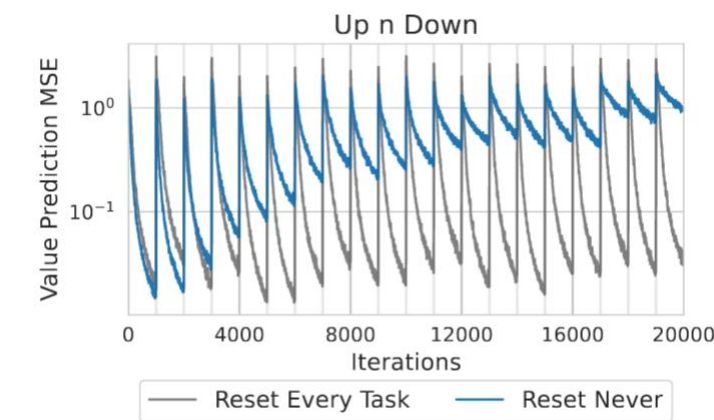


## Introduction

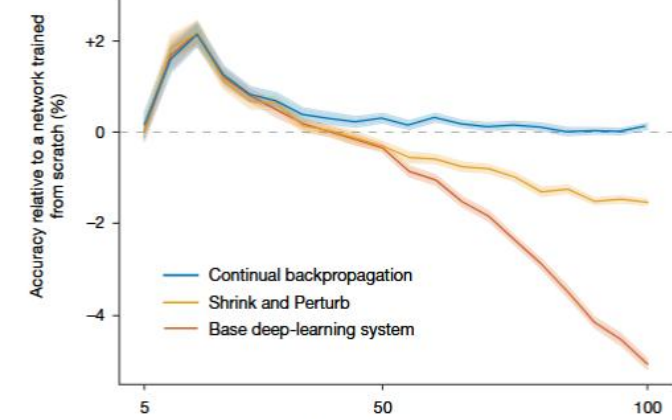
### Loss of Plasticity in Deep Continual Learning

#### Reinforcement Learning



Nikishin et. al., 2023

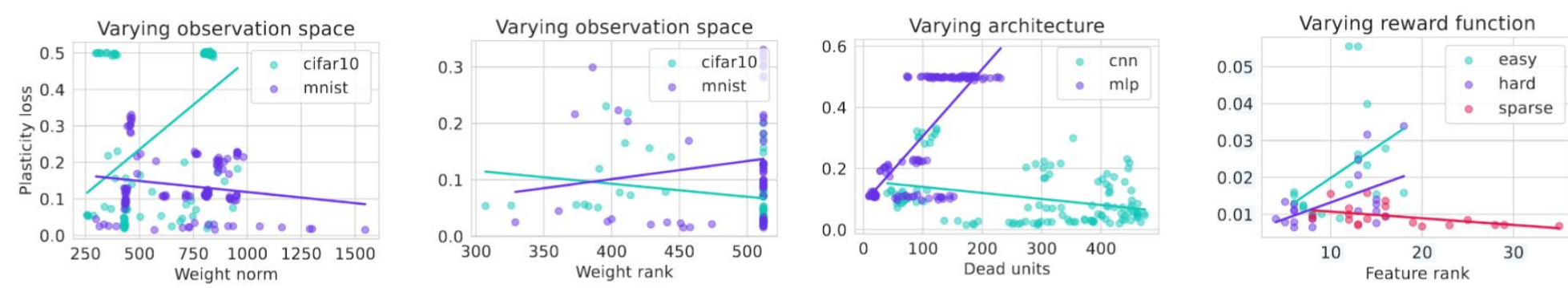
#### Continual Learning



Dohare et. al., 2024

**Loss of plasticity** is a widely observed phenomenon in both continual learning and RL. It refers to the degradation of performance on new tasks, which eventually prevents the system from learning continuously.

