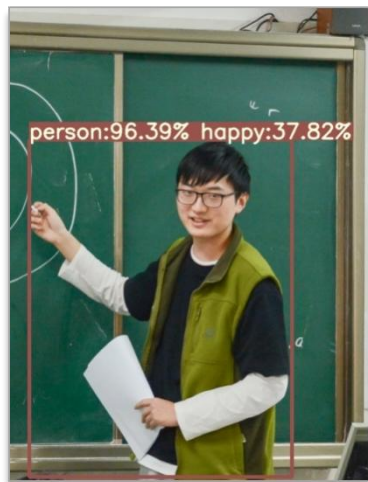
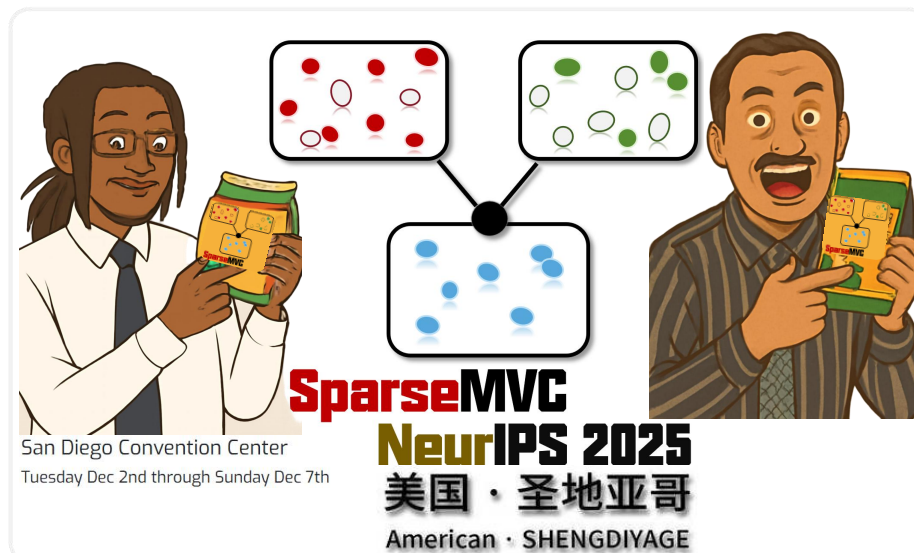


SparseMVC: Probing Cross-view Sparsity Variations for Multi-view Clustering

Ruimeng Liu · Xin Zou · Chang Tang* ·
Xiao Zheng · Xingchen Hu · Kun Sun · Xinwang Liu



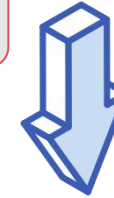
刘睿萌



We explicitly identify, analyze, and define the problem of **cross-view sparsity variations** in multi-view data,



Identify problem, solve problem.



and to propose a dedicated framework **SparseMVC** that offers a targeted and principled solution.

1. Multi-view clustering: Multi-view refers to data composed of multiple views from distinct sources. Clustering, which emphasizes unsupervised learning, essentially treats clustering algorithms as probes to assess the representational performance of the features extracted by the network.

2. View sparsity ratio in multi-view datasets:

To quantify cross-view sparsity variations, we define the sparsity ratio s_v for the v -th view:

$$s_v = \frac{1}{N \cdot F} \sum_{j=1}^N \sum_{i=1}^F \mathbf{I}[x_{i,j}^v = 0],$$

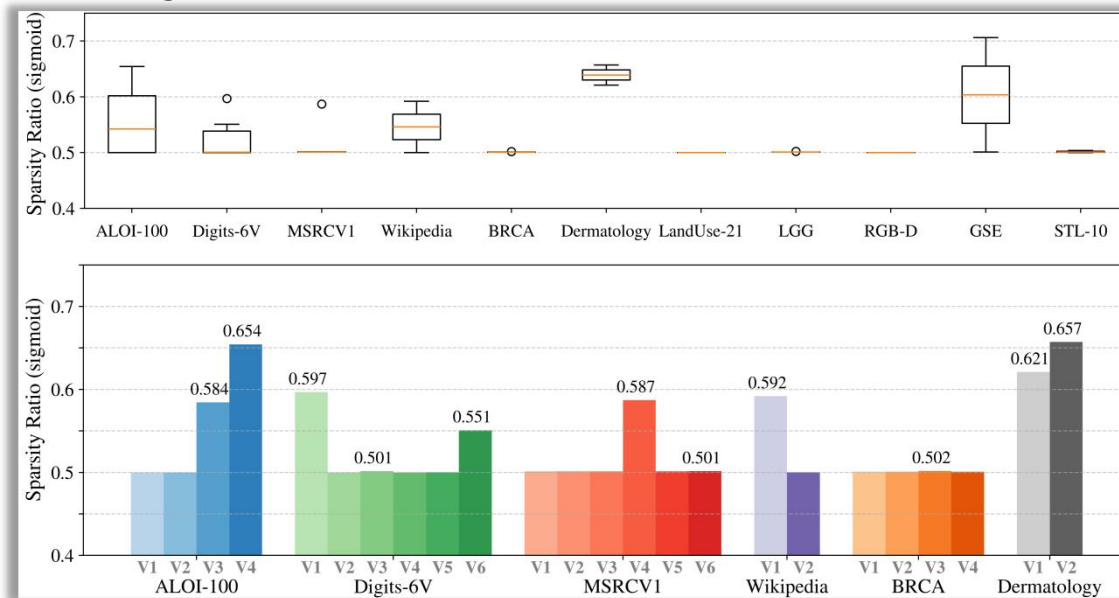
Identify problem: **cross-view sparsity variations**

