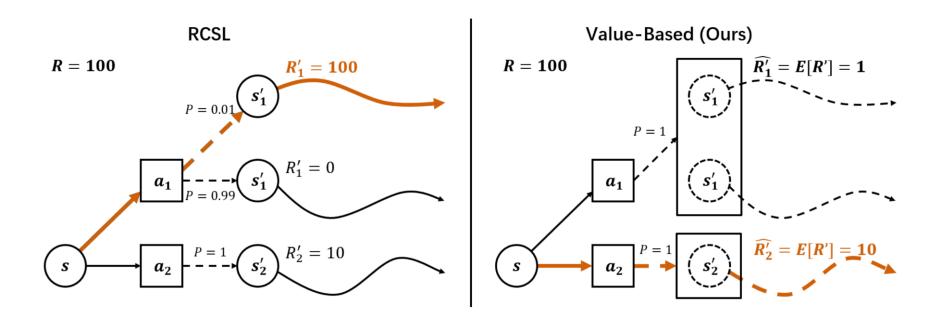


# Value-Guided Decision Transformer: A Unified Reinforcement Learning Framework for Online and Offline Settings

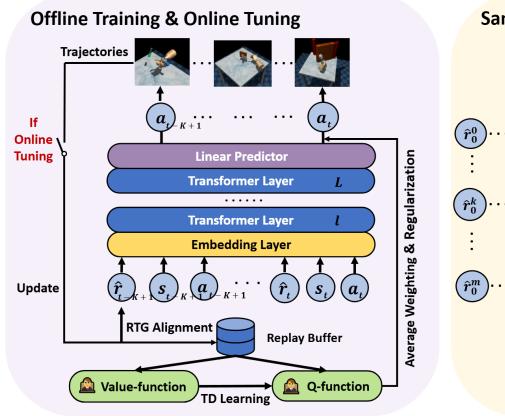
## **Motivation**

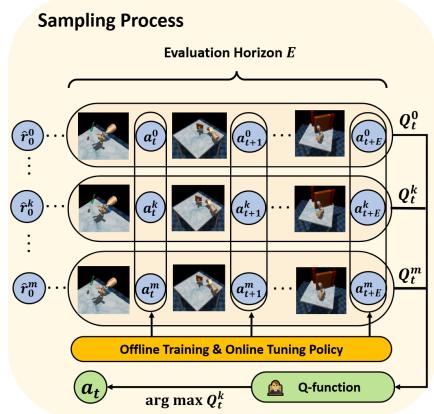




- □ Insufficient Value Function Integration: Prior methods simply relabel returns or add penalties, failing to fully harness value functions for optimization and regularization in DTs.
- □ Offline-to-Online Gap: ODT extends DTs to online RL but cannot achieve expert performance with limited or low-quality data and only improves notably after online fine-tuning.
- Need for a Unified Framework: There is a strong demand for a unified RL method that bridges offline and online RL, robustly handles suboptimal data, and better integrates value functions with Transformer architectures.







# **Offline Training Phase**



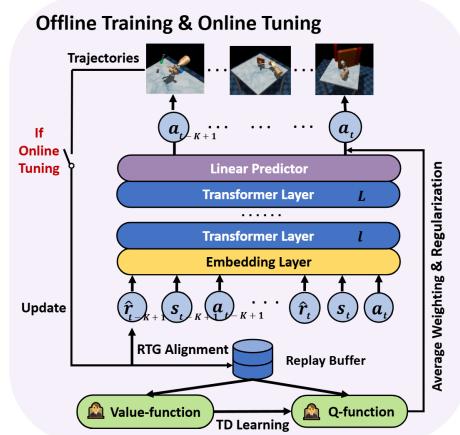
### Value function training

$$L_V(\psi) = \mathbb{E}_{(s_t, a_t) \sim \mathcal{D}} \left[ L_2^{\epsilon} \left( Q_{\hat{\theta}}(s_t, a_t) - V_{\psi}(s_t) \right) \right]$$

$$L_2^{\epsilon}(u) = |\epsilon - \mathbb{I}(u < 0)|u^2$$

$$\mathbb{E}_{(s_t, a_t, r_t, \dots, s_{t+n}) \sim \mathcal{D}} \left[ \left( \sum_{k=0}^{n-1} \gamma^k r_{t+k} + \gamma^n V_{\psi}(s_{t+n}) - Q_{\theta_i}(s_t, a_t) \right)^{2^{-1}} \right]$$

