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Less is More: Local Intrinsic Dimensions of Contextual Language Models

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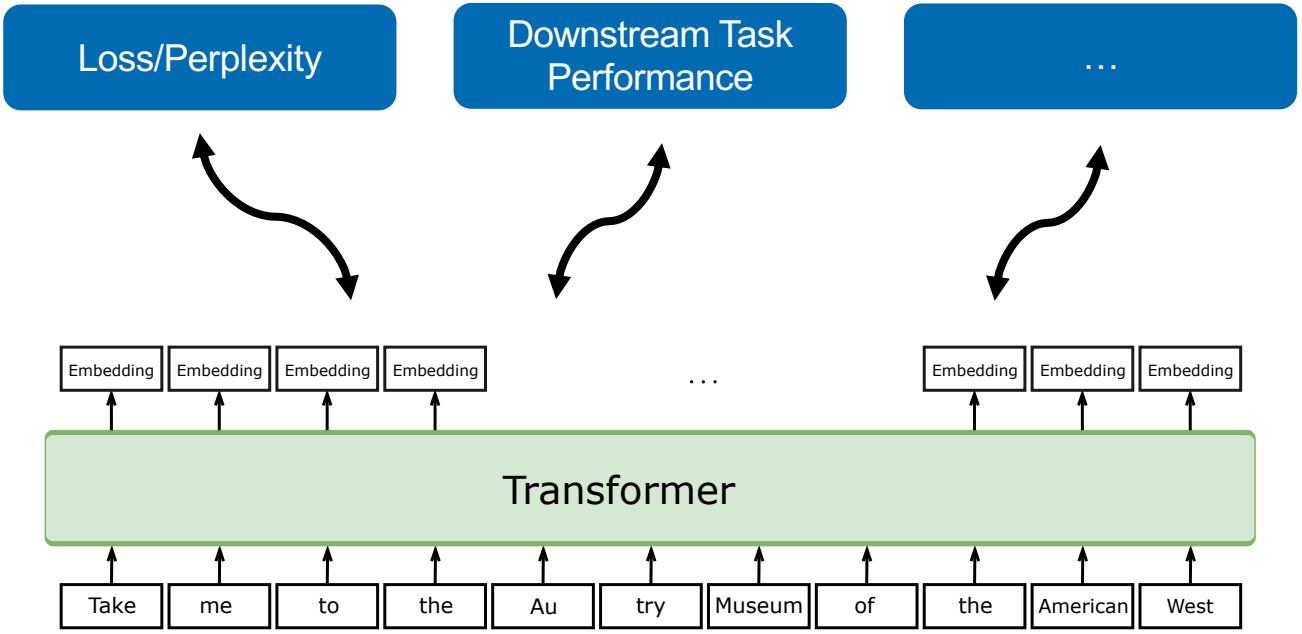
AIDOS Lab, **University of Fribourg**, Switzerland