Potential factors of LoP are Inconclusive and Indirect

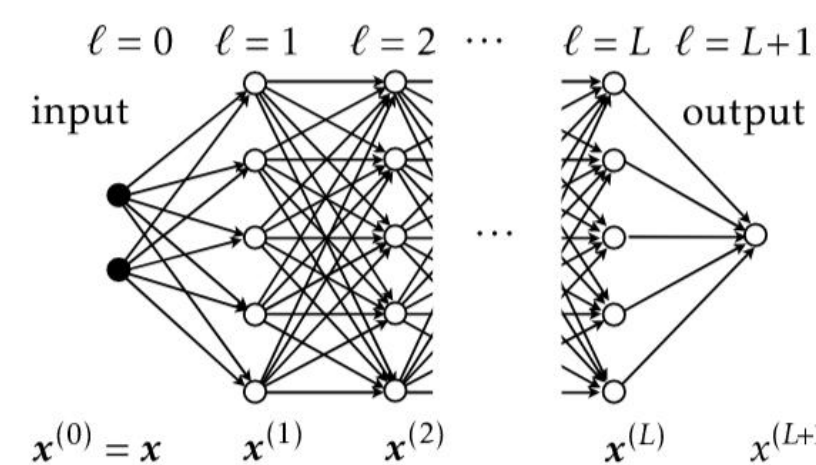


Lyle et. al., 2023

A more comprehensive understanding of LoP is in need.

## Preliminary

### A Framework Combining FTLE and UFM



Finite Time Lyapunov Exponent:

$$\delta x^{(\ell)} = \mathbb{J}_{\ell} \delta x \quad \lambda_1^{(\ell)}(x) \equiv \ell^{-1} \log \Lambda_1^{(\ell)}(x)$$

L. Storm et. al., 2024

(NC1) Variability collapse:  $\Sigma_W \rightarrow 0$ .  
(NC2) Convergence to simplex ETF:

$$\begin{aligned} \|\mu_c - \mu_G\|_2 - \|\mu_{c'} - \mu_G\|_2 &\rightarrow 0 \quad \forall c, c' \\ \langle \tilde{\mu}_c, \tilde{\mu}_{c'} \rangle &\rightarrow \frac{C}{C-1} \delta_{c,c'} - \frac{1}{C-1} \quad \forall c, c'. \end{aligned}$$

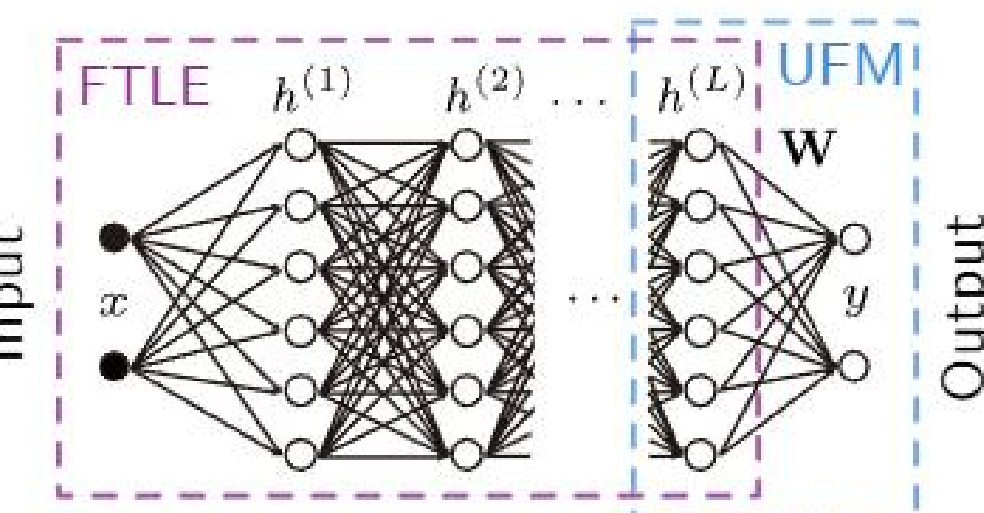
(NC3) Convergence to self-duality:

$$\left\| \frac{W^T}{\|W\|_F} - \frac{\tilde{M}}{\|\tilde{M}\|_F} \right\|_F \rightarrow 0.$$

(NC4) Simplification to NCC:

$$\arg \max_{c'} \langle w_{c'}, h \rangle + b_{c'} \rightarrow \arg \min_{c'} \|h - \mu_{c'}\|_2,$$