For a single dataset, does **sparsity variation** exist among the internal views?

1. Multi-view data consist of **multiple distinct data sources**.

2. **Sparsity is a prevalent characteristic** in multi-view data.

Sparsity ratios across views in multi-view datasets.



Exist and exist widely

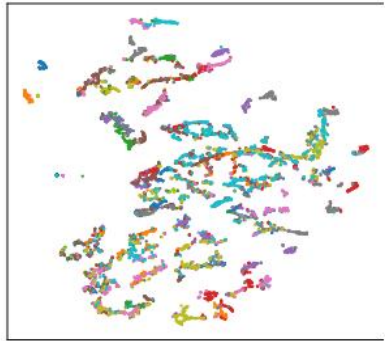
- **Top box plot:** Distribution, median (orange line), interquartile range (box), outliers (outside whiskers).
- **Bottom bar plot:** Sparsity ratios for each view in the datasets.
- **The sparsity ratios in Figure are transformed using the sigmoid function**, which shifts the baseline from 0 (the bottom of the image) to 0.5 (the middle of the image) for better visualization, as many views have very small sparsity values (less than 0.01) that would be hard to see with the original scale.

Motivation

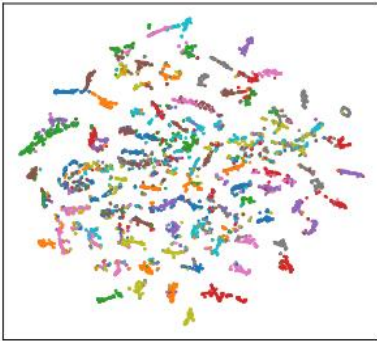
Method

Experiment

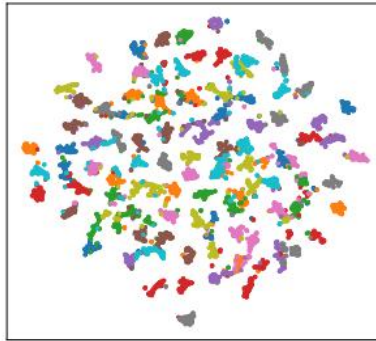
Conclusion



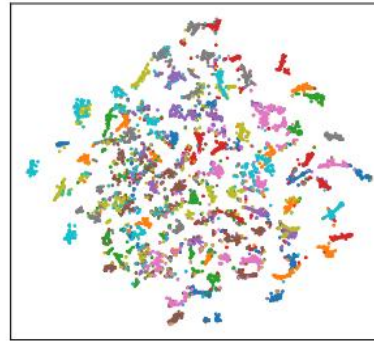
(a) GCFAgg (CVPR'23)



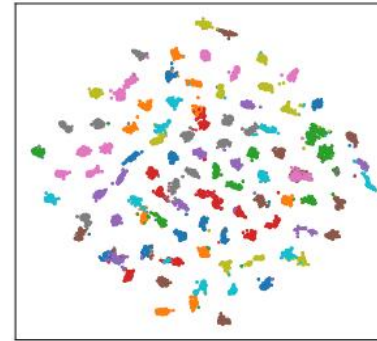
(b) CPSPAN(CVPR'23)



(c) SCMVC (TMM'24)



(d) MVCAN (CVPR'24)



(e) SparseMVC (Ours)