### Loss function

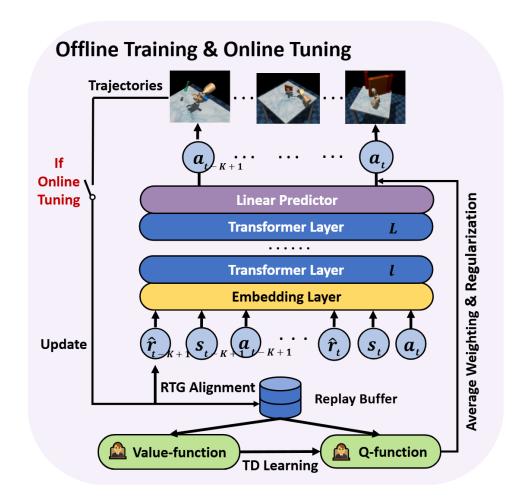


$$\mathbb{E}_{\substack{\tau_t \sim \mathcal{D} \\ (s_t, a_t) \sim \tau_t}} \left[ \exp(\eta(\min_{i=1,2} Q_{\hat{\theta}_i}(s_t, a_t) - V_{\psi}(s_t))) \|\pi_{DT}(\tau_t) - a_t\|^2 - \lambda \cdot \min_{i=1,2} Q_{\hat{\theta}_i}(s_t, \pi_{DT}(\tau_t)) \right]$$

# **Online Tuning Phase**



- □ Trajectory-Level Replay Buffer: During the online tuning phase, VDT adopts a trajectory-level replay buffer, storing complete trajectories rather than single transitions. The buffer is first filled with the highest-return trajectories from offline data, and is updated in a first-in-first-out manner whenever the policy generates a new trajectory. A two-step sampling strategy ensures uniform sampling of subtrajectories, improving the diversity and quality of training data during online updates.
- Return-to-go Alignment: VDT implements a return-to-go (RTG) alignment mechanism. Instead of conditioning on a fixed, predefined RTG as in offline training, the RTG token is dynamically updated at each timestep with the actual rewards collected by the agent during online interaction.