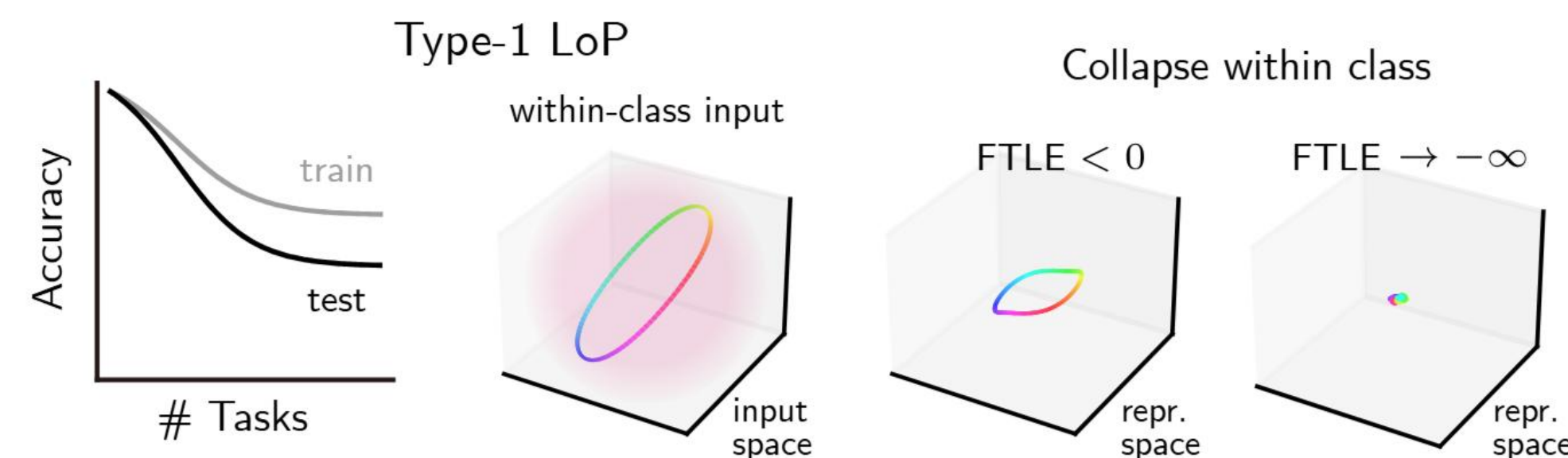
Vardan Papyan et al. 2020



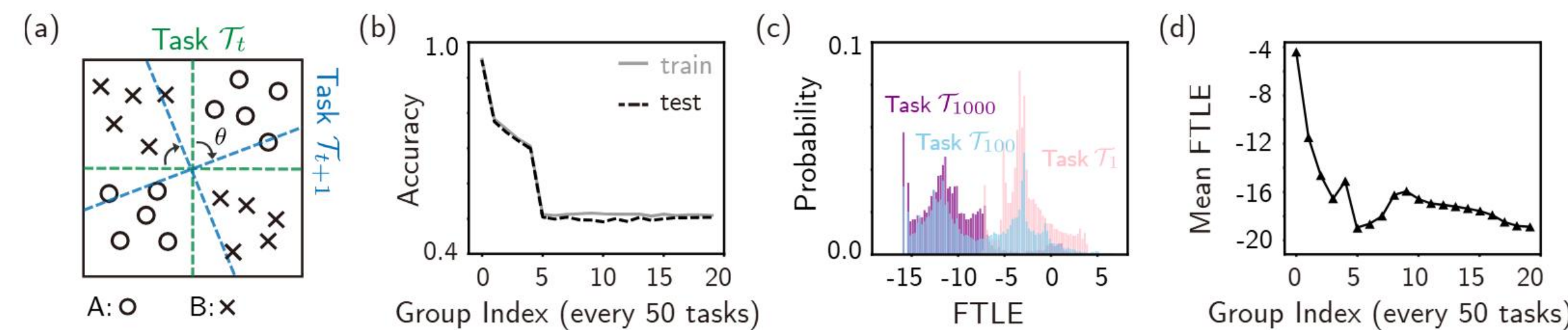
**FTLE** quantifies how the mapping properties of neural networks from the input layer to the representation layer evolve during training, while **UFM** offers analytical tractability for optimization in the representation space.

