



Product Ranking for Revenue Maximization with Multiple Purchases

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Problem setting

- **Basic setting**
 - **Product ranking** is the core problem for revenue-maximizing online retailers
- **Related works**
 - Most existing works suppose each consumer purchases **at most one product**
- **In this paper,**
 - We propose a more realistic consumer choice model to characterize consumer behaviors under **multiple-purchase** settings

Method

- We study the optimal product ranking policy to maximize online retailers' revenue in both offline and online settings
 - Achieve $\tilde{O}(\sqrt{T})$ regret on the revenue in online settings

Algorithm 1: MPB-UCB (Non-contextual)

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1 Input: Products revenue  $r$  and hyper-parameter  $\epsilon_Q$ .
2 Initialization:  $\tilde{\lambda}_{0,k} = 1$  for  $k \in [N]$ ,  $\tilde{q}_0 = 1 - \epsilon_Q$ ,  $\tilde{w}_0 = 1 - \epsilon_Q$ .
3 for  $t=1:T$  do
4   Let  $\sigma_t$  be the optimal offline policy from Theorem 4.1 with  $\lambda = \tilde{\lambda}_{t-1}$ ,  $q = \tilde{q}_{t-1}$ , and
    $s = \tilde{w}_{t-1}/\tilde{q}_{t-1}$ .
5   Offer ranking policy  $\sigma_t$  and observe  $\Phi_t, \Gamma_t, \eta_t, \mu_t$ .
6   Update statistics  $C_{t,k}, c_{t,k}, D_t^Q, d_t^Q, D_t^W$ , and  $d_t^W$ .
7   Calculate  $\tilde{\lambda}_{t,k}$ ,  $\tilde{q}_t$ , and  $\tilde{w}_t$  by Equations (6) and (8).
8 end
  
```

Algorithm 1: MPB-UCB (Non-contextual)

Algorithm 2: MPB-UCB (Contextual)

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1 Input: Products revenue  $r$  and hyper-parameter  $\epsilon_Q, \alpha_\Lambda, \alpha_Q$ , and  $\alpha_W$ .
2 Initialization:  $\hat{\beta}_0^\Lambda = \mathbf{0}$ ,  $\hat{\beta}_0^Q = \mathbf{0}$ , and  $\hat{\beta}_0^W = \mathbf{0}$ .
3 for  $t=1:T$  do
4   Observe consumer features  $x_t$  and  $y_{t,k}$  for  $k \in [N]$ . Let  $z_t = \text{vec}(x_t x_t^\top)$ .
5   Calculate  $\tilde{\lambda}_{t,k}$ ,  $\tilde{q}_t$ , and  $\tilde{w}_t$  according to Equation (16).
6   Let  $\sigma_t$  be the optimal ranking policy from Theorem 4.1 with  $\lambda = \tilde{\lambda}_t$ ,  $q = \tilde{q}_t$ , and  $s = \tilde{w}_t/\tilde{q}_t$ .
7   Offer ranking policy  $\sigma_t$  and observe  $\Phi_t, \Gamma_t, \eta_t, \mu_t$ .
8   Calculate statistics  $\Sigma_t^\Lambda, \rho_t^\Lambda, \Sigma_t^Q, \rho_t^Q, \Sigma_t^W$ , and  $\rho_t^W$ .
9   Calculate estimated parameters  $\hat{\beta}_t^\Lambda, \hat{\beta}_t^Q$ , and  $\hat{\beta}_t^W$  according to Equations (12), (13) and (14).
10 end
  
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Algorithm 2: MPB-UCB (Contextual)

Experiments

- We conduct experiments on both synthetic data and semi-synthetic.

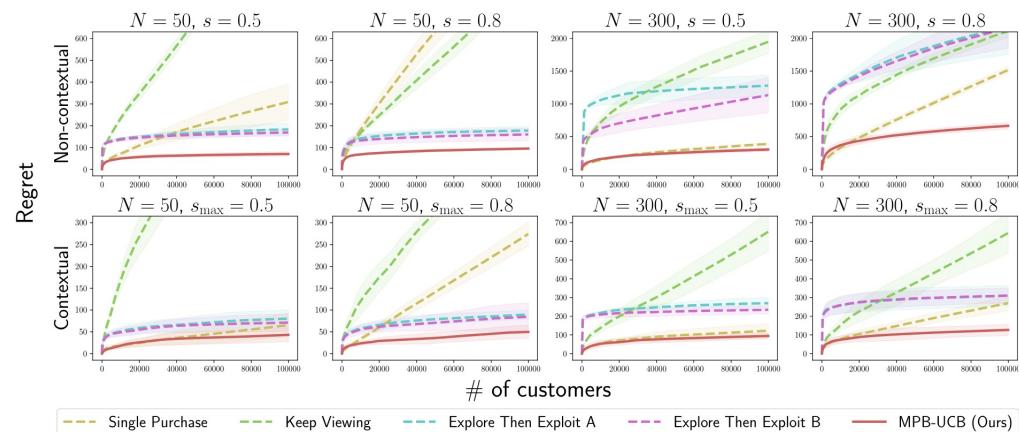


Figure 1: Results on the synthetic data

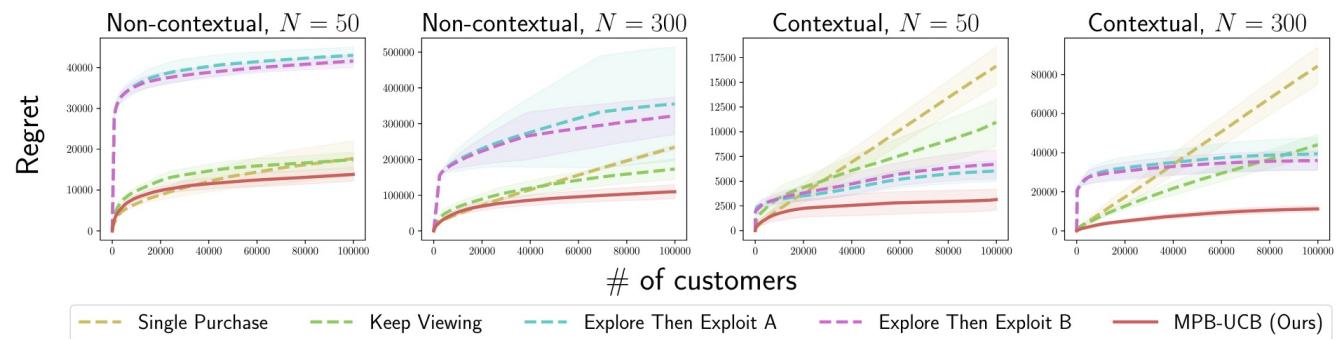


Figure 2: Results on the semi-synthetic data



Thanks!

Paper is available at <https://arxiv.org/abs/2210.08268>

Code is available at <https://github.com/windxrz/MPB-UCB>