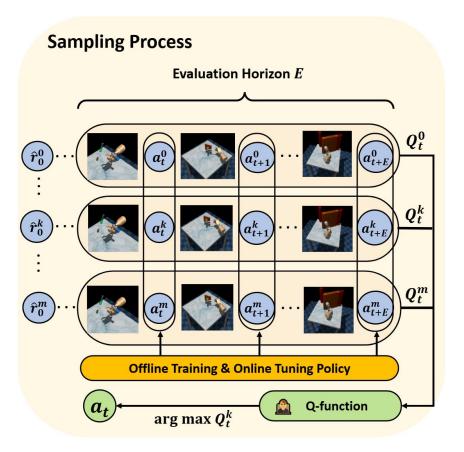
# **Sampling Process**

### **Algorithm 3** Sampling Process

```
Input: Initial state s_0, candidate RTGs \{\hat{r}_0^1,...,\hat{r}_0^m\}, Evaluation horizon E, Discount \gamma, Policy
\pi_{DT}, Q-networks Q_{\hat{\theta}_1}, Q_{\hat{\theta}_2}
Initialize: Current state s_t \leftarrow s_0, Active trajectories \{\tau^k\}_{k=1}^m \leftarrow \{(s_0, \hat{r}_0^k)\}_{k=1}^m, Target Q-
networks Q_{\hat{\theta}}.
while not termination condition do
   // Parallel candidate action generation
   for k=1 to m in parallel do
      Sample action a_t^k \sim \pi_{DT}(\tau^k)
   end for
   // Batched trajectory prediction
   for k = 1 to m in parallel do
       Initialize predicted trajectory \tau_{\text{pred}}^k \leftarrow (s_t, a_t^k)
       Initialize cumulative Q-value Q_{\text{total}}^k \leftarrow 0
      for i = 0 to E - 1 do
          Predict next state: s_{t+i+1}^k \leftarrow \text{EnvModel}(\tau_{\text{nred}}^k)
          Sample next action: a_{t+i+1}^k \sim \pi_{DT}(\tau_{\text{pred}}^k)
          Compute Q-value: q_i^k = \min_{j=1,2} Q_{\hat{\theta}_j}(s_{t+i}^k, a_{t+i}^k)
          Accumulate: Q_{\text{total}}^k \leftarrow Q_{\text{total}}^k + \gamma^i q_i^k
          Append (a_{t+i+1}^k, s_{t+i+1}^k) to \tau_{\text{pred}}^k
      end for
   end for
   // Optimal action selection
   Select optimal index: k^* \leftarrow \arg\max_{1 \le k \le m} Q_{\text{total}}^k
   Execute action: a_t \leftarrow a_t^{k^*}
   // Environment interaction & trajectory update
   Observe reward r_t, next state s_{t+1} from environment
   for k=1 to m do
      Update RTG: \hat{r}_{t+1}^k \leftarrow \hat{r}_t^k - r_t
      Append transition: \tau^k \leftarrow \tau^k \oplus (a_t, r_t, s_{t+1}, \hat{r}_{t+1}^k)
   end for
   t \leftarrow t + 1
end while
```

$$Q_{t}^{k} = \sum_{i=0}^{E} \gamma^{i} \cdot Q(s_{t+i}^{k}, a_{t+i}^{k})$$





# **Experiment**



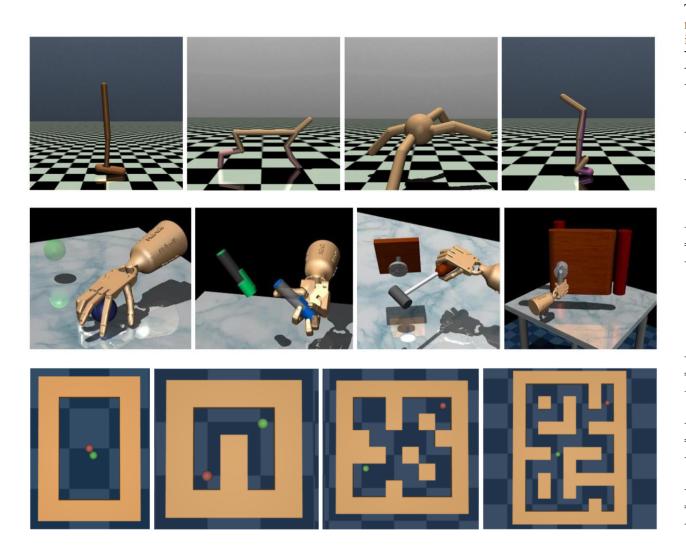


Table 1: Offline training performance of VDT and state-of-the-art baselines on D4RL tasks. For VDT, results are reported as the mean and standard error of normalized rewards over 30 random rollouts (3 independently trained models with 10 trajectories each), generally showing low variance.