## Dissection

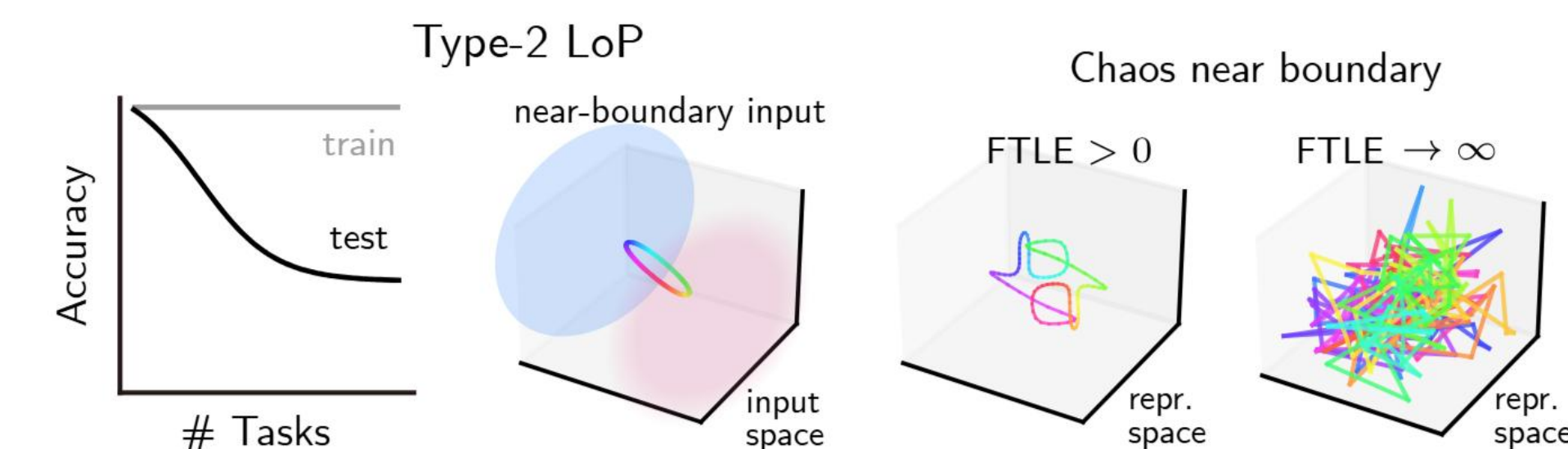
- We identify the existence of **two subtypes of LoP**. On the level of task performance, they only **differ in training accuracy**.
- We unveil that the causes of the two LoP subtypes are exactly opposite: **collapse of representation vs. chaotic behavior**.



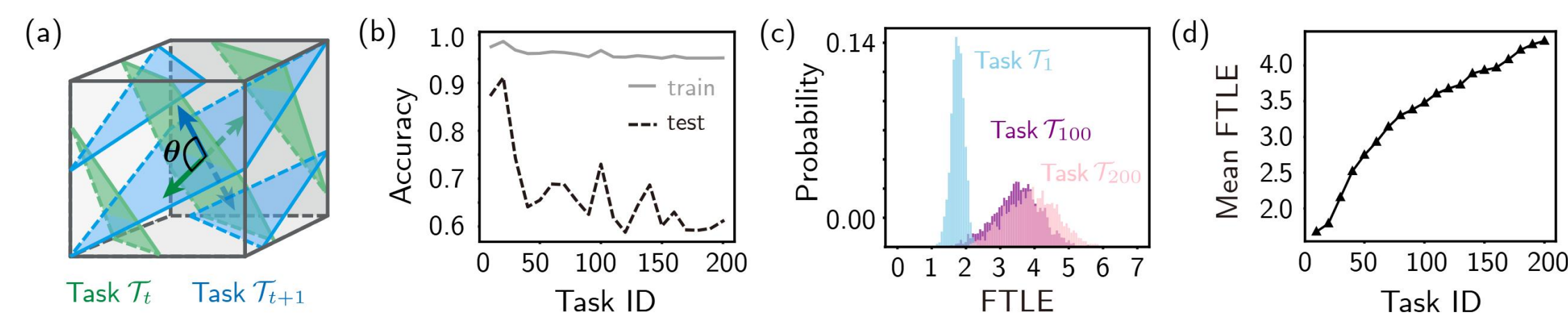
### Type-1 LoP: the Collapse of Representation Space



**Type-1 LoP:** Learning causes within-class regions to collapse progressively. These collapsed areas accumulate during continual learning. Type-1 LoP occurs when representations of a new task approach these collapsed regions, characterized by **highly negative FTLEs**. Both training and test accuracies drop sharply, indicating a loss of capacity in learning.

