

# DynSep:

## Dynamic Configuration for Cutting Plane Separators via Reinforcement Learning on Incremental Graph

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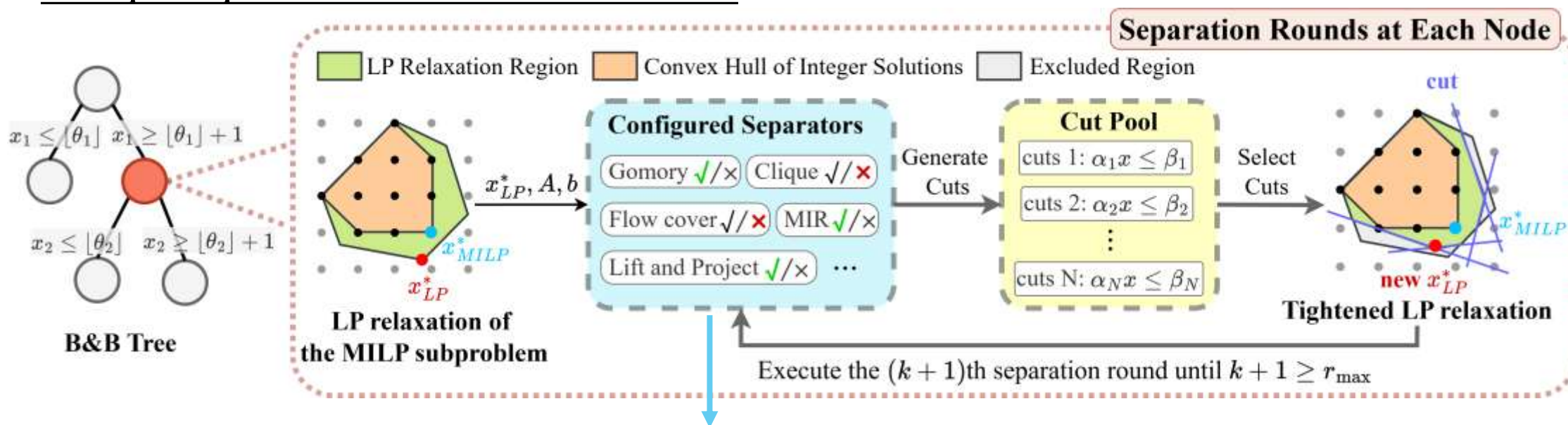
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## Background: How Cuts Are Born in MILP Solver

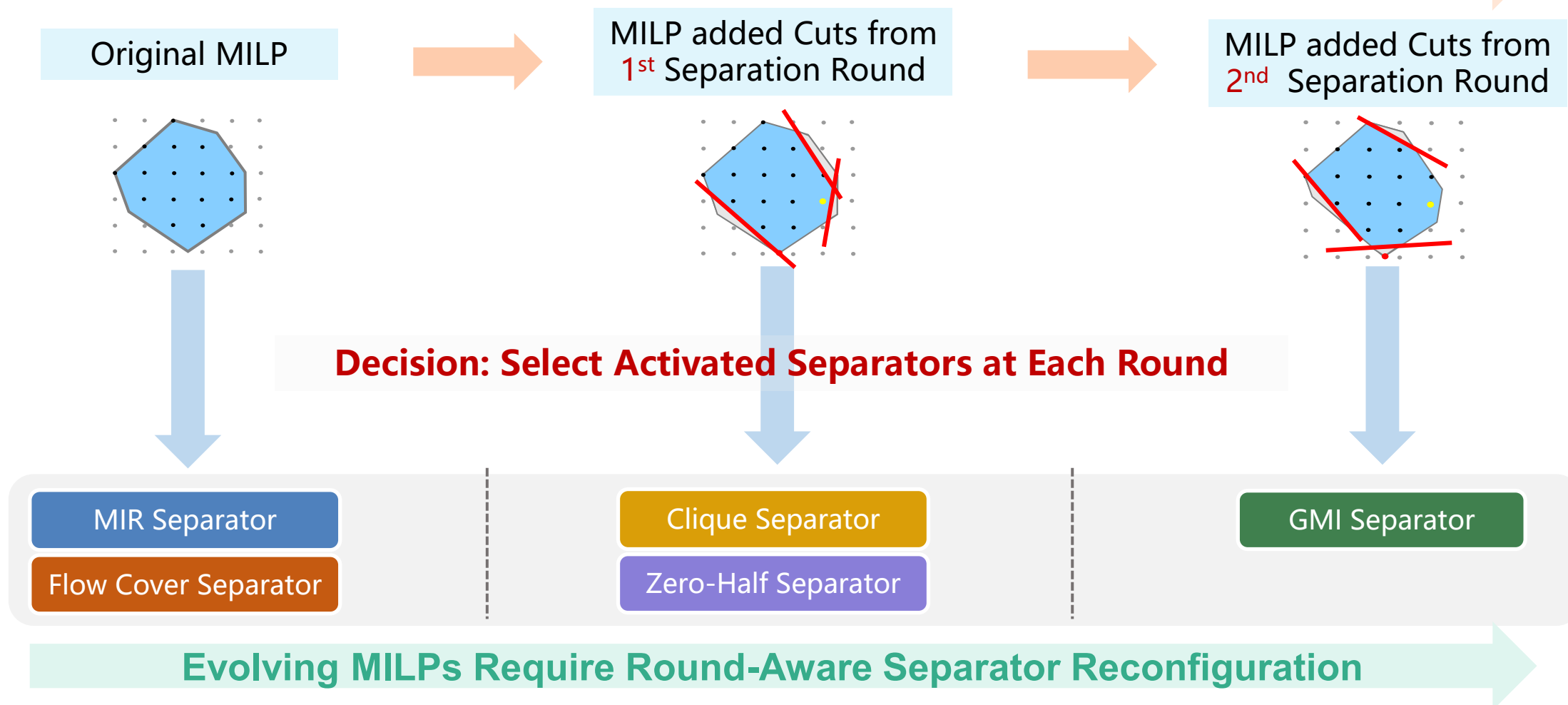
- Cutting planes (cuts) are essential for solving **mixed-integer linear programming (MILP)** problems, as they tighten the feasible solution space and accelerate the solving process.
- Separators: **cutting plane algorithms** built in MILP solver (e.g., Gomory cuts, Clique cuts).
- Separator configuration: Determine which separators to activate and how aggressively to activate. The configuration of separators determines the quality of candidate cuts and thus the solver's convergence behavior.
- Multiple Separation Rounds in MILP Solver:



