

# FactorizePhys: Matrix Factorization for Multidimensional Attention in Remote Physiological Sensing

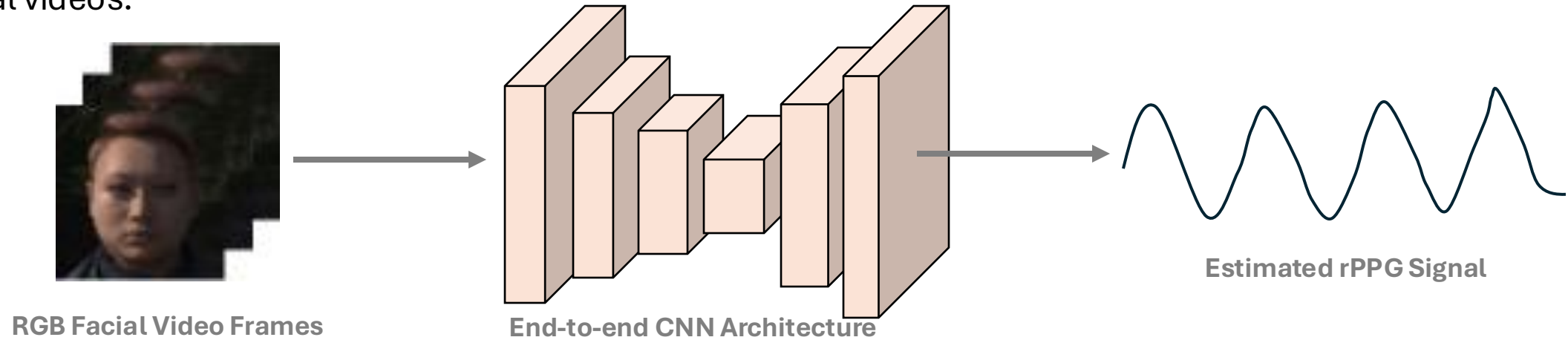
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# Remote Physiological Sensing

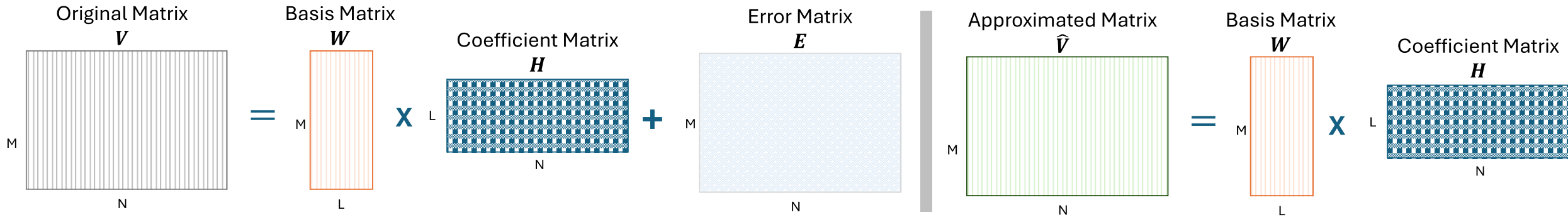
- ❖ Remote photoplethysmography (rPPG) enables non-invasive extraction of blood volume pulse (BVP) signals from facial videos.



- ❖ End-to-end estimation of BVP requires the network to selectively learn spatial-temporal features, while being invariant to head movement, lighting, and skin tones.
- ❖ Existing convolutional attention mechanisms derive attention in spatial, temporal, and channel dimensions disjointly.
- ❖ This highlights the complexity of this spatial-temporal task and presents a valuable opportunity to explore attention mechanisms within a multidimensional feature space.

# Nonnegative Matrix Factorization as Global Context Block

- ❖ Nonnegative matrix factorization (NMF) [1] is a dimensionality reduction paradigm that decomposes  $M \times N$  matrix  $V = [v_1, v_2, \dots, v_N] \in R_{\geq 0}^{M \times N}$  into nonnegative  $M \times L$  basis matrix  $W = [w_1, w_2, \dots, w_L] \in R_{\geq 0}^{M \times L}$  and nonnegative  $L \times N$  coefficient matrix  $H = [h_1, h_2, \dots, h_N] \in R_{\geq 0}^{L \times N}$ .