Dataset	Value-Based Methods				Conditional Sequence Modeling Methods							
Gym Tasks	BEAR	BCQ	CQL	IQL	MoRel	BC	DT	StAR	GDT	CGDT	DC	VDT
halfcheetah-medium-replay-v2	38.6	34.8	37.5	44.1	40.2	36.6	36.6	36.8	40.5	40.4	41.3	39.4 ±2.0
hopper-medium-replay-v2	33.7	31.1	95.0	92.1	93.6	18.1	82.7	29.2	85.3	93.4	94.2	96.0 <sub>±1.9</sub>
walker2d-medium-replay-v2	19.2	13.7	77.2	73.7	49.8	32.3	79.4	39.8	77.5	78.1	76.6	82.3 ±2.1
halfcheetah-medium-v2	41.7	41.5	44.0	47.4	42.1	42.6	42.6	42.9	42.9	43.0	43.0	43.9 <sub>±0.7</sub>
hopper-medium-v2	52.1	65.1	58.5	63.8	95.4	52.9	67.6	59.5	77.1	96.9	92.5	98.3 <sub>±0.1</sub>
walker2d-medium-v2	59.1	52.0	72.5	79.9	77.8	75.3	74.0	73.8	76.5	79.1	79.2	81.6 <sub>±1.7</sub>
halfcheetah-medium-expert-v2	53.4	69.6	91.6	86.7	53.3	55.2	86.8	93.7	93.2	93.6	93.0	93.9 <sub>±0.1</sub>
hopper-medium-expert-v2	96.3	109.1	105.4	91.5	108.7	52.5	107.6	111.1	111.1	107.6	110.4	111.5 <sub>±3.8</sub>
walker2d-medium-expert-v2	40.1	67.3	108.8	109.6	95.6	107.5	108.1	109.0	107.7	109.3	109.6	110.4 <sub>±0.9</sub>
Average	48.2	53.8	77.6	76.5	72.9	52.6	76.2	66.2	79.1	82.4	82.2	84.1
Adroit Tasks	BEAR	BCQ	CQL	IQL	MoRel	EDAC	BC	DT	D-QL	StAR	GDT	VDT
pen-human-v1	-1.0	66.9	37.5	71.5	-3.2	52.1	63.9	79.5	72.8	77.9	92.5	126.7 <sub>±4.3</sub>
hammer-human-v1	2.7	0.9	4.4	1.4	2.3	0.8	1.2	3.7	0.2	3.7	5.5	3.2 ±0.3
door-human-v1	2.2	-0.05	9.9	4.3	2.3	10.7	2.0	14.8	0.0	1.5	18.6	19.7 <sub>±0.5</sub>
pen-cloned-v1	-0.2	50.9	39.2	37.3	-0.2	68.2	37.0	75.8	57.3	33.1	86.2	145.6 <sub>±4.0</sub>
hammer-cloned-v1	2.3	0.4	2.1	2.1	2.3	0.3	0.6	3.0	3.1	0.3	8.9	19.6 <sub>±1.6</sub>
door-cloned-v1	2.3	0.01	0.4	1.6	2.3	9.6	0.0	16.3	0.0	0.0	19.8	30.6 <sub>±0.7</sub>
Average	1.0	19.8	15.6	19.7	1.0	23.6	17.5	32.2	22.2	19.4	38.9	57.6
Kitchen Tasks	BEAR	BCQ	CQL	IQL	O-RL	BC	DT	DD	StAR	GDT	DC	VDT
kitchen-complete-v0	0.0	8.1	43.8	62.5	2.0	65.0	50.8	65.0	40.8	43.8	40.9	65.9 <sub>±0.2</sub>
kitchen-partial-v0	13.1	18.9	49.8	46.3	35.5	33.8	57.9	57.0	12.3	73.3	66.8	76.1 <sub>±10.8</sub>
Average	6.6	13.5	46.8	54.4	18.8	51.5	54.4	61.0	26.6	58.6	58.7	71.0
Maze2D Tasks	BEAR	BCQ	CQL	IQL	СОМВО	BC	MPPI	DT	QDT	GDT	DC	VDT
maze2d-umaze-v1	65.7	49.1	86.7	42.1	76.4	85.7	33.2	31.0	57.3	50.4	20.1	88.0 <sub>±4.6</sub>
maze2d-medium-v1	25.0	17.1	41.8	34.9	38.5	38.3	10.2	8.2	13.3	7.8	38.2	60.3 <sub>±0.5</sub>
Average	45.35	33.1	64.3	38.5	72.5	63.6	21.7	19.6	35.3	29.1	57.6	74.2
AntMaze Tasks	BEAR	BCQ	CQL	IQL	O-RL	BC	DT	RvS	StAR	GDT	DC	VDT
antmaze-umaze-v0	73.0	78.9	74.0	87.1	64.3	54.6	59.2	65.4	51.3	76.0	85.0	100.0 <sub>±5.5</sub>
antmaze-umaze-diverse-v0	61.0	55.0	84.0	64.4	60.7	45.6	66.2	60.9	45.6	69.0	78.5	100.0 <sub>±4.7</sub>
antmaze-medium-diverse-v0	8.0	0.0	53.7	70.0	0.0	0.0	7.5	67.3	0.0	0.0	0.0	30.0 <sub>±2.8</sub>
Average	47.3	44.6	70.6	73.8	41.7	33.4	44.3	75.0	32.3	48.3	54.5	76.7

# **Experiment**

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Table 2: Offline-to-online performance of each method, with average rewards reported before (left of arrow) and after (right of arrow) online tuning.