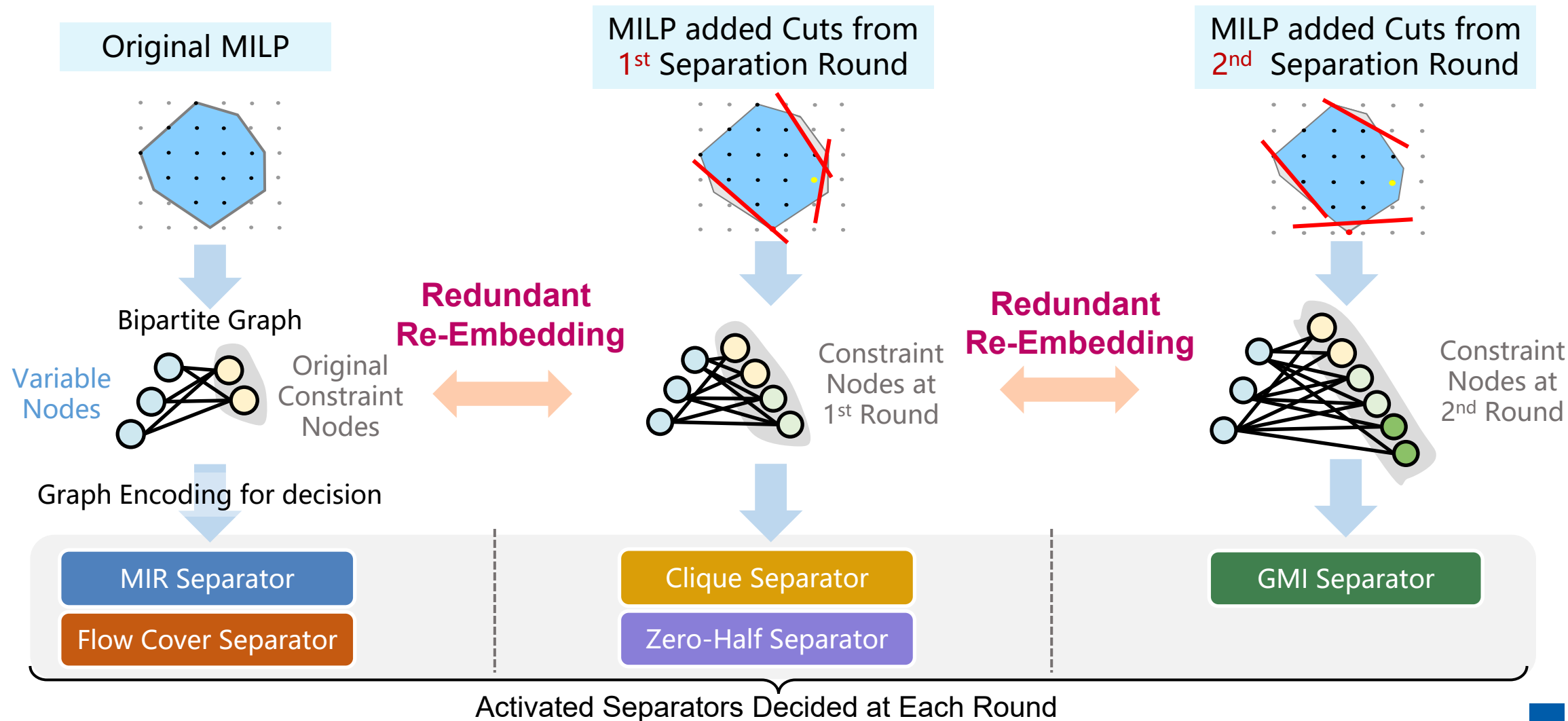
**Separator Set** ( ✓ : activate ✗ : deactivate)