- ❖ A recent work formulated NMF as an approach to compute low-rank embeddings as a global context block [2], which was shown to be effective in semantic segmentation and image generation tasks.

- ❖ Our work focuses on deploying NMF as a multidimensional attention to learn robust spatial-temporal features, without reducing the tensor dimensions.

[1] Lee, D. D., & Seung, H. S. (1999). Learning the parts of objects by non-negative matrix factorization. *nature*, 401(6755), 788-791.

[2] Geng Z. et al., (2021), Is attention better than matrix decomposition? International Conference on Learning Representations.

[3] Hu, J., Shen, L., & Sun, G. (2018). Squeeze-and-excitation networks. In Proceedings of the IEEE conference on computer vision and pattern recognition (pp. 7132-7141).

# Factorized Self-Attention Module (FSAM)

❖ For rPPG estimation task, the spatial-temporal input data is expressed as  $\mathcal{J} \in R^{T \times C \times H \times W}$  where:

- $T$  = Total frames in a video
- $C$  = Channels in a frame (e.g. for RGB)
- $H$ , and  $W$  = Height and width

❖ Feature extractor generates voxel embeddings  $\varepsilon \in R^{\tau \times \kappa \times \alpha \times \beta}$ , with temporal ( $\tau$ ), channel ( $\kappa$ ) and spatial ( $\alpha, \beta$ ) dimensions.

❖  $\varepsilon$  is transformed to  $V^{st} \in R^{M \times N}$ , such that:

$$1 \quad V^{st} \in R^{M \times N} = \Gamma^{\tau \kappa \alpha \beta \mapsto MN} \left( \xi_{pre}(\varepsilon \in R^{\tau \times \kappa \times \alpha \times \beta}) \right) \\ \exists \kappa \times \alpha \times \beta \mapsto N; \tau \mapsto M$$

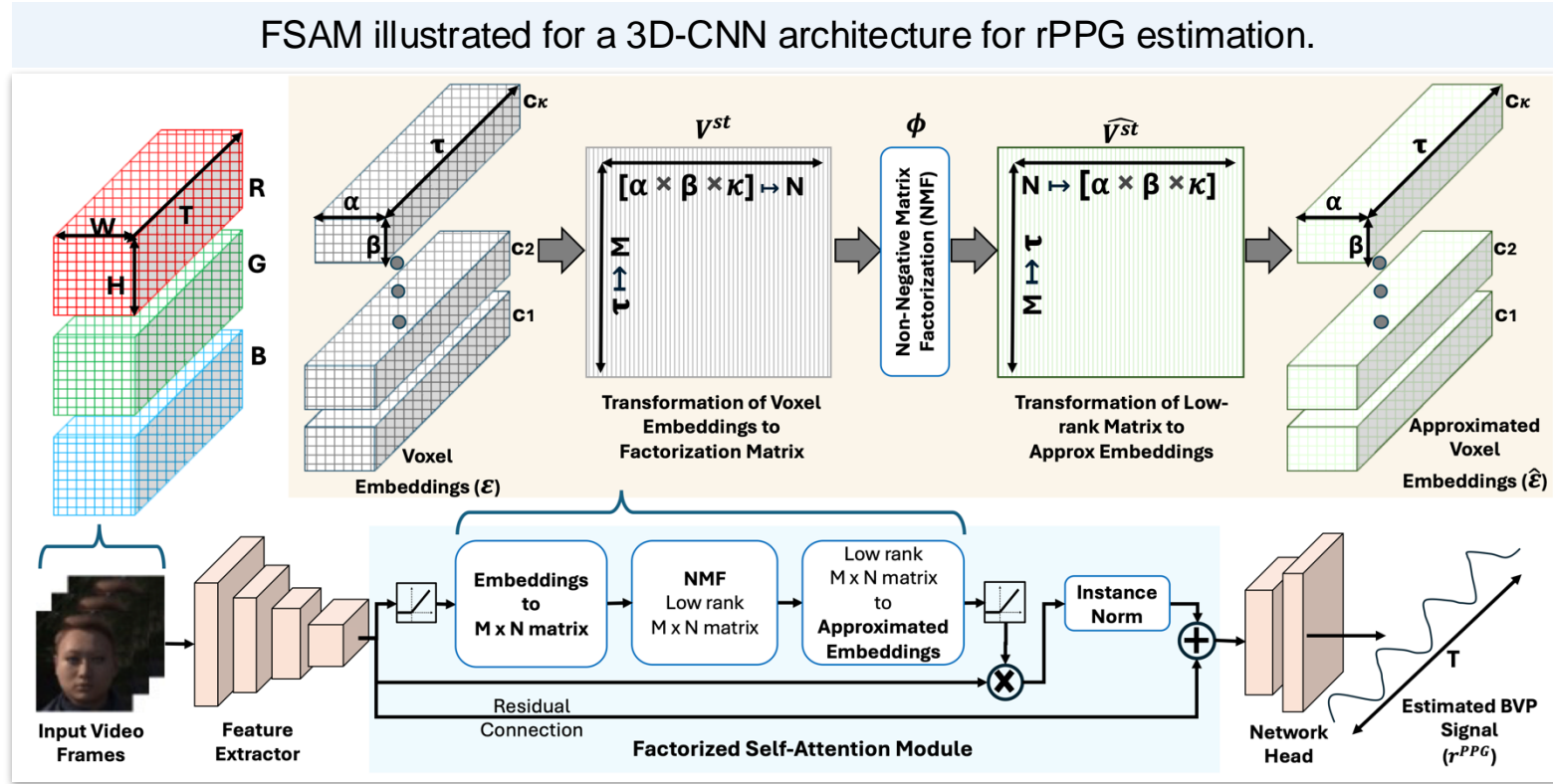
❖  $V^{st}$  is factorized, and remapped to embeddings dimension:

$$2 \quad \widehat{V}^{st} = \phi(V^{st})$$

$$3 \quad \hat{\varepsilon} = \Gamma^{MN \mapsto \tau \kappa \alpha \beta}(\widehat{V}^{st} \in R^{M \times N})$$

❖ Low rank  $\hat{\varepsilon}$  serves as an attention for rPPG estimation.

$$4 \quad r^{ppg} = \omega \left( \varepsilon + \mathcal{I}\mathcal{N} \left( \varepsilon \odot \xi_{post}(\hat{\varepsilon}) \right) \right)$$



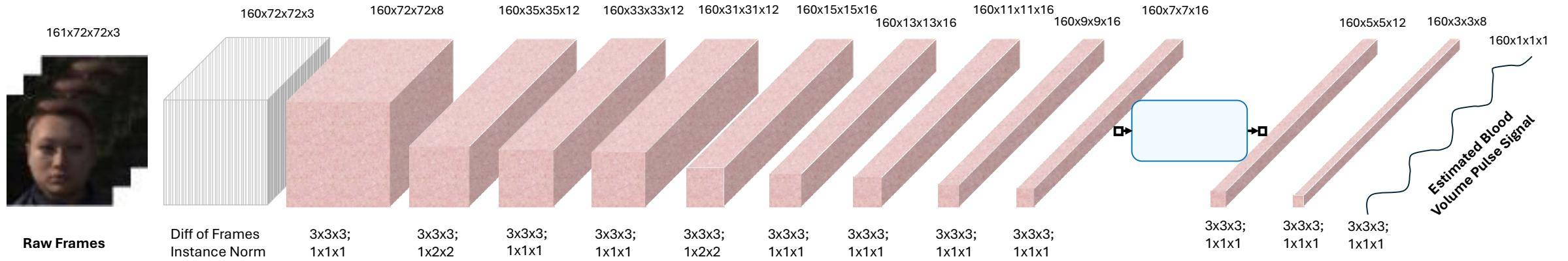
$\xi_{pre}, \xi_{post} = Conv$  layers

$\omega = Network$  Head

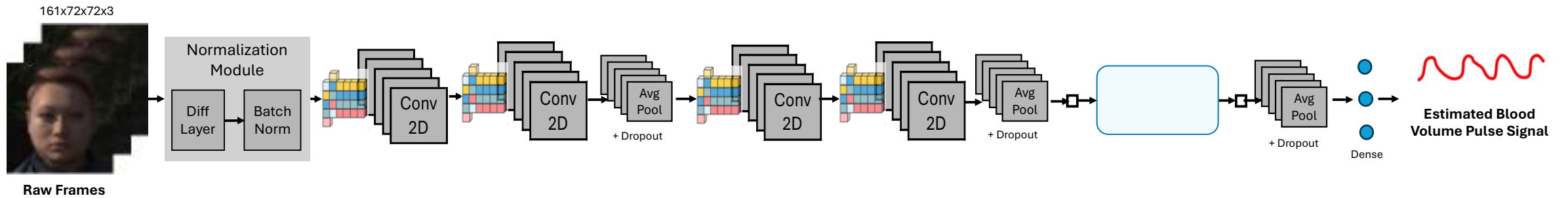
$\mathcal{I}\mathcal{N} = Instance$  Normalization

# FSAM Implemented for 3D-CNN and 2D-CNN Architectures

## FactorizePhys, Proposed 3D-CNN Architecture, that Implements FSAM



## Adaptation of FSAM for EfficientPhys [4], the SOTA 2D-CNN rPPG method



# Main Results

Cross-Dataset Evaluation on PURE Dataset							
Training Dataset	Model	Attention Module	MAE (HR) ↓	RMSE (HR) ↓	MAPE (HR) ↓	Corr (HR) ↑	SNR (BVP) ↑
iBVP	PhysNet	-	7.78	19.12	8.94	0.59	9.90
	PhysFormer	TD-MHSA	6.58	16.55	6.93	0.76	9.75
	EfficientPhys	SASN	0.56	1.40	0.87	0.998	11.96
	EfficientPhys	FSAM	<b>0.44</b>	<b>1.19</b>	<b>0.64</b>	<b>0.999</b>	12.64
	FactorizePhys	FSAM	0.60	1.70	0.87	0.997	<b>15.19</b>
SCAMPS	PhysNet	-	26.74	36.19	46.73	0.45	-2.21
	PhysFormer	TD-MHSA	16.64	28.13	30.58	0.51	0.84
	EfficientPhys	SASN	6.21	18.45	12.16	0.74	4.39
	EfficientPhys	FSAM	8.03	19.09	15.12	0.73	3.81
	FactorizePhys	FSAM	<b>5.43</b>	<b>15.80</b>	<b>11.1</b>	<b>0.80</b>	<b>11.40</b>
UBFC-rPPG	PhysNet	-	10.38	21.14	20.91	0.66	11.01
	PhysFormer	TD-MHSA	8.90	18.77	17.68	0.71	8.73
	EfficientPhys	SASN	4.71	14.52	7.63	0.80	8.77
	EfficientPhys	FSAM	3.69	13.27	5.85	0.83	9.65
	FactorizePhys	FSAM	<b>0.48</b>	<b>1.39</b>	<b>0.72</b>	<b>0.998</b>	<b>14.16</b>

TD-MHSA: Temporal Difference Multi-Head Self-Attention [5]; SASN: Self-Attention Shifted Network [4]