Dataset	TD3+BC	AWAC	CQL	IQL	PDT	ODT	VDT
halfcheetah-medium-replay-v2	$44.6 \rightarrow 48.1$	$24.3 \rightarrow 39.0$	$45.5 \rightarrow 44.3$	$44.1 \rightarrow 44.0$	$31.4 \rightarrow 42.8$	$39.9 \rightarrow 40.4$	$39.4 \rightarrow 49.2$
hopper-medium-replay-v2	$60.9 \rightarrow 90.7$	$77.3 \rightarrow 79.6$	$95.0 \rightarrow 95.3$	$92.1 \rightarrow 93.5$	$84.5 \rightarrow 94.8$	$86.6 \rightarrow 88.9$	$96.0 \rightarrow 119.2$
walker2d-medium-replay-v2	$81.8 \rightarrow 82.0$	$63.8 \rightarrow 44.0$	$77.2 \rightarrow 78.0$	$73.7 \rightarrow 60.9$	$54.5 \rightarrow 79.0$	$68.9 \rightarrow 76.9$	$82.3 \rightarrow 95.5$
halfcheetah-medium-v2	$48.3 \to 50.9$	$37.4 \rightarrow 41.1$	$44.0 \to 29.1$	$47.4 \to 48.0$	39.4 → <b>69.5</b>	42.7→ 42.2	$43.9 \to 53.5$
hopper-medium-v2	$59.3 \rightarrow 64.6$	$72.0 \rightarrow 91.0$	$58.5 \rightarrow 95.7$	$63.8 \rightarrow 44.3$	$74.4 \to 100.2$	$66.9 \rightarrow 97.5$	$98.3 \rightarrow 108.1$
walker2d-medium-v2	$83.7 \rightarrow 85.2$	$30.1 \rightarrow 79.1$	$72.5 \rightarrow 89.4$	$79.9 \rightarrow 68.9$	$63.4 \rightarrow 88.1$	$72.2 \rightarrow 76.8$	$81.6 \rightarrow 89.8$
halfcheetah-medium-expert-v2	$90.7 \to 92.1$	$36.8 \rightarrow 41.0$	$91.6 \rightarrow 99.9$	$86.7 \to 95.3$	$82.6 \rightarrow 93.3$	$36.8 \rightarrow 100.9$	$93.9 \rightarrow 101.7$
hopper-medium-expert-v2	$98.0 \rightarrow 110.2$	$80.9 \rightarrow 111.9$	$105.4 \rightarrow 106.3$	$91.5 \rightarrow 92.9$	$77.0 \rightarrow 80.0$	$74.3 \rightarrow 99.1$	$111.5 \rightarrow \textbf{117.8}$
walker2d-medium-expert-v2	$110.1 \rightarrow 110.1$	$42.7 \rightarrow 78.3$	$108.8 \rightarrow 110.1$	$109.6 \rightarrow 109.6$	$99.1 \rightarrow 108.9$	$62.0 \rightarrow 78.7$	$110.4 \rightarrow \textbf{112.7}$
antmaze-umaze-v0	$78.6 \to 79.1$	$56.7 \to 59.0$	$70.1 \to 99.4$	$86.7 \to 96.0$	$48.6 \rightarrow 66.8$	$53.1 \rightarrow 88.5$	$100.0 \rightarrow 110.0$
antmaze-umaze-diverse-v0	$71.4 \rightarrow 78.1$	$49.3 \rightarrow 49.0$	$31.1 \rightarrow 99.4$	$75.0 \rightarrow 84.0$	$72.7 \rightarrow 79.3$	$50.2 \rightarrow 56.0$	$100.0 \rightarrow \textbf{100.0}$
antmaze-medium-diverse-v0	$0.0 \rightarrow 56.7$	$0.7 \rightarrow 0.3$	$23.0 \rightarrow 32.3$	$68.3 \rightarrow 72.0$	$8.0 \rightarrow 63.4$	$0.8 \rightarrow 55.6$	$20.0 \rightarrow 75.0$
Average	79.0	59.4	81.6	75.78	80.51	75.13	94.38