## Motivation: The Optimal Separators Choice Keep Changing

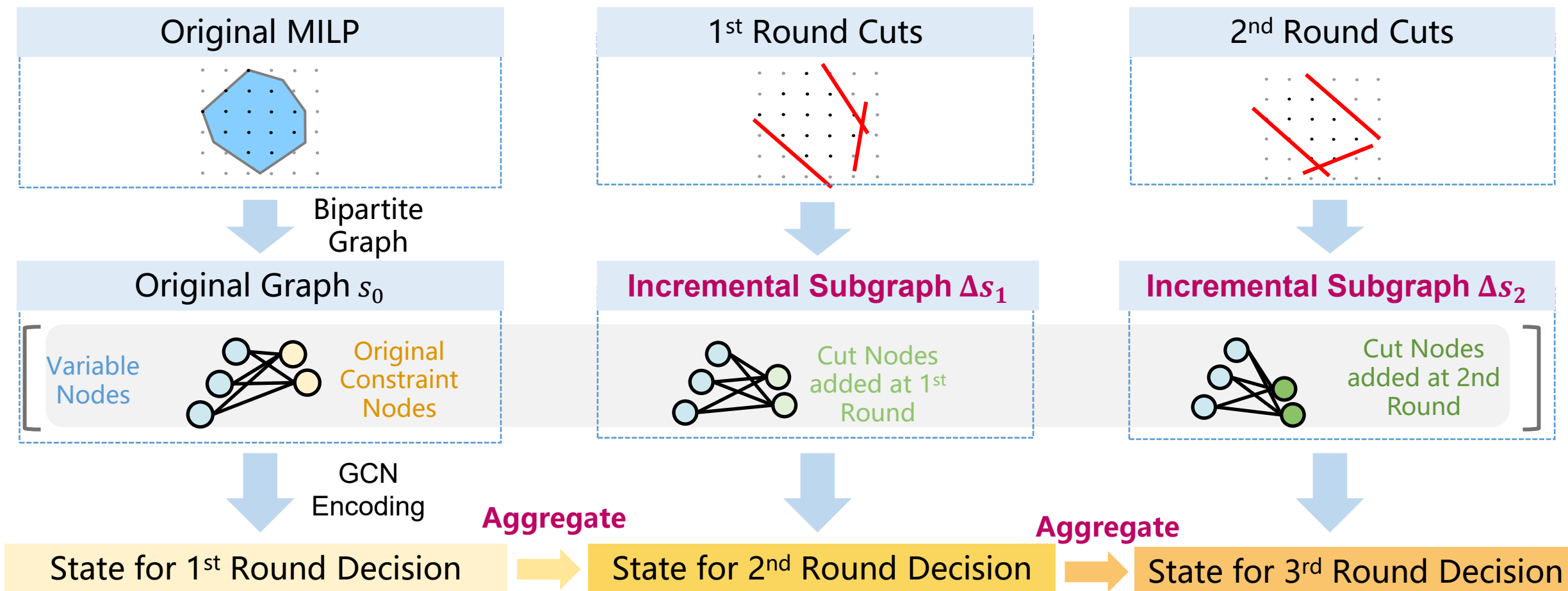
Cut passes induce the evolving MILPs...



## Motivation: Evolving Graph & Redundant Re-Embedding



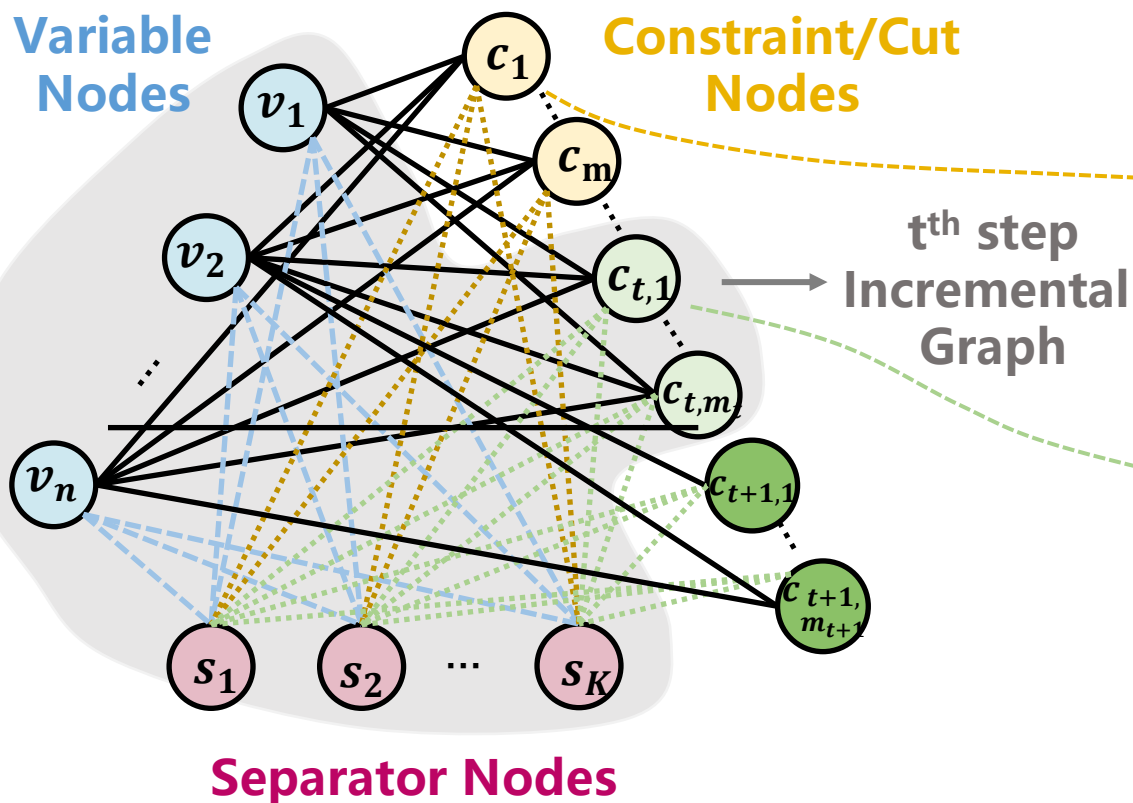
## Insight: Computing the Incremental Graph at each decision



Aggregate current-round incremental changes with history to form the full decision state