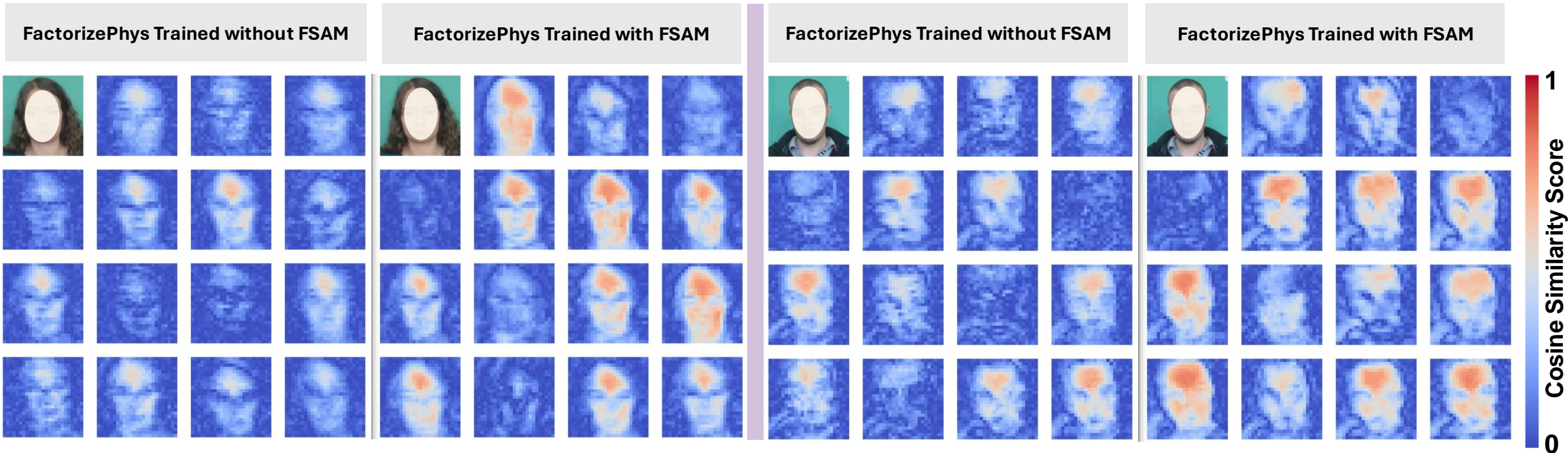
❖ For complete set of main and supplementary results on multiple datasets, please visit our paper.

[4] Liu, et al., (2023). Efficientphys: Enabling simple, fast and accurate camera-based cardiac measurement. WACV (pp. 5008-5017).

[5] Yu et al., (2022). Physformer: Facial video-based physiological measurement with temporal difference transformer. CVPR(pp. 4186-4196).