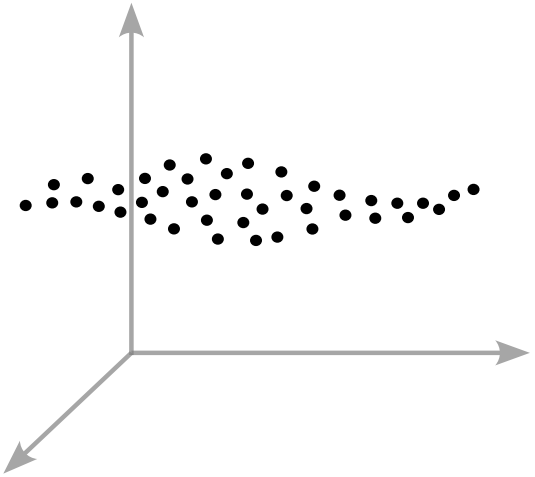
Motivation

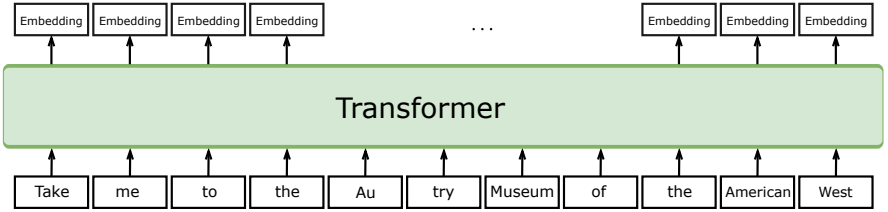
- LLMs learn **contextual token embeddings** in high-dimensional spaces
- Most diagnostics: supervised, task-specific



Motivation

- Few methods explore the **geometry** of the embedding spaces





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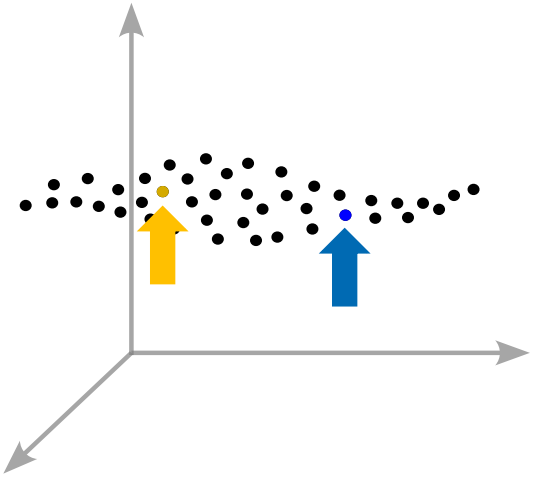
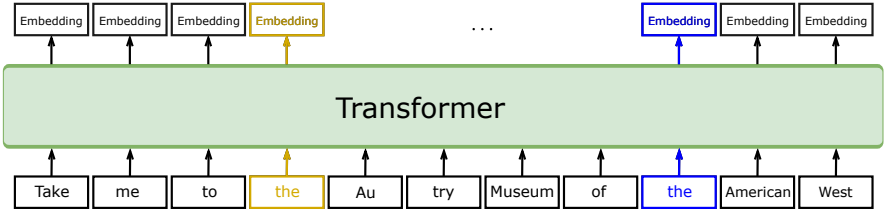
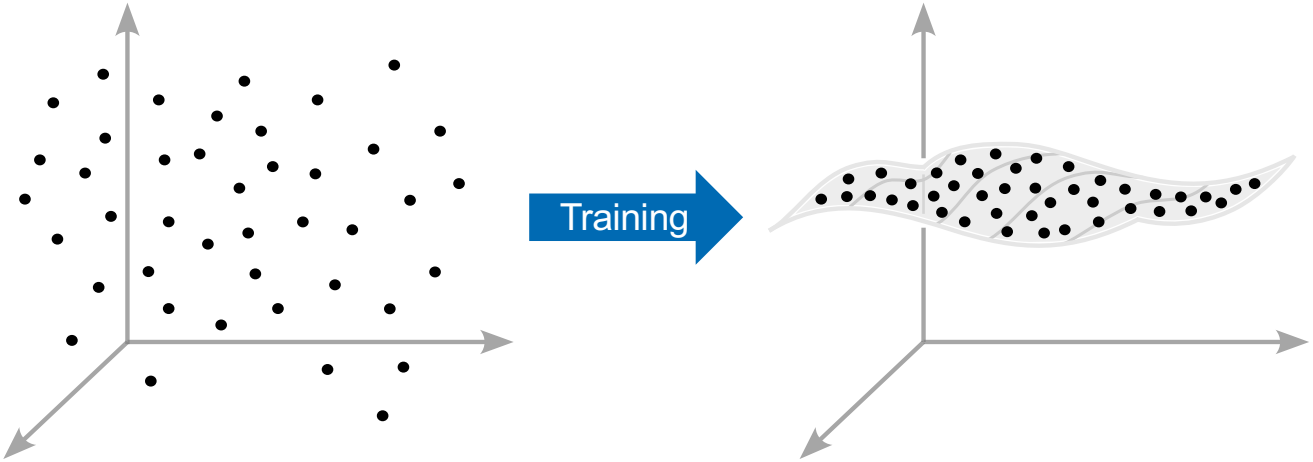