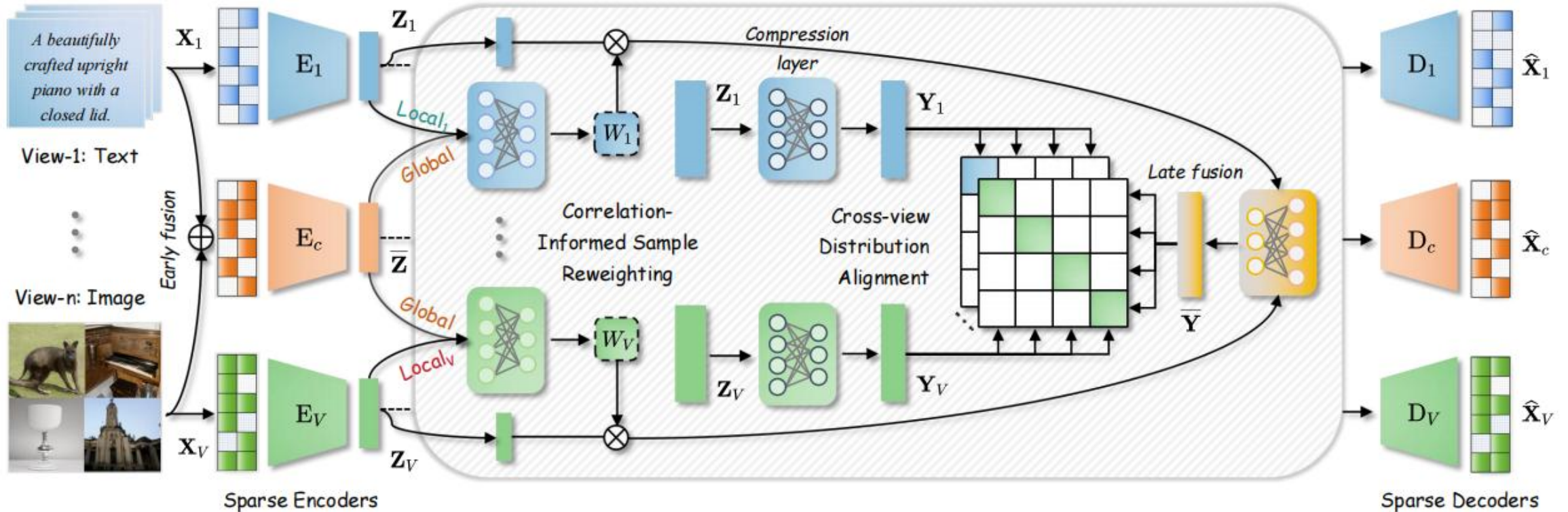
**T-SNE
visualization
for comparison**

Datasets	Sparsity of Different Views	Accuracy		NMI			
		[Ours]	[2nd]	[Ours]	[2nd]		
ALOI-100	[0.0001, 0.0001, 0.3415, 0.6383]	82.21	↑4.49	77.72	92.65	↑1.78	90.87
MSRCV1	[0.0049, 0.0048, 0.0048, 0.3478, 0.0051, 0.0048]	97.14	↑5.71	91.43	94.22	↑6.32	87.90
LGG	[0.0040, 0.0038, 0.0078, 0.0037]	83.15	↑0.38	82.77	54.13	↑0.49	54.13
Synthetic3d	[0.0017, 0.0017, 0.0017]	98.33	↑0.16	98.17	98.33	↑0.16	98.17

- Above table demonstrates that SparseMVC maintains robust performance across datasets with **significant** sparsity differences (e.g., a 6000-fold disparity between the maximum and minimum view sparsity ratios in **ALOI-100**) as well as those with **minimal** sparsity variations (e.g., no view sparsity differences in **Synthetic3D**).

solve problem: **cross-view sparsity variations**

Overview of SparseMVC



SparseMVC is a framework designed to address varying sparsity across views. It begins by utilizing sparse autoencoders with adaptive constraints, which dynamically adjust the coding strategy based on the probed s_v , to generate latent features (Z), making the reconstructed features (\hat{X}) approximate the original input features (X). Subsequently, the correlation between the early-fused global features (\bar{Z}) and view-specific features ($\{Z_v\}_{v=1}^n$) guides the computation of sample-level weights ($\{W_v\}_{v=1}^n$) via the attention mechanism within the correlation-informed sample reweighting module. Finally, the cross-view distribution alignment module enhances clustering performance by setting the late-fused global features \bar{Y} as the anchor latent representation, and then simultaneously aligning the multi-view feature distribution between \bar{Y} and each view-specific compressed feature ($\{Y_v\}_{v=1}^n$).