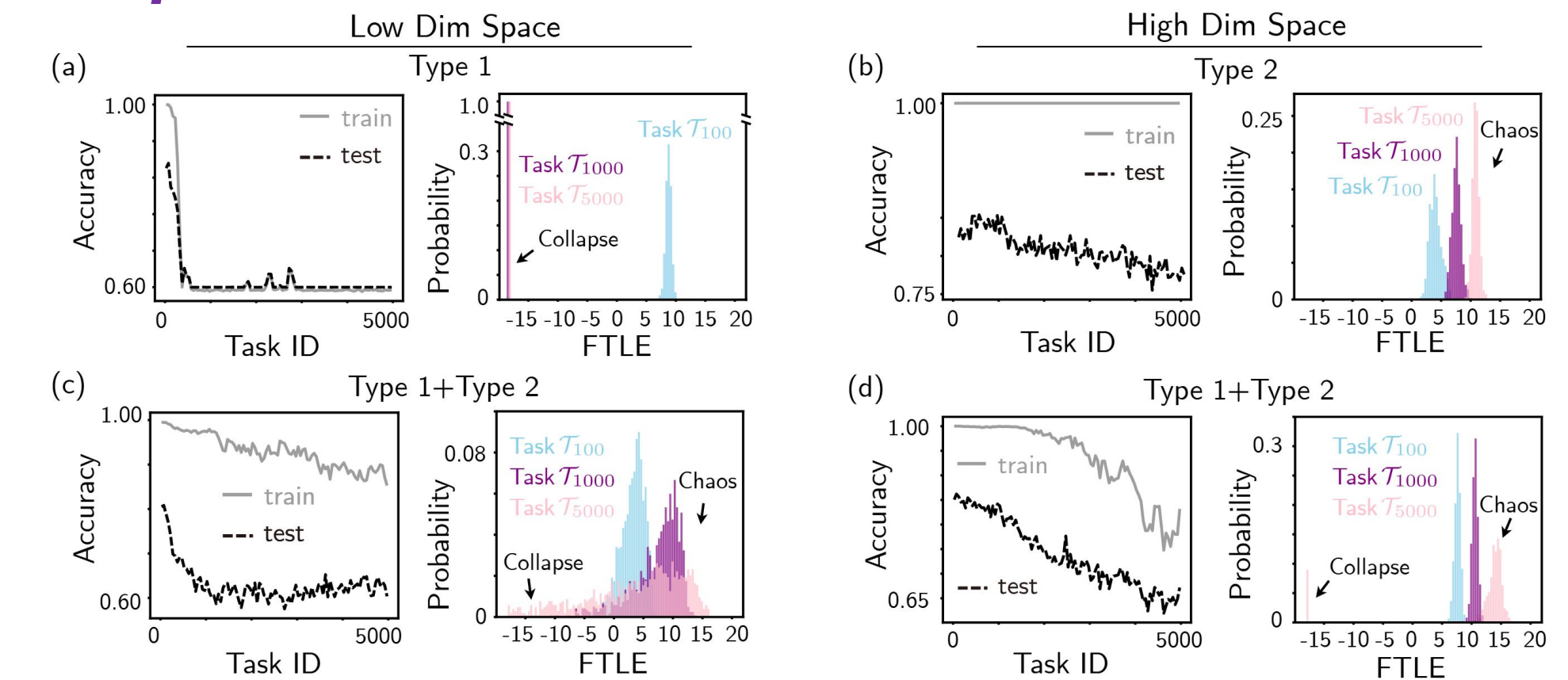


### Type-2 LoP : Over-stretched Boundaries and Chaotic Behaviors



**Type-2 LoP:** Learning causes inter-class regions to expand progressively. These expansions accumulate during continual learning. Type-2 LoP occurs when representations of a new task approach these overly stretched regions in representation space, characterized by **highly positive FTLEs**. Training accuracy remains high due to the chaotic and over-expressive representation space, while test accuracy degrades, indicating a loss of capacity to generalize.