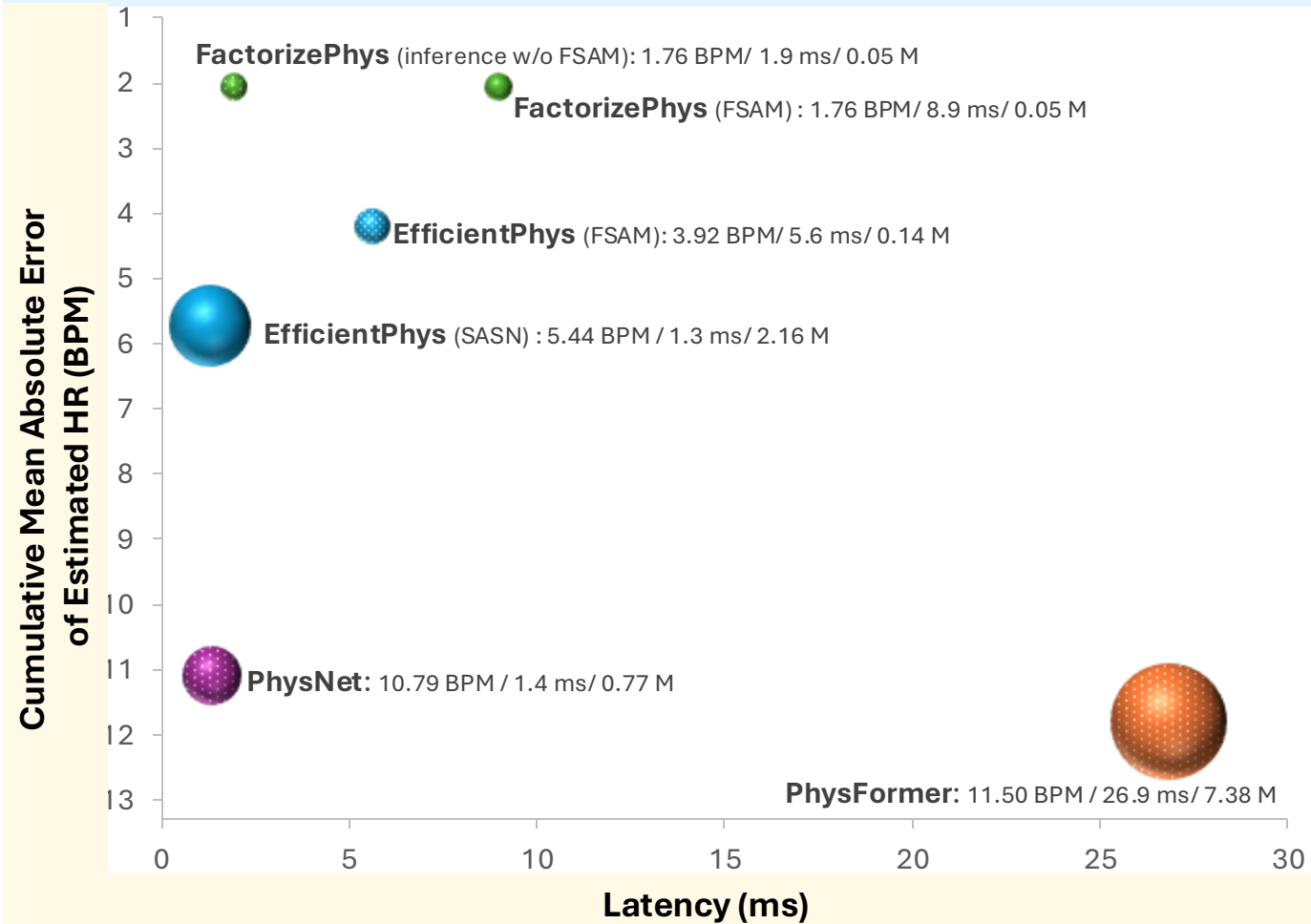
# Learned Spatial Temporal Features



Each tile represents cosine similarity (CSIM) map computed between the ground-truth PPG signal and the temporal dimension of each channel of the embedding layer. The magnitude and spatial spread of CSIM scores, as depicted with the heatmaps, highlight the effectiveness of the FSAM.

# Summarized Performance on Multiple rPPG Datasets

## Cumulative Cross-dataset Performance v/s Latency Plot



Sphere Size  $\propto$  No. of parameters