## Method-Step 1: Triplet Graph Modeling

Incremental Triplet Graph  
updated by iteratively added cuts



$$\delta_1: a_{11}x_1 + \cdots + a_{1n}x_n \leq b_1$$

$$\delta_m: a_{m1}x_1 + \cdots + a_{mn}x_n \leq b_m$$

$m$  rows of  
original  
constraints

$$\delta_{t,1}: a_{(t,1),1}x_1 + \cdots + a_{(t,1),n}x_n \leq b_{t,1}$$

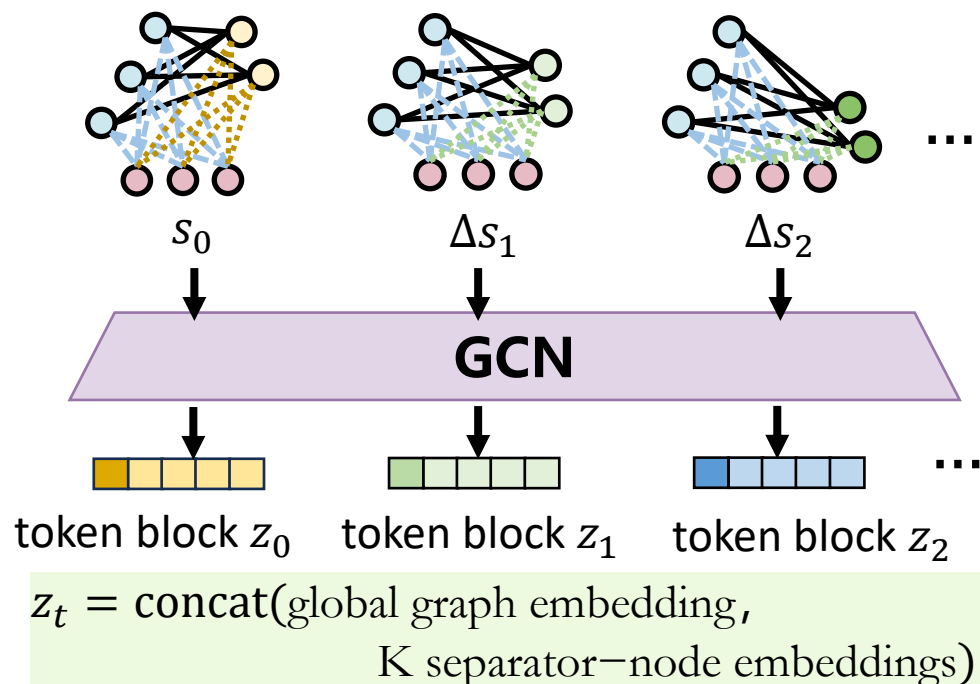
$$\delta_{t,m_t}: a_{(t,m_t),1}x_1 + \cdots + a_{(t,m_t),n}x_n \leq b_{t,m_t}$$

Newly  
added  
cuts at  $t$ -th  
round

$$x_i \in \mathbb{Z}, \forall i \in I$$

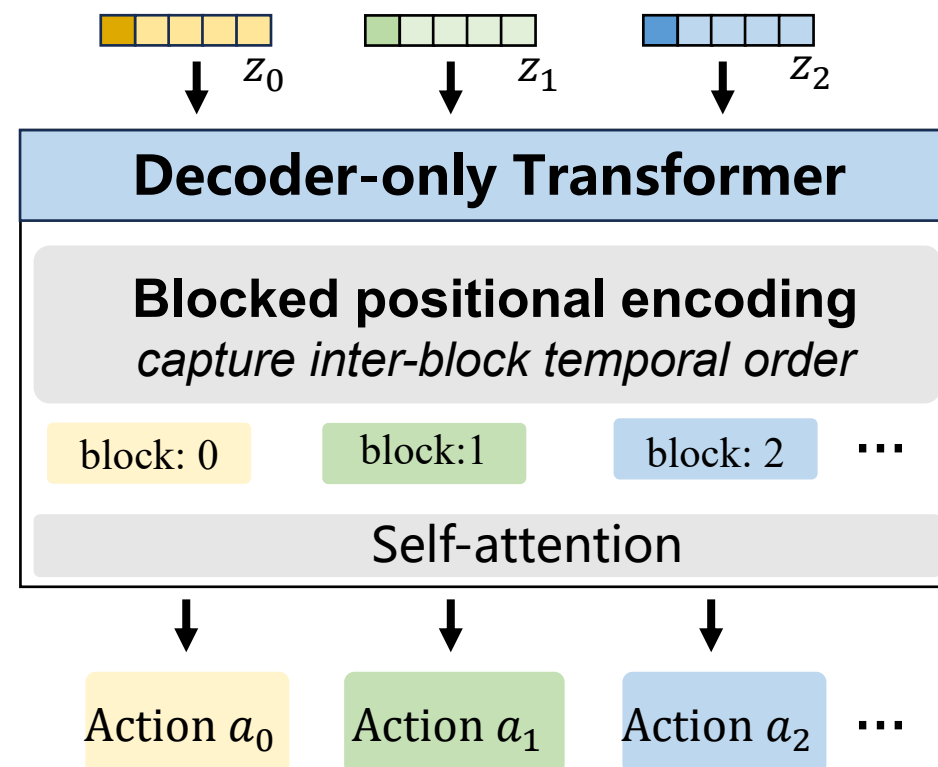
## Method-Step 2: Sequential Encoding & Tokenizer the Incremental Graph

- Encode each round's incremental subgraph as a **token block** and arrange a temporal token sequence



Token sequence:  $\langle z_0, z_1, z_2, \dots \rangle$

- Autoregressive decision model with blocked PE;
- captures inter-block order and retains **permutation equivariance** inside each block



