# Exploiting the Asymmetric Uncertainty Structure of Pre-trained VLMs on the Unit Hypersphere

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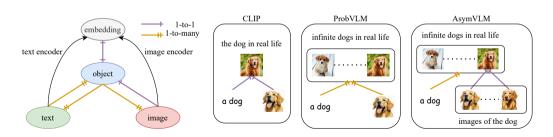
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### Rethinking Building VLMs

- CLIP: "Image—text is an one-to-one mapping".
- ProbVLM¹: "Image—text is a (symmetric) many-to-many mapping".
- AsymVLM: "Image—text is a many-to-many mapping with an asymmetric structure".



<sup>&</sup>lt;sup>1</sup>Upadhyay et al., "Probvlm: Probabilistic adapter for frozen vison-language models".

### Building the method

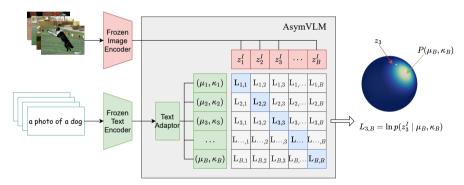
- Text encoder (text  $\rightarrow$  embedding): one-to-many, modelled by probabilistic embeddings.
- Image encoder (image → embedding): one-to-one, modelled by deterministic embedding.

Additionally, we need to utlize the pre-trained models (CLIP, BLIP, SigLIP, etc), which have deterministic embeddings on  $\mathbb{S}^{d-1}$ :

- The method should be post-hoc.
- Probabilistic embeddings should be modelled by directional distributions.

#### Deriving the Loss

We want to maximize  $p(z^l(i) | \theta(t))$  if t and i match, and minimize it if they do not:



To maximize the diagonals and minimize the off-diagonals, InfoNCE loss is applied.

#### Discussion

Unified objectives:

$$\underset{\theta \in \Theta}{\arg\min} - \frac{1}{2B} \sum_{n=1}^{B} \left[ \ln \frac{\exp\left(\tau \delta(n,n)\right)}{\sum_{m=1}^{B} \exp\left(\tau \ln \delta(n,m)\right)} + \ln \frac{\exp\left(\tau \delta(n,n)\right)}{\sum_{m=1}^{B} \exp\left(\tau \delta(m,n)\right)} \right].$$

Denoting  $\mathsf{CosSim}(r,s) = \mu(t_r)^{ op} z_s^I$ , for any  $r,s \in [B]$  we have,

$$\begin{split} \text{for CLIP: } & \delta_{\text{CLIP}}(r,s) = \text{CosSim}(r,s), \\ \text{for AsymVLM}_{\text{vMF}} \colon & \delta_{\text{vMF}}(r,s) = \kappa(t_r) \cdot \text{CosSim}(r,s) + F_d(\kappa(t_r)), \\ \text{for AsymVLM}_{\text{PS}} \colon & \delta_{\text{PS}}(r,s) = \kappa(t_r) \ln(1 + \text{CosSim}(r,s) + \ln C_d(\kappa(t_r)). \end{split}$$

## Empirical results: Uncertainty evaluation