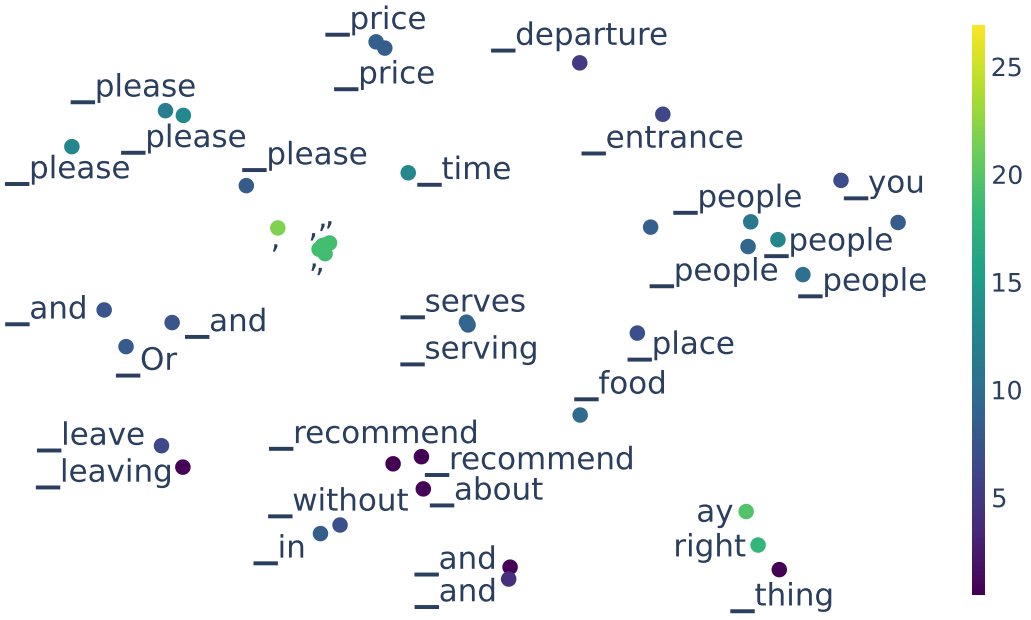
Can Embedding Geometry Reveal Learning Dynamics?



Structural **changes in the embedding space**
→ Unsupervised insights into model behaviour across language tasks?

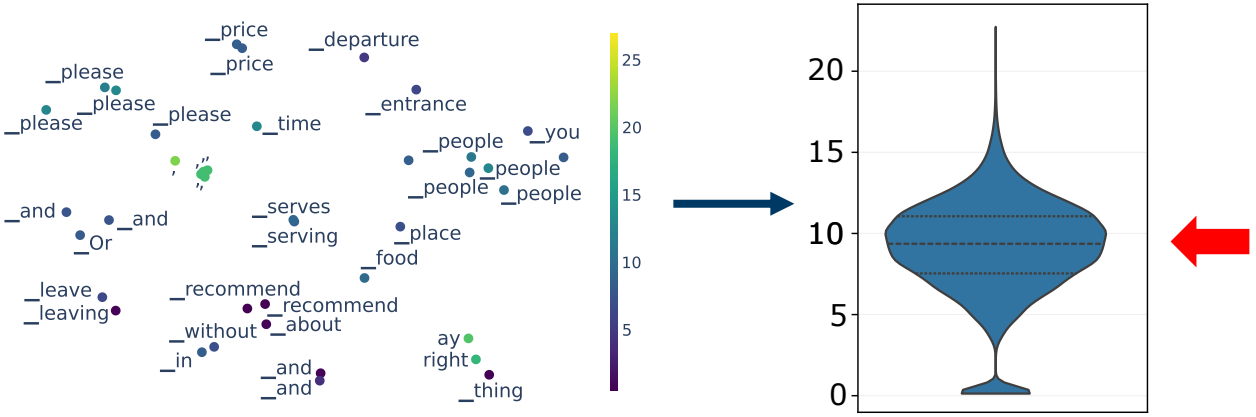
Method: Local Intrinsic Dimension via TwoNN