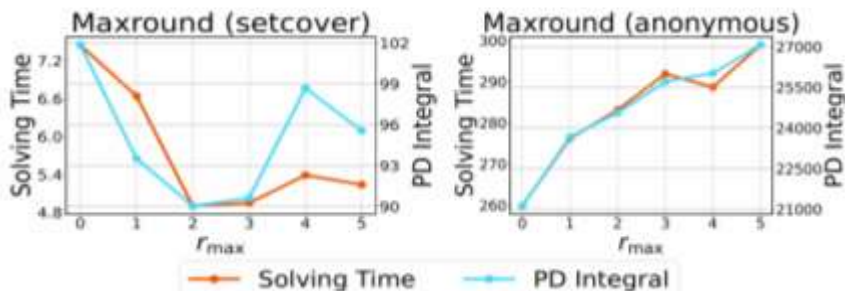


## Method-Step 3: Decision Modeling

➤ Evolving MILPs Require **Round-Aware** Separator configuration:

### 1 Decide when to stop separation round:

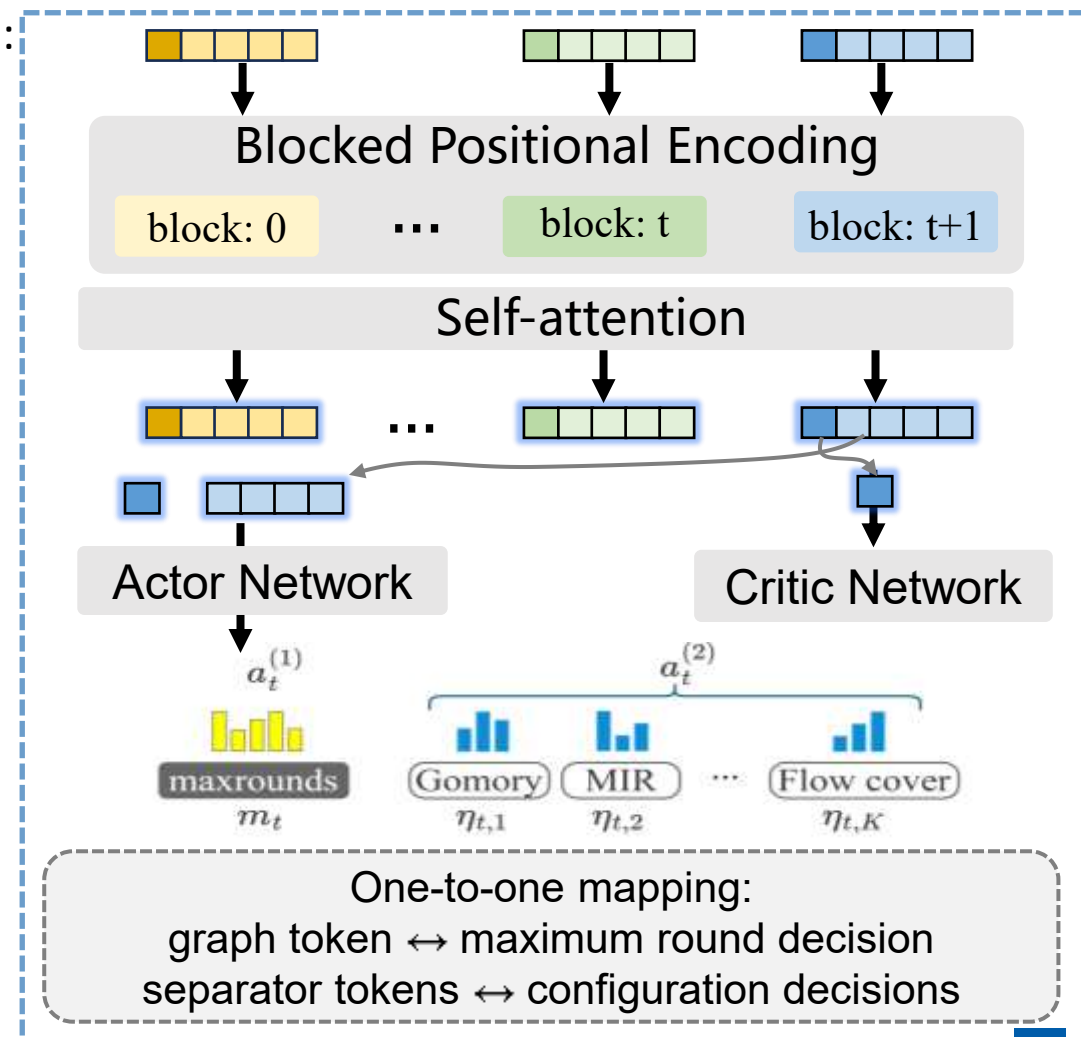
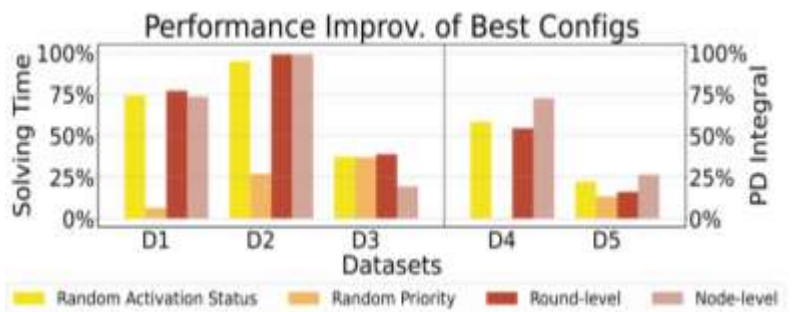
Performance is highly sensitive to  $r_{\max}$ ; More rounds do not necessarily perform better.



### 2

### Decide which separators to activate:

Proper round-aware configurations yield obvious performance gains.