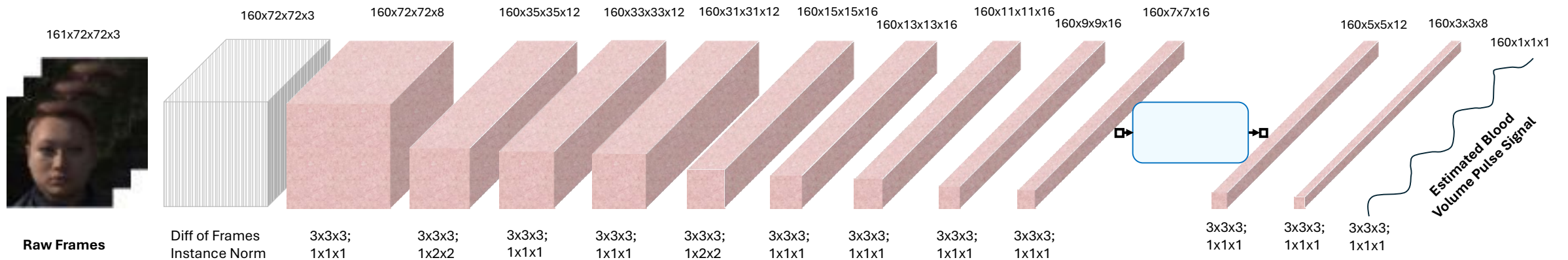
Model: MAE/ Latency/ No. of parameters



# Conclusion

- ❖ FactorizePhys, equipped with FSAM, provides robust cross-dataset generalization for the extraction of rPPG signals.
- ❖ FSAM serves as an efficient multi-dimensional attention mechanism for remote physiological sensing, with potential applicability to other spatial-temporal downstream tasks.

## FactorizePhys with FSAM



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❖ Code: <https://github.com/PhysiologicAllab/FactorizePhys>