Motivation

Method

Experiment

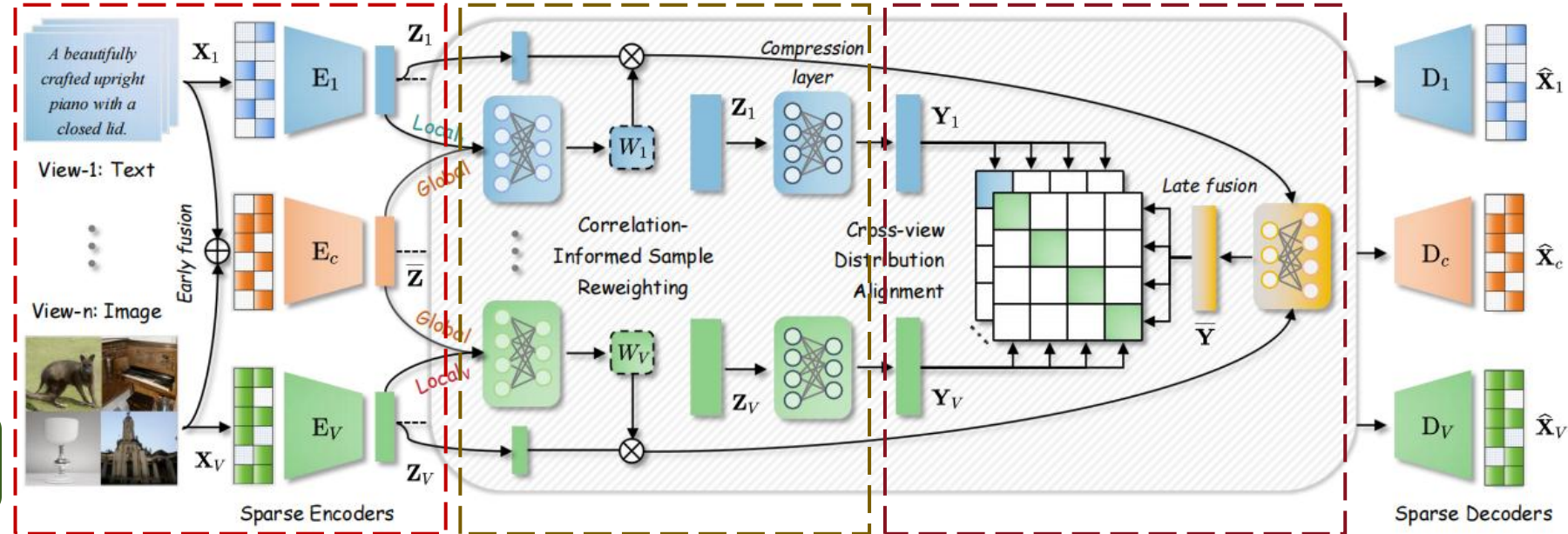
Conclusion

How to enable autoencoders to adaptively encode features?

How to mitigate the side effects of encoding discrepancies?

How to align feature distributions across multiple views?

Part 2. Correlation weights based on the early-fused global and view-specific features

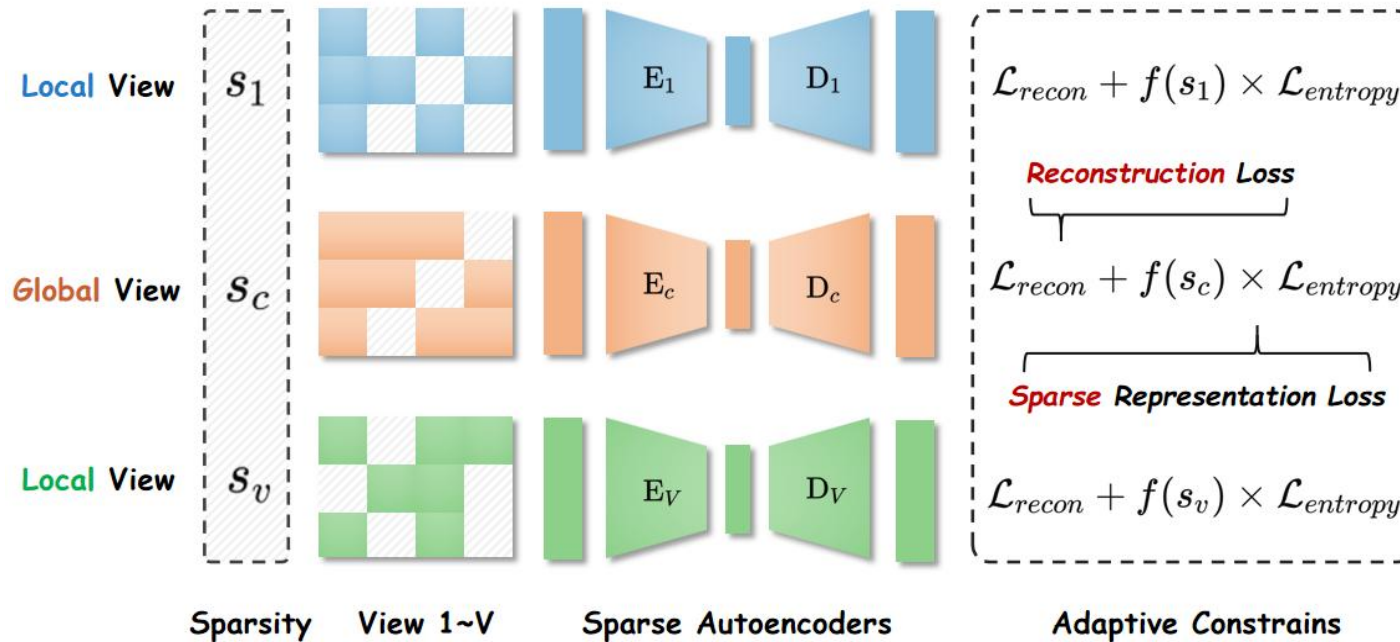


Part 1. Sparse autoencoders with constraints that vary based on view-level sparsity

Part 3. Sample pairs distribution alignment based on contrastive learning

- SparseMVC** is specifically designed to handle **view-level sparsity variations**, a prevalent yet underexplored characteristic of multi-view data, through a complete data-driven and tightly integrated architecture.