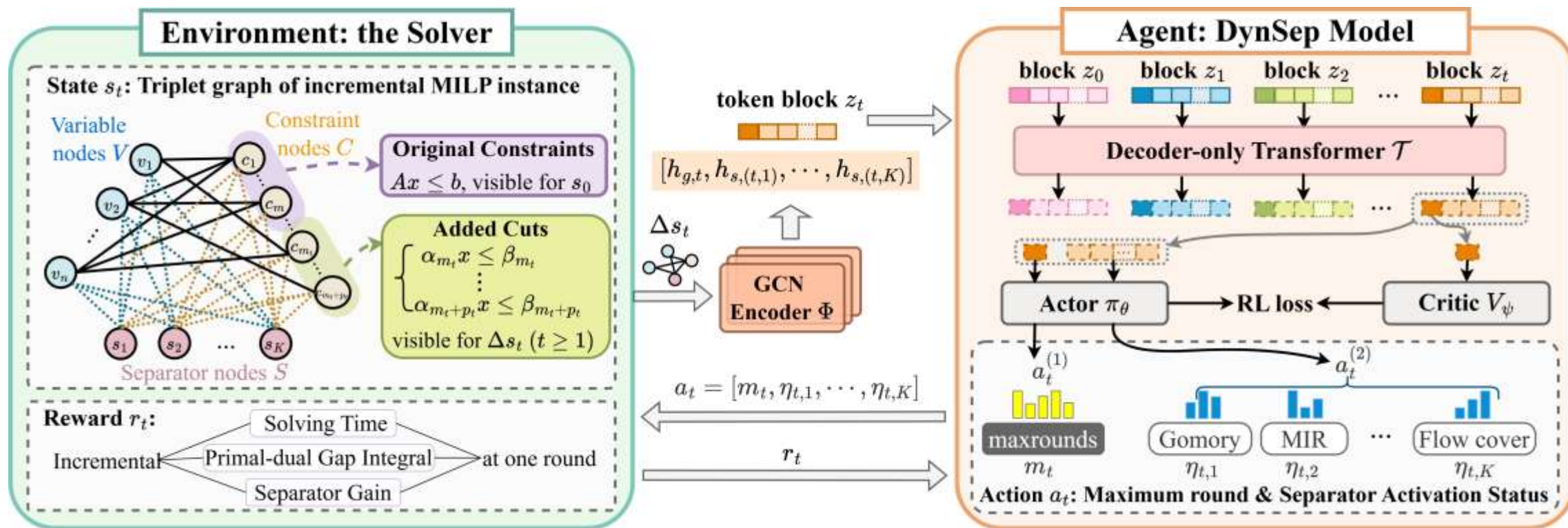


Table 1: **Comparative evaluation on easy, medium, and hard datasets.** Best performance is in bold, with the greatest improvement (Improv.) both bolded and underlined. Sizes of nine benchmarks are in parentheses, with  $n$  and  $m$  representing the average numbers of variables and constraints, respectively. The values report the mean (standard deviation) of time and PD integral metrics.

Easy: Set Covering ( $n = 1000, m = 500$ )				Easy: Max Independent Set ( $n = 500, m = 1953$ )			Easy: Multiple Knapsack ( $n = 720, m = 72$ )		
Method	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓
NoCuts	7.45 (5.87)	NA	101.86 (55.59)	15.32 (5.82)	NA	146.4 (56.99)	13.84 (28.79)	NA	25.21 (26.6)
Default	5.24 (1.79)	29.66	95.56 (36.86)	30.4 (8.02)	-98.43	289.51 (103.81)	2.01 (1.82)	85.48	18.6 (10.49)
Search(50)	1.7 (0.44)	77.18	36.77 (8.48)	4.42 (3.89)	71.15	23.28 (19.02)	4.12 (5.52)	70.23	13.38 (7.36)
Prune	7.45 (5.14)	0.00	66.83 (45.97)	5.03 (3.18)	67.17	30.93 (22.39)	0.64 (0.48)	95.38	9.89 (3.82)
L2Sep(R1)	6.56 (4.35)	11.95	62.12 (39.08)	5.42 (3.86)	64.62	34.21 (25.97)	7.45 (12.07)	46.17	12.99 (8.66)
L2Sep(R2)	7.35 (4.88)	1.34	70.00 (43.57)	5.36 (3.76)	65.01	33.94 (25.33)	9.14 (12.89)	33.96	14.40 (8.72)
LLM4Sepasel	11.73 (12.09)	-57.45	110.73 (91.14)	5.13 (4.19)	66.51	27.18 (20.17)	4.8 (5.51)	65.32	17.79 (8.9)
DynSep (Ours)	1.51 (0.27)	79.73	33.88 (9.34)	0.53 (0.20)	96.54	9.66 (2.40)	0.52 (0.24)	96.24	9.71 (5.39)

Medium: Corlat ( $n = 466, m = 486$ )				Medium: MIK ( $n = 413, m = 346$ )			Hard: Anonymous ( $n = 37881, m = 49603$ )		
Method	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓	Time(s) ↓	PD integral ↓	Improv. ↑ (PD Int., %)
NoCuts	74.66 (122.23)	NA	2687.68 (6209.48)	190.28 (113.97)	NA	887.85 (859.76)	259.77 (75.71)	21117.12 (9234.01)	NA
Default	111.55 (132.19)	-49.41	10573.14 (13070.46)	16.65 (18.06)	91.25	82.80 (56.24)	298.92 (4.09)	27069.58 (4892.8)	-28.19
Search(50)	55.74 (97.19)	25.34	2910.77 (6585.5)	24.99 (20.56)	86.87	89.27 (55.85)	270.68 (65.52)	24028.68 (9007.57)	-13.79
Prune	89.09 (125.52)	-19.33	2615.71 (5814.74)	300.01 (0.0)	-57.67	2237.28 (1023.8)	241.75 (100.61)	17304.91 (9563.3)	18.05
L2Sep(R1)	91.14 (124.12)	-22.07	3124.07 (6914.50)	15.50 (17.60)	91.85	61.09 (44.50)	239.52 (94.82)	16970.35 (10108.40)	19.64
L2Sep(R2)	89.84 (124.30)	-20.33	3113.29 (6927.16)	11.13 (9.09)	94.15	44.69 (25.06)	240.54 (93.80)	16850.57 (10052.83)	20.20
LLM4Sepasel	64.03 (110.63)	14.24	2921.73 (6860.21)	17.94 (17.76)	90.57	85.66 (65.34)	284.57 (34.79)	25384.48 (8100.56)	-20.21
DynSep (Ours)	22.96 (38.93)	69.25	2233.42 (3868.43)	10.99 (9.44)	94.22	134.15 (44.21)	241.89 (100.75)	15656.7 (8996.14)	25.86