- **Localized TwoNN estimator** *(Facco et al., 2017)*
- Applied to **subsample** of contextual token embeddings



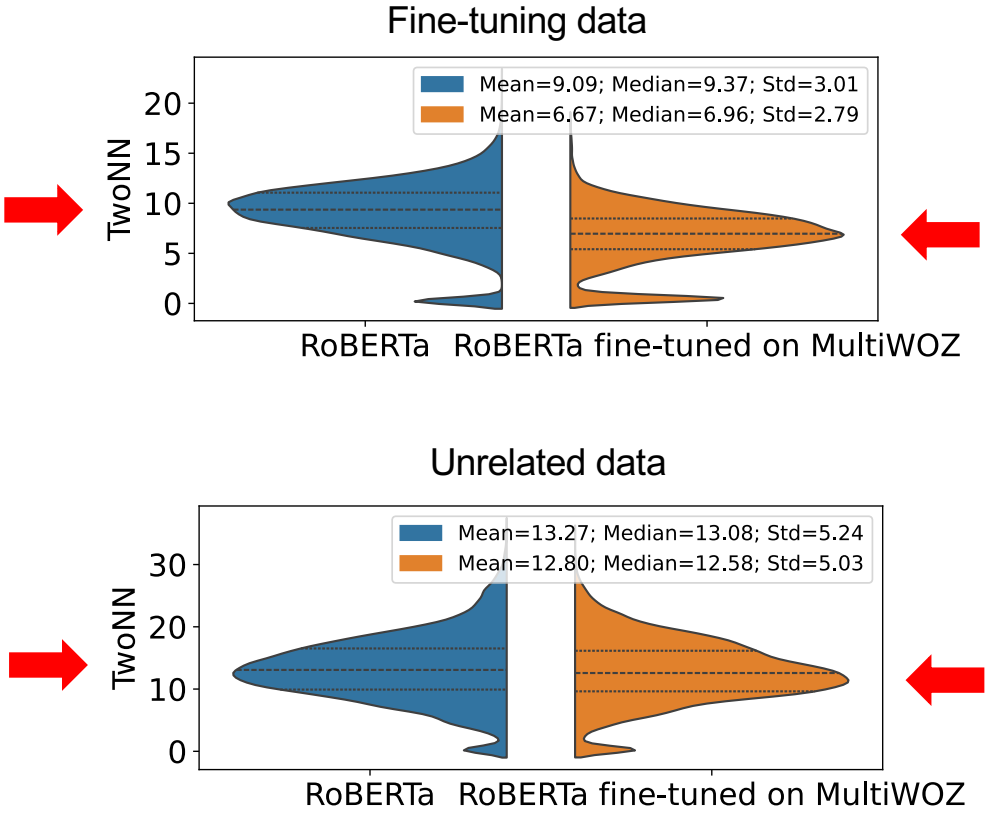
Dimensional “Signatures”

- Dimension distribution reflects *information organization*
- Local variations form **geometric fingerprint**
- Enables **unsupervised** analysis, no labels needed