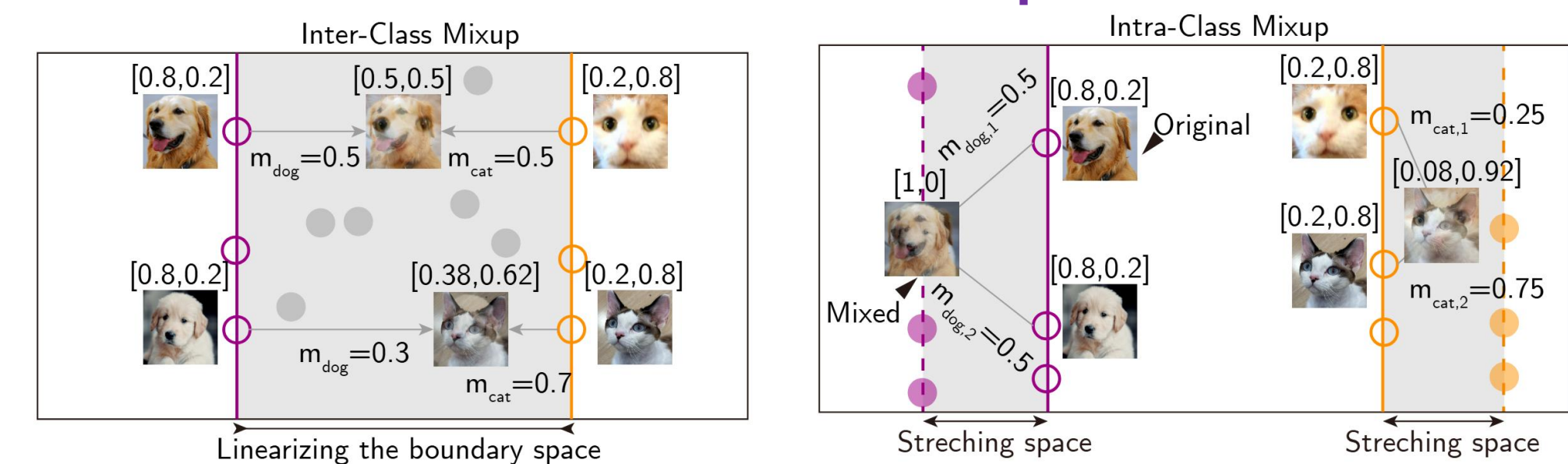
## Experiments



- Both types of LoP exist in real datasets and they can impair task performance simultaneously.

## Mitigation

### Generalized Mixup



$$\begin{aligned} x^m &= mx^K + (1-m)x^{K'}, \\ y^m &= my^K + (1-m)y^{K'} \end{aligned}$$

$$\begin{aligned} y_K^m &= y^K + \frac{M}{2} - M|0.5 - m| \\ y_{K'}^m &= y^{K'} - \frac{M}{2} + M|0.5 - m| \end{aligned}$$

- Classical Mixup** (Inter-Class) suppresses Type-2 LoP by **linearizing the decision boundaries**.
- Generalized Mixup** (Intra-Class) mitigates Type-1 LoP by **expanding the intra-class representation**.

### Verified in Continual Imagenet Benchmark

Table 1: SmallConv Acc. on Continual ImageNet

Task ( $\times 1000$ )	0-1	1-2	2-3	3-4	4-5
No Intv.	0.817	0.805	0.562	0.500	0.500
Retrained	0.853	0.845	0.845	0.840	0.840
L2 init	0.804	0.796	0.786	0.785	0.788
Layernorm	0.753	0.760	0.759	0.751	0.751
CBP	0.834	0.847	0.846	0.847	0.857
G-mixup[ours]	<b>0.866</b>	<b>0.881</b>	<b>0.885</b>	<b>0.880</b>	<b>0.879</b>

Table 2: ConvNet Acc. on Continual ImageNet

Task ( $\times 1000$ )	0-1	1-2	2-3	3-4	4-5
No Intv.	0.794	0.778	0.604	0.537	0.500
Retrained	0.857	0.851	0.850	0.849	0.846
L2 init	0.814	0.805	0.800	0.803	0.807
Layernorm	0.782	0.768	0.752	0.749	0.755
CBP	0.848	0.867	0.864	0.863	0.878
G-mixup[ours]	<b>0.875</b>	<b>0.896</b>	<b>0.899</b>	<b>0.894</b>	<b>0.896</b>

**G-Mixup** consistently outperforms other methods across tasks and settings, demonstrating superior capacity to preserve plasticity over long task sequences.

## Acknowledgment

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