Hard: Load Balancing ( $n = 61000, m = 64304$ )				Hard: MIPLIB mixed neos ( $n = 6958, m = 5660$ )			Hard: MIPLIB mixed supportcase ( $n = 19766, m = 19910$ )		
Method	Time(s) ↓	PD integral ↓	Improv. ↑ (PD Int., %)	Time(s) ↓	PD integral ↓	Improv. ↑ (PD Int., %)	Time(s) ↓	PD integral ↓	Improv. ↑ (PD Int., %)
NoCuts	300.11 (0.02)	15093.26 (940.68)	NA	275.04 (43.23)	14618.53 (12214.63)	NA	181.26 (120.25)	12959.99 (10506.47)	NA
Default	300.14 (0.02)	15187.19 (936.38)	-0.62	282.98 (29.49)	18500.5 (9386.15)	-26.56	244.75 (105.8)	21561.09 (10434.42)	-66.37
Search(50)	300.04 (0.05)	3783.52 (448.59)	74.93	274.23 (44.64)	15619.98 (11969.47)	-6.85	133.36 (131.32)	10241.17 (10794.69)	20.98
Prune	300.07 (0.12)	10597.31 (671.55)	29.79	249.37 (87.7)	14464.45 (12569.32)	1.05	158.63 (141.48)	9827.52 (11433.13)	24.17
L2Sep(R1)	300.02 (0.03)	10548.89 (4474.08)	30.11	242.83 (99.02)	10383.49 (11808.13)	28.97	162.18 (138.25)	11318.55 (11796.53)	12.67
L2Sep(R2)	300.03 (0.10)	10860.13 (4348.96)	28.05	242.90 (98.90)	13989.09 (12116.88)	4.31	166.23 (134.71)	11489.15 (11849.13)	11.35
LLM4Sepasel	300.04 (0.06)	4769.47 (709.05)	68.40	276.34 (47.32)	14109.36 (13706.18)	3.48	256.48 (100.88)	22618.21 (10234.21)	-74.52
DynSep (Ours)	300.04 (0.08)	3720.26 (499.37)	75.35	235.19 (112.26)	8511.58 (12413.9)	41.78	132.50 (130.32)	9212.24 (9840.56)	28.92

- **64%** time speed-up on easy/medium datasets
- **16%** PD-integral reduction on hard datasets

Table 2: Ablation study comparing five variants of DynSep on three datasets.

	Easy: Multiple Knapsack ( $n = 720, m = 72$ )			Medium: Corlat ( $n = 466, m = 486$ )			Hard: MIPLIB mixed neos ( $n = 6958, m = 5660$ )		
Method	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓	Time(s) ↓	PD integral ↓	Improv. ↑ (PD Int., %)
NoCuts	13.84 (28.79)	NA	25.21 (26.6)	74.66 (122.23)	NA	2687.68 (6209.48)	275.04 (43.23)	14618.53 (12214.63)	NA
Default	2.01 (1.82)	85.48	18.6 (10.49)	111.55 (132.19)	-49.41	10573.14	282.98 (29.49)	18500.5 (9386.15)	-26.56
w/o MaxR	0.67 (0.46)	95.16	10.07 (5.35)	28.28 (53.99)	62.12	2688.01 (5424.21)	263.63 (63.0)	9029.4 (12114.3)	38.23
w/o TF	0.64 (0.53)	95.38	9.82 (5.24)	25.82 (61.58)	65.42	2552.91 (6146.98)	245.04 (95.2)	9448.22 (11932.01)	35.37
w/o DynG	0.70 (1.23)	94.94	10.03 (5.86)	28.05 (50.97)	62.43	2635.47 (5086.84)	270.66 (50.83)	9233.22 (12003.39)	36.84
w/o DynG&TF	0.58 (0.41)	95.81	<b>9.65 (5.28)</b>	110.31 (131.6)	-47.75	10396.1 (12887.24)	300.0 (0.0)	17330.56 (9660.1)	-18.55
w/o BlockPE	0.93 (1.81)	93.28	11.12 (9.16)	34.4 (65.33)	53.92	2870.01 (5533.02)	242.39 (99.79)	<b>8291.49 (12533.67)</b>	<b>43.28</b>
DynSep (Ours)	<b>0.52 (0.24)</b>	<b>96.24</b>	9.71 (5.39)	<b>22.96 (38.93)</b>	<b>69.25</b>	<b>2233.42 (3868.43)</b>	<b>235.19 (112.26)</b>	8511.58 (12413.9)	41.78