Part 1.



$$\boxed{2} \mathcal{L}_{sparse}^v = f(s_v) \cdot \mathcal{L}_{entropy}^v = f(s_v) \cdot \sum_{k=1}^H \left(\rho \log \frac{\rho}{\hat{h}_k^v} + (1 - \rho) \log \frac{1 - \rho}{1 - \hat{h}_k^v} \right)$$

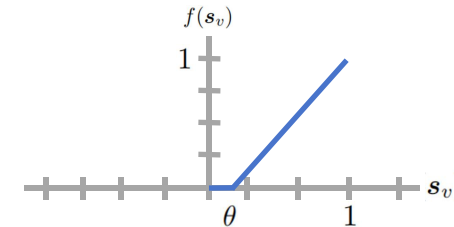
$$\boxed{1} \mathcal{L}_{recon}^v = \frac{1}{N} \sum_{j=1}^N (\hat{x}_j^v - x_j^v)^2$$

$$\mathcal{L}_{recon}^v \oplus \mathcal{L}_{sparse}^v$$

$$\mathcal{L}_{recon}^v \oplus f(s_v) \cdot \mathcal{L}_{entropy}^v$$

We use the sparsity ratio of each view as prior knowledge:

$$f(s_v) = \begin{cases} 0, & \text{if } s_v \leq \theta, \\ \frac{s_v - \theta}{1 - \theta}, & \text{if } s_v > \theta, \end{cases}$$

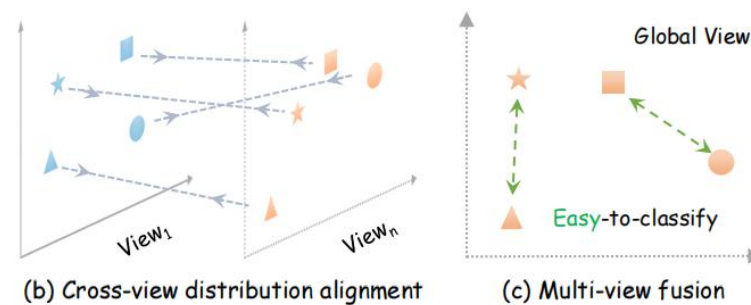
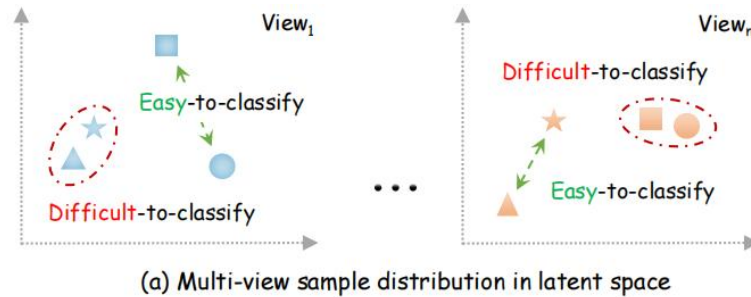


- To address the sparsity variations across views within a dataset, we propose an adaptive encoding strategy that allows the encoders to automatically transition between standard and various degrees of sparse encoding

Part 2.

- To mitigate the enlarged representation gap caused by heterogeneous encoding, we incorporate a correlation-guided fusion strategy that leverages **global-to-local feature relationships** established in the early encoding stage to guide the weighting of local features during late fusion.

Part 3.



Algorithm 1 Training Steps for SparseMVC

Input: Multi-view data $\{X_v\}_{v=1}^V$, cluster number K , and number of training epochs $E_{\text{pre}}, E_{\text{con}}$.

Output: Late-stage fusion representation \bar{Y} .

- 1: Initialize random seed and select Adam optimizer.
- 2: **for** $epoch = 1 : E_{\text{pre}} + E_{\text{con}}$ **do**
- 3: Update $\{Z_v\}_{v=1}^V$ by minimizing $\{\mathcal{L}_{\text{recon}}^v\}_{v=1}^V$ and $\{\mathcal{L}_{\text{entropy}}^v\}_{v=1}^V$ utilizing Eqs. (2) and (4).
- 4: Update \bar{Z} , formed by the concatenation of $\{Z_v\}_{v=1}^V$, utilizing Eq. (2) and Eq. (4).
- 5: **if** $epoch > E_{\text{pre}}$ **then**
- 6: Update weights $\{W_v\}_{v=1}^V$ by Eq. (9).
- 7: Update \bar{Y} by minimizing \mathcal{L}_{CDA} utilizing Eq. (13).
- 8: **end if**
- 9: **end for**
- 10: Perform K -means clustering on representation \bar{Y} .