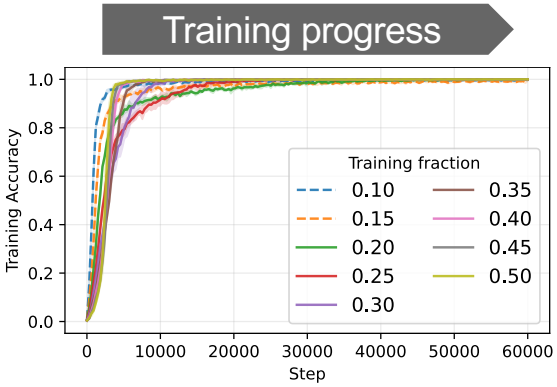


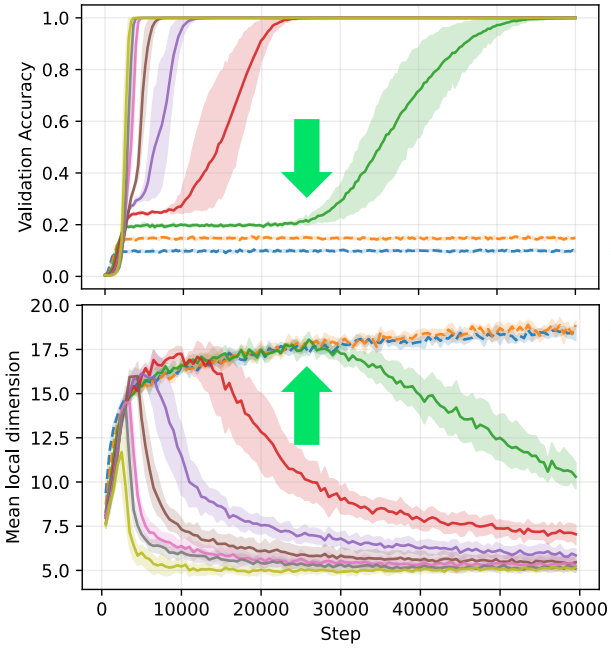
Mean local dimension: Stable estimate over different data splits and models