Table 3: Ablation study on model components during offline training. We have abbreviated some task names for simplicity, which does not affect understanding. All experiments are repeated three times, and the average value is taken.

Advantage Weighting	Regularization	Sampling	hopper-m	walker-m-e	pen-cloned	maze2d-m	antmaze-u
$\checkmark$			90.3	99.9	86.1	12.1	75.1
	$\checkmark$		88.9	78.1	99.3	30.5	60.9
		$\checkmark$	78.6	80.3	82.0	19.3	0.0
$\checkmark$	$\checkmark$		95.6	103.6	131.8	40.5	95.9
	$\checkmark$	$\checkmark$	98.3	110.4	145.6	60.3	100.0

# **Experiment**



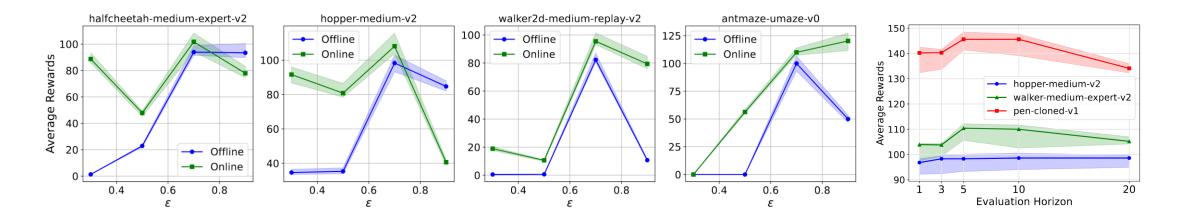


Table 4: Ablation on the computational complexity.

Complexity	Off	line Train	ing	Online Tuning			
Complexity	IQL	ODT	VDT	IQL	ODT	VDT	
Memory ↓	2128 M	3968 M	4024M	2128M	3968 M	4024M	
Params ↑	3.31 M	5.01M	5.24 M	3.31 M	5.01M	5.24 M	
Clock Time ↓	$\approx 6.0 \text{ h}$	$\approx 9.0 \text{ h}$	$\approx 5.0 \text{ h}$	$\approx 10.0 \text{ h}$	$\approx 4.5 \text{ h}$	$\approx 4.0 \text{ h}$	

Table 5: Offline training performance of VDT with different context lengths (K) on Gym tasks.

Datasets	<b>VDT (8)</b>	<b>VDT (20)</b>	<b>VDT</b> (60)	<b>VDT(120)</b>
halfcheetah-medium	28.6	43.9	44.6	43.0
hopper-medium	77.0	98.3	99.1	65.4
walker2d-medium	52.6	81.6	79.9	80.5
halfcheetah-medium-expert	89.5	93.9	93.9	77.0
hopper-medium-expert	109.3	111.5	112.7	111.2
walker2d-medium-expert	100.6	110.4	110.4	103.8
Average	76.3	89.9	90.1	80.2

# **Conclusion**



- We incorporate the value function into the CSM architecture and enhance behavior cloning with advantageweighted learning and regularization constraints. We further provide a theoretical guarantee of its superior performance.
- We leverage the inherent strengths of the value function to fine-tune the policy with a limited number of interactions in the online phase. By introducing the trajectory-level replay buffer and return-to-go alignment, we bridge the gap between offline training and online tuning, offering insights into the design of generalizable architectures.
- We demonstrate the effectiveness of VDT across a broad spectrum of benchmarks, exhibiting superior performance in both pure offline and offline-to-online settings.



# Thanks!

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