SparseMVC
Algorithm

- View distribution alignment based on contrast** (with arbitrary view numbers).

$$\mathcal{L}_{\text{total}} = \sum_{v=1}^V (\mathcal{L}_{\text{recon}}^v + f(s_v) \cdot \mathcal{L}_{\text{entropy}}^v) + \lambda_{\text{CR}} \cdot \mathcal{L}_{\text{CDA}}$$

SparseMVC: Probing Cross-view Sparsity Variations for Multi-view Clustering

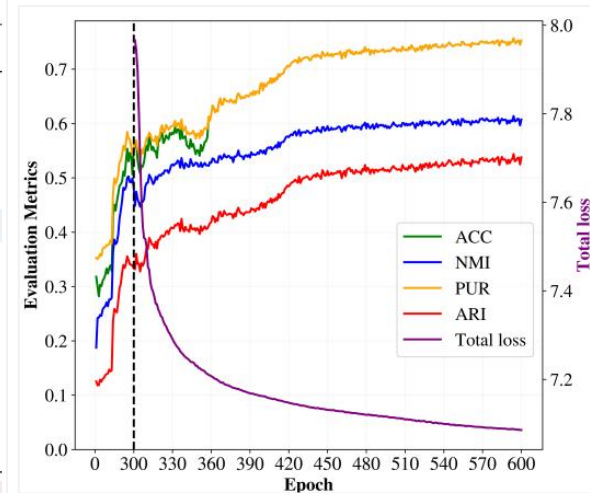
Motivation

Method

Experiment

Conclusion

Methods \ Datasets	Out-Scene			ALOI-100			Wikipedia			MSRCV1		
	ACC	NMI	PUR	ACC	NMI	PUR	ACC	NMI	PUR	ACC	NMI	PUR
COMPLETER [CVPR'21] [44]	69.79	55.39	69.79	30.70	62.12	33.63	57.14	53.10	59.31	90.00	<u>87.90</u>	90.00
DCP [TPAMI'22] [45]	56.03	45.59	56.32	34.01	60.28	37.32	45.31	43.16	46.32	25.71	23.25	27.14
MFLVC [CVPR'22] [48]	58.97	51.31	58.97	33.17	73.28	33.17	40.12	27.52	41.70	63.33	66.11	64.29
DSMVC [CVPR'22] [43]	62.13	53.01	64.25	71.52	<u>90.87</u>	72.72	<u>60.32</u>	54.74	<u>62.19</u>	64.29	54.29	64.29
SURE [TPAMI'22] [62]	60.97	48.09	60.97	10.13	34.19	11.90	50.65	39.97	54.11	<u>91.43</u>	85.84	<u>91.43</u>
DealMVC [MM'23] [49]	69.57	59.44	69.57	13.11	48.54	13.10	38.96	37.09	38.96	82.00	75.54	82.00
GCFAgg [CVPR'23] [3]	68.23	57.14	68.23	74.11	88.30	76.63	51.80	45.87	56.57	39.52	31.91	42.86
CPSPAN [CVPR'23] [51]	59.15	50.46	59.15	56.96	78.78	67.99	22.08	8.35	24.39	67.62	69.83	89.52
SDMVC [TKDE'23] [50]	56.03	46.18	59.93	52.02	74.70	56.56	55.99	53.98	62.05	59.52	52.51	45.24
CVCL [ICCV'23] [46]	<u>73.51</u>	59.59	<u>73.51</u>	21.86	43.13	23.29	14.17	42.81	32.69	48.44	84.57	90.62
MVCAN [CVPR'24] [52]	70.98	58.23	49.95	67.48	83.78	56.71	59.02	55.81	67.97	71.54	60.19	71.54
SCMVC [TMM'24] [47]	71.54	<u>60.19</u>	71.54	<u>77.72</u>	89.42	<u>81.05</u>	53.54	35.59	55.84	90.95	83.92	90.95
SparseMVC (Ours)	77.49	63.34	77.49	82.21	92.65	84.19	61.04	<u>54.79</u>	62.91	97.14	94.22	97.14

