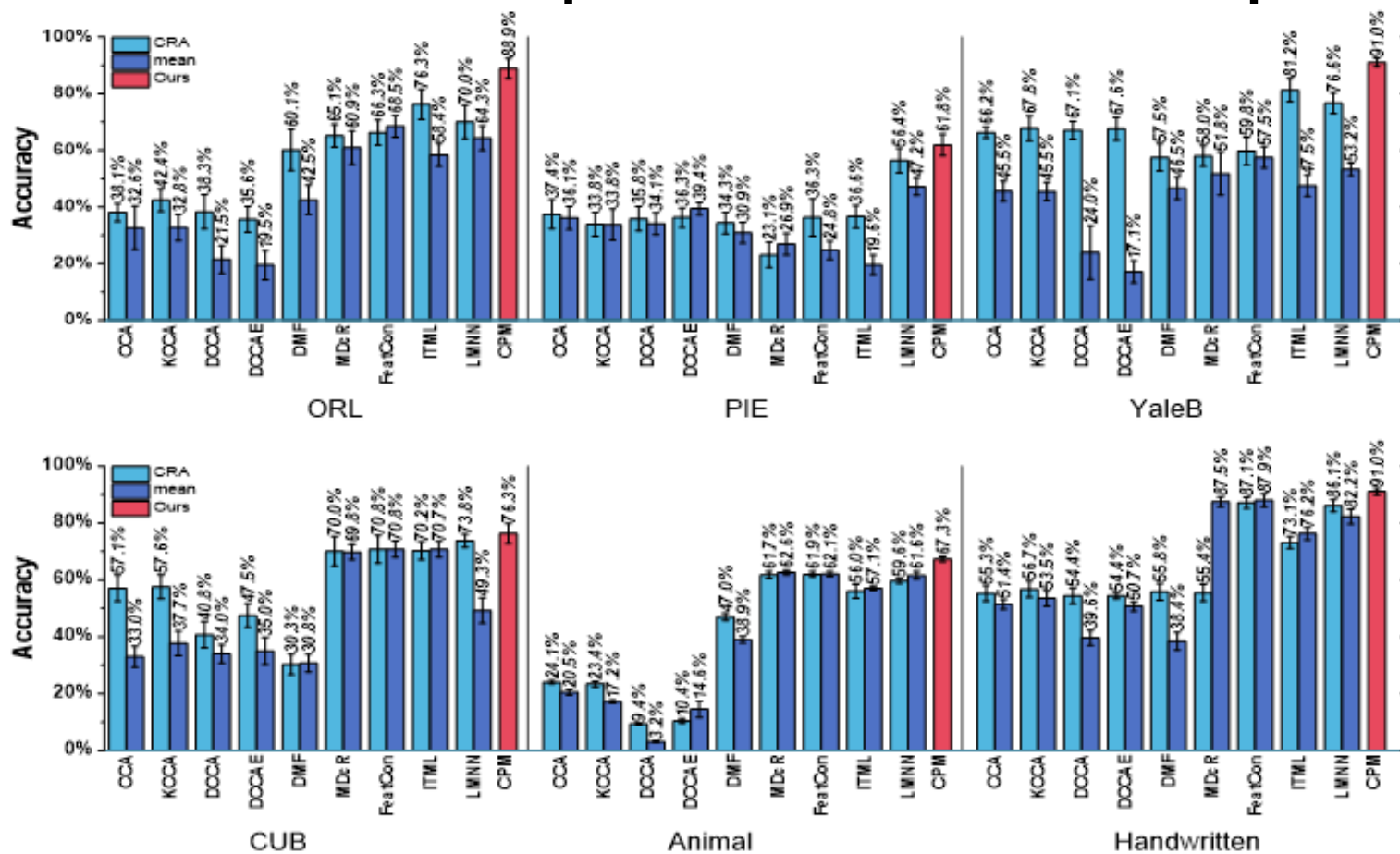
(f) Handwritten

- **CCA-based methods:** CCA/Kernelized CCA/Deep CCA;
- **Matrix Factorization-based method:** Deep MF;
- **Metric Learning Methods:** LMNN/ITML.