(1) Fine-Tuning Induces Dataset-Specific Dimensional Shifts



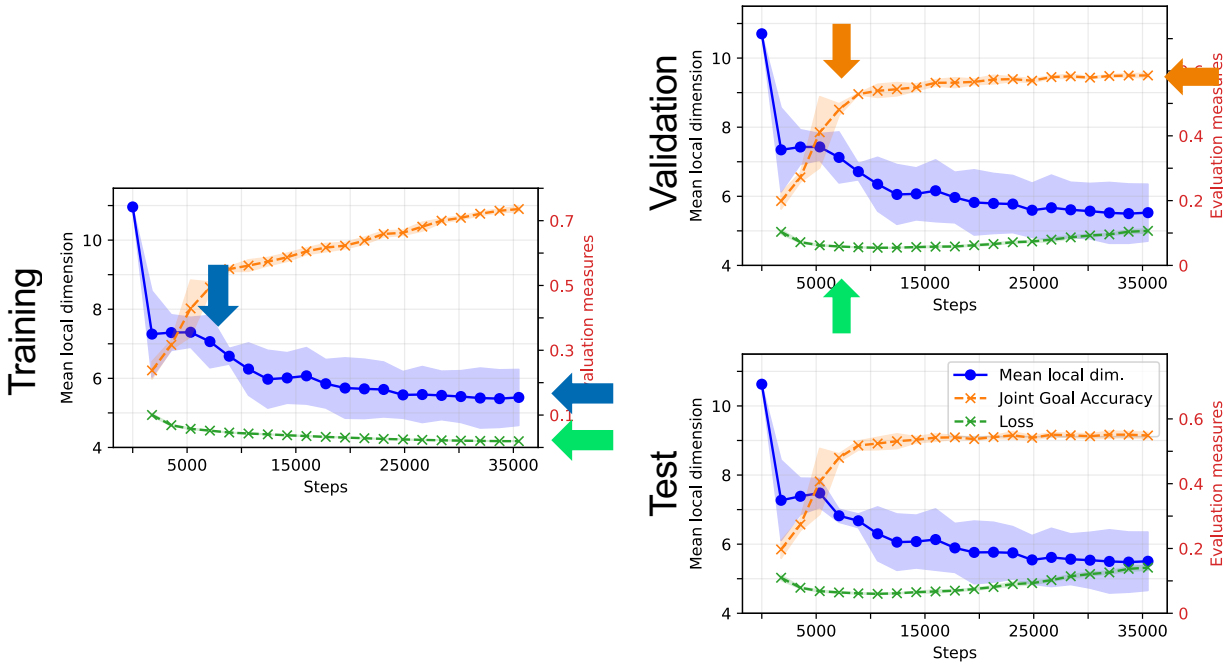
(2) Dimension Drop Anticipates Grokking





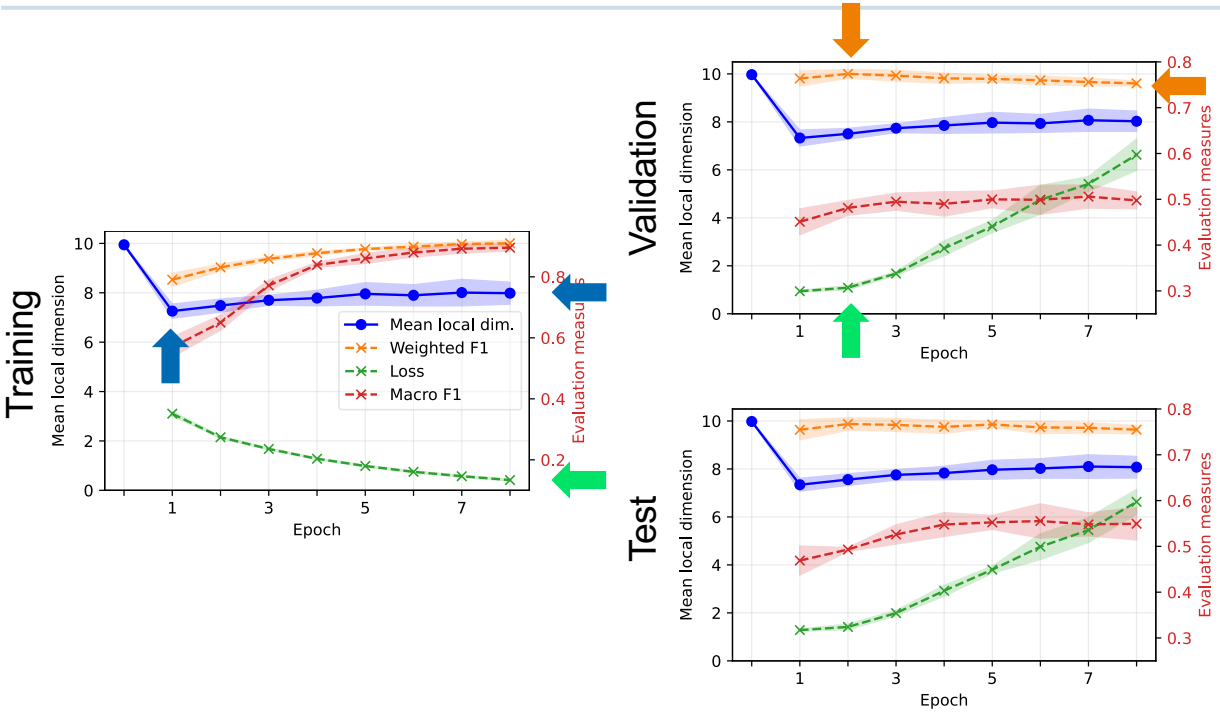
- Task: Synthetic modular-arithmetic
- **Dimension drop ↔ Generalization**

(3) Dimension Stabilization Tracks Learning



- Task: Sequence-tagging-based Dialogue State Tracking
- **Stabilizing dimension ↔ Training convergence**

(4) Dimension Increase Detects Overfitting



- Task: Classify dialogue utterances into emotion
- **Initial drop followed by a rise in dimension ↔ Overfitting**

Summary

Across diverse tasks, a sustained **drop in mean local dimension** reliably predicts **improved generalization.**

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Google Cloud

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Code (GitHub)

Paper (NeurIPS 2025)

We are looking forward to your questions!