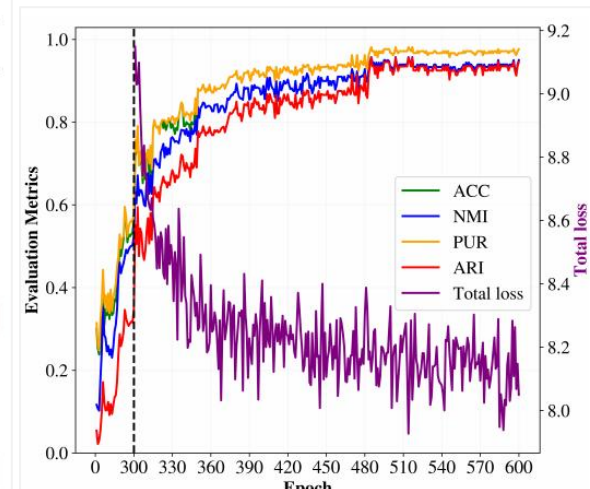


Out-Scene
big dataset

Comparative Results

Convergence Analysis

Methods \ Datasets	Synthetic3d			LGG			Dermatology			BRCA		
	ACC	NMI	PUR	ACC	NMI	PUR	ACC	NMI	PUR	ACC	NMI	PUR
COMPLETER [CVPR'21] [44]	93.33	76.06	93.33	80.15	49.25	80.15	77.65	80.11	82.12	55.53	34.65	65.33
DCP [TPAMI'22] [45]	97.17	87.60	97.17	59.55	44.82	73.03	72.91	77.22	80.73	57.29	<u>39.51</u>	60.55
MFLVC [CVPR'22] [48]	90.67	72.59	90.67	79.03	49.73	79.03	58.10	56.20	62.85	55.53	27.74	60.05
DSMVC [CVPR'22] [43]	96.83	86.64	96.83	<u>82.77</u>	<u>54.13</u>	<u>82.77</u>	92.74	87.82	92.74	54.52	33.53	68.84
SURE [TPAMI'22] [62]	96.33	85.16	96.33	62.92	38.01	65.17	88.27	77.03	88.55	39.70	12.85	48.99
DealMVC [MM'23] [49]	87.50	72.07	87.50	72.28	40.55	72.28	45.53	31.13	45.53	59.55	32.79	61.56
GCFAgg [CVPR'23] [3]	96.67	85.54	96.67	55.06	22.95	61.80	88.27	79.25	88.27	51.51	32.41	61.31
CPSPAN [CVPR'23] [51]	97.83	90.15	<u>97.83</u>	63.30	30.53	63.30	76.26	84.63	85.20	<u>66.83</u>	34.48	74.12
SDMVC [TKDE'23] [50]	96.83	86.47	90.00	63.67	43.86	67.79	70.67	83.30	84.92	57.79	33.80	64.57
CVCL [ICCV'23] [46]	95.31	82.36	95.31	58.20	23.73	58.20	56.25	56.01	67.97	61.98	34.68	68.49
MVCAN [CVPR'24] [52]	<u>98.17</u>	<u>91.27</u>	94.59	59.55	42.57	27.18	58.38	66.73	51.58	57.79	35.70	32.24
SCMVC [TMM'24] [47]	97.00	87.11	97.00	73.41	39.76	73.41	<u>93.85</u>	<u>88.44</u>	<u>93.85</u>	50.25	30.70	60.80
SparseMVC (Ours)	98.33	92.01	98.33	83.15	54.62	83.15	95.25	89.86	95.25	70.10	44.90	<u>70.85</u>



MSRCV1
small dataset

Ablation Study

1.Loss Function

Datasets	Loss Function			Evaluation Metrics		
	\mathcal{L}_{recon}	$\mathcal{L}_{entropy}$	\mathcal{L}_{CDA}	ACC	NMI	PUR
ALOI-100	✓			45.27	71.21	30.41
	✓	✓		66.35	81.65	70.62
	✓		✓	64.11	80.23	67.33
	✓	✓	✓	82.21	92.65	84.19
Dermatology	✓			70.11	74.41	59.69
	✓	✓		75.70	83.36	69.36
	✓		✓	70.95	71.06	83.80
	✓	✓	✓	95.25	89.86	95.25
MSRCV1	✓			58.57	48.63	32.76
	✓	✓		70.48	65.27	52.08
	✓		✓	92.38	87.62	92.38
	✓	✓	✓	97.14	94.22	97.14



2.Network Components

Components \ Datasets	ALOI-100			Dermatology			MSRCV1		
	ACC	NMI	PUR	ACC	NMI	PUR	ACC	NMI	PUR
all sparse autoencoders w/o CSR	78.56	88.92	81.12	77.37	74.38	86.03	91.90	88.56	91.90
all sparse autoencoders	80.42	89.19	82.44	89.11	78.37	89.11	92.38	88.61	92.38
adaptive autoencoders w/o CSR	81.04	89.58	83.17	88.83	78.23	88.83	95.71	92.69	95.71
adaptive autoencoders (Ours)	82.21	92.65	84.19	95.25	89.86	95.25	97.14	94.22	97.14