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# Comparison with Completion Methods



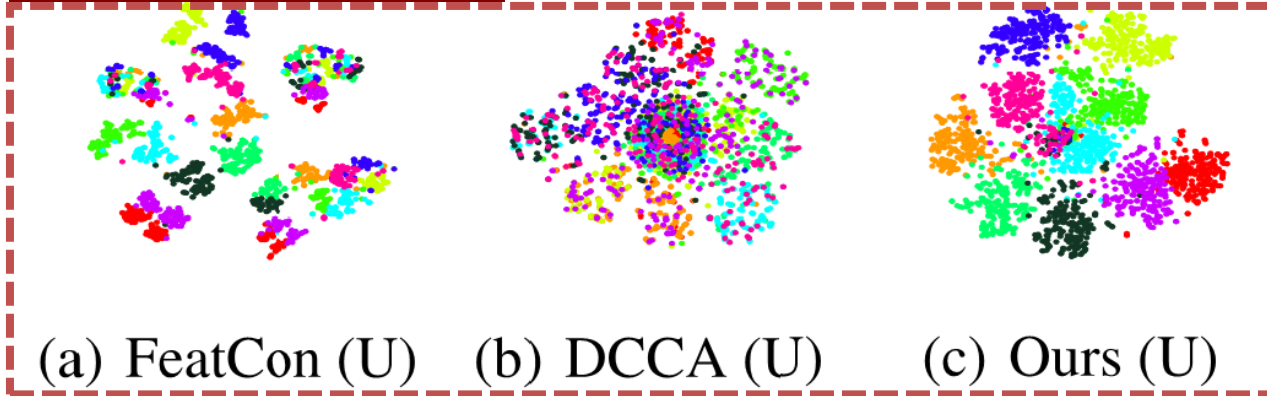
■ CRA (CVPR'17) [1];  
 ■ Mean: Complete the missing values with the mean of the observed in the same class.

[1] Missing modalities imputation via cascaded residual autoencoder. CVPR, 2017.

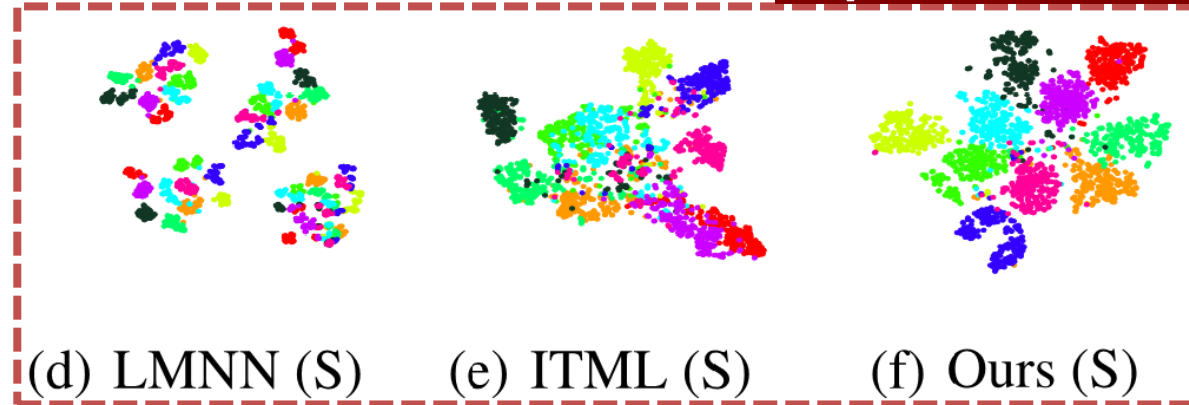
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# Visualization under Missing Rate: $\eta = 0.5$

## Unsupervised Case



## Supervised Case



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# Conclusion

- **Complete Representation:** Information preservation & flexibility for arbitrary view-missing pattern;
- **Nonparametric Classifier:** Nonparametric classifier for structured representation;
- **Theoretical Guarantee:** Strict guarantee for ideal case and bound for practical case;
- **Applicable:** Large-scale/Small-Sample-Size

*Thanks!*