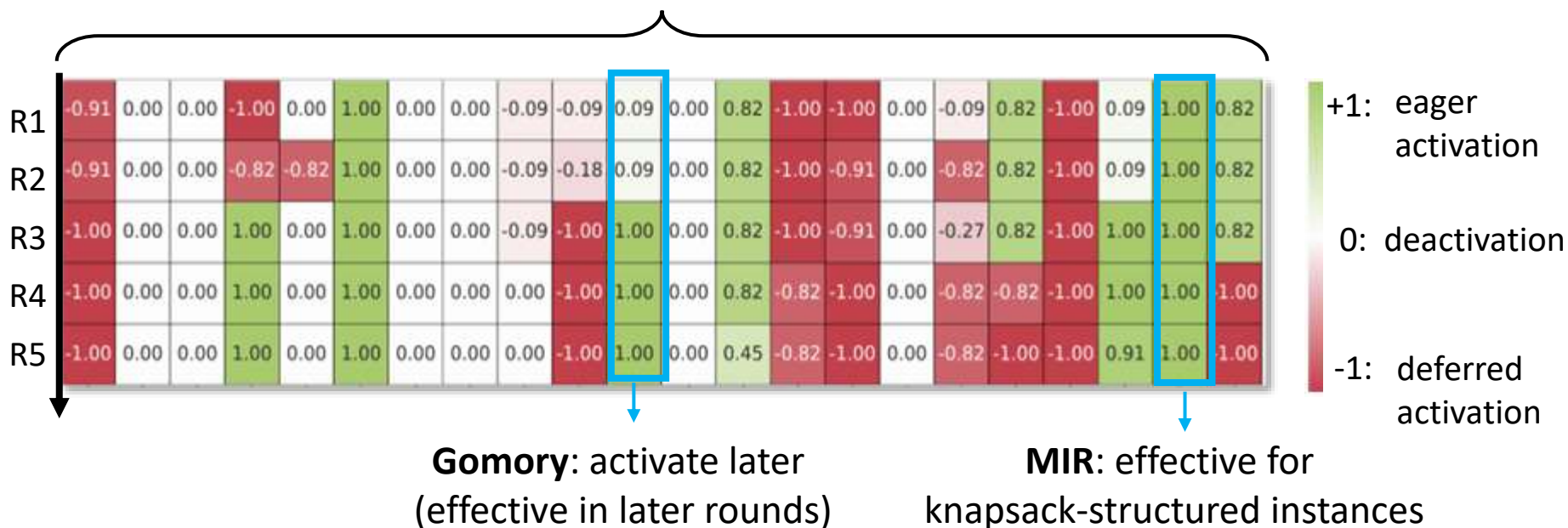
Table 3: Evaluate the generalization ability of DynSep on MIS.

Set Covering ( $n = 1000, m = 1000, 2\times$ )				Set Covering ( $n = 1000, m = 2000, 4\times$ )		
Method	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓
NoCuts	78.91 (76.53)	NA	579.09 (507.14)	282.27 (52.86)	NA	3109.87 (1013.74)
Default	11.54 (3.55)	85.38	255.69 (92.95)	19.74 (8.06)	93.01	<b>606.90 (310.79)</b>
Search(30)	116.95 (92.25)	-48.821	912.87 (647.22)	292.54 (35.54)	-3.64	3827.701 (1057.08)
Prune	107.86 (90.55)	-36.69	826.38 (660.27)	295.01 (29.73)	-4.51	4805.02 (1302.02)
L2Sep(R1)	105.48 (92.68)	-33.67	803.32 (656.89)	294.85 (31.41)	-4.46	4728.1 (1325.35)
L2Sep(R2)	116.43 (95.6)	-47.55	905.98 (694.71)	293.77 (33.96)	-4.07	4481.42 (1377.69)
LLM4Sepasel	149.28 (105.45)	-89.18	1115.22 (767.04)	295.4 (29.34)	-4.65	3881.22 (1001.51)
DynSep (Ours)	<b>4.03 (0.64)</b>	<b>94.89</b>	<b>104.62 (20.19)</b>	<b>19.05 (26.92)</b>	<b>93.25</b>	629.28 (1106.36)

Max Independent Set ( $n = 1000, m = 3946, 4\times$ )				Max Independent Set ( $n = 1500, m = 5940, 9\times$ )		
Method	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓	Time(s) ↓	Improv. ↑ (time, %)	PD integral ↓
NoCuts	195.53 (95.78)	NA	1056.83 (544.51)	300.01 (0.01)	NA	2226.72 (370.66)
Default	88.17 (66.05)	54.91	813.36 (512.14)	177.19 (91.28)	40.94	1782.96 (887.23)
Search(30)	151.51 (98.42)	22.51	462.18 (339.23)	299.08 (9.17)	0.31	1251.49 (332.08)
Prune	105.83 (86.46)	45.88	396.8 (318.97)	292.94 (26.42)	2.36	1312.04 (343.31)
L2Sep(R1)	144.67 (94.46)	26.01	546.58 (370.45)	299.34 (6.19)	0.22	1504.9 (354.98)
L2Sep(R2)	138.82 (92.89)	29.00	530.09 (367.16)	299.49 (5.2)	0.17	1494.7 (346.61)
LLM4Sepasel	60.68 (42.03)	68.97	222.88 (143.29)	264.44 (58.96)	11.86	942.49 (337.13)
DynSep (Ours)	<b>5.47 (19.09)</b>	<b>97.20</b>	<b>36.75 (71.49)</b>	<b>26.66 (77.49)</b>	<b>91.11</b>	<b>151.39 (364.6)</b>

## Knapsack family: Round-wise Activation Status of 22 SCIP Separators



Thanks for your

$$\text{softmax}\left(\frac{\begin{matrix} \text{Q} \\ \text{3x3 grid} \end{matrix} \times \begin{matrix} \text{K}^T \\ \text{3x3 grid} \end{matrix}}{\sqrt{d_k}}\right) \begin{matrix} \text{V} \\ \text{3x3 grid} \end{matrix}$$