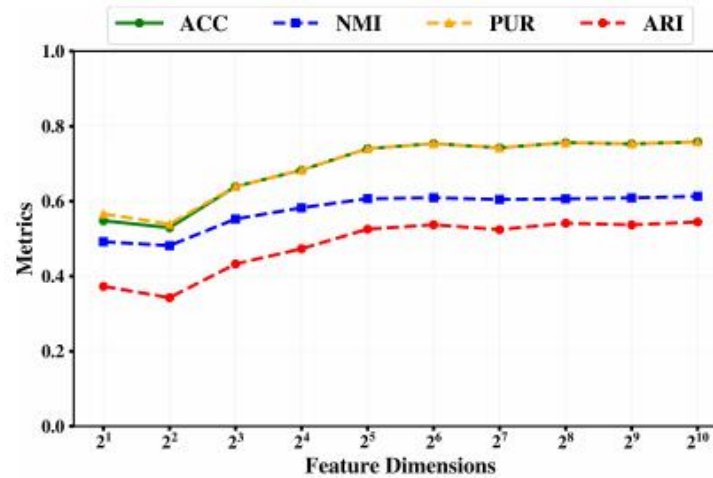
Motivation

Method

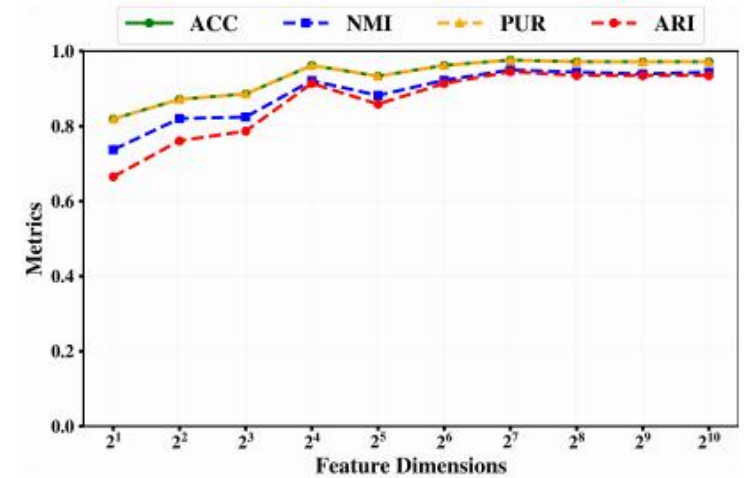
Experiment

Conclusion

**1.Feature (Z_v) dimension
/Latent space size
Sensitivity Analysis**

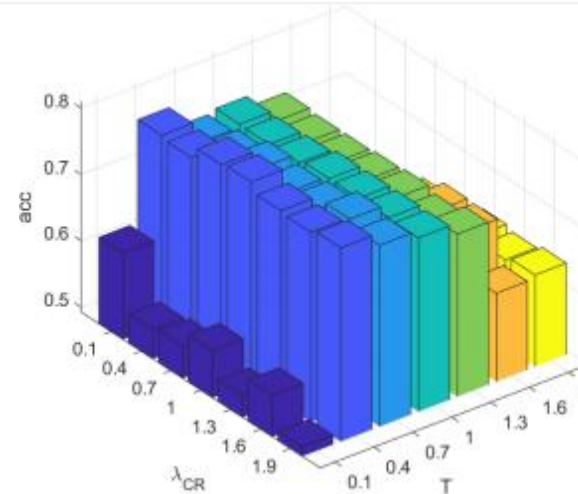


(a) Out-Scene

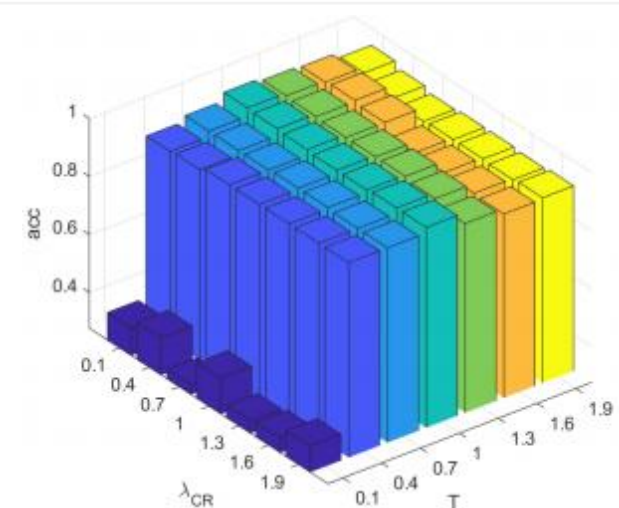


(b) MSRCV1

**2.Loss Function
Parameter
Sensitivity Analysis**



(a) Out-Scene



(b) MSRCV1

Limitations:

- SparseMVC does not incorporate a targeted design or specialized mechanisms to address view misalignment and random view missingness;
- the use of contrastive learning inherently introduces computational overhead, making it unlikely to rank among the fastest available approaches.



Conclusion:

- This paper highlights a frequently overlooked issue in deep multi-view learning: **varying sparsity ratios across views**;
- We systematically define, quantify, and analyze cross-view sparsity variation as a fundamental characteristic of multi-view data;
- Our framework advances the field by extending sparsity handling from the data-level to view-level and mitigating the adverse effects of encoding discrepancies through sample-level dynamic weighting;
- We hope this work inspires greater attention to the intrinsic characteristics of data and to the design of architectures driven by data.