

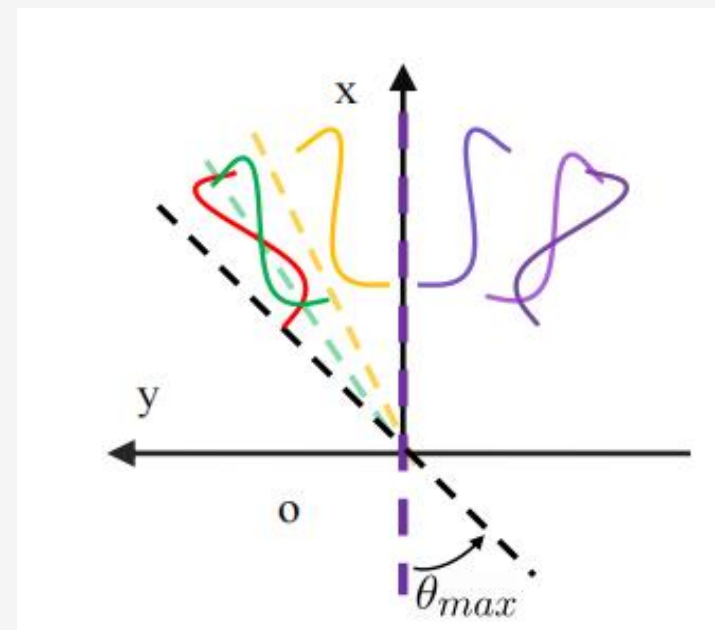
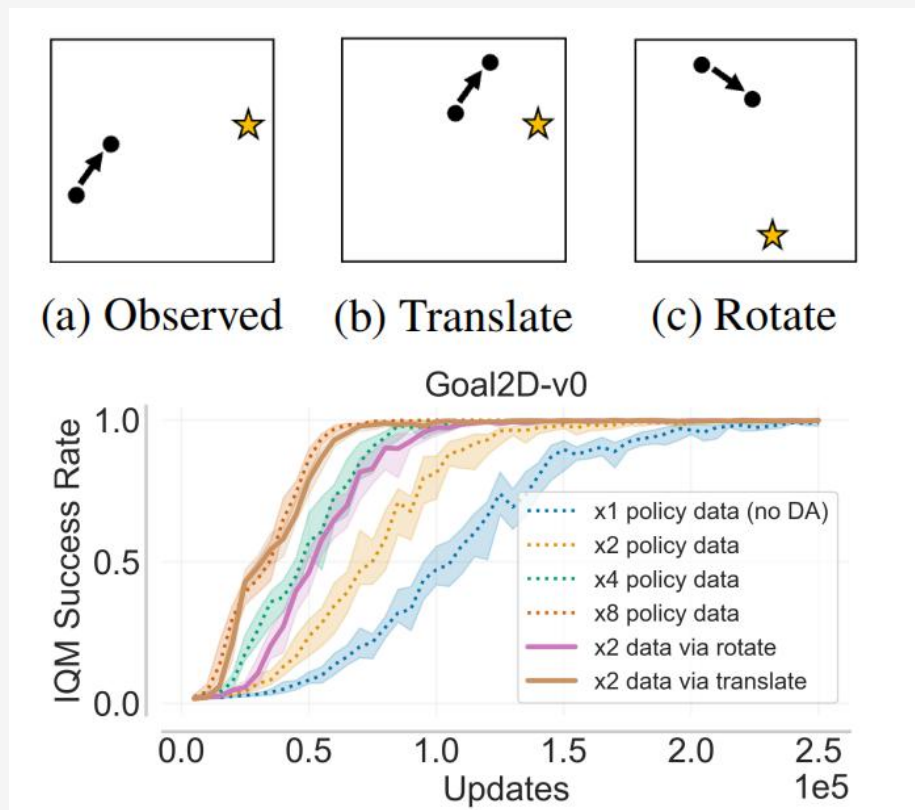
Time Reversal Symmetry for Efficient Robotic Manipulations in Deep Reinforcement Learning

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Symmetry in Deep RL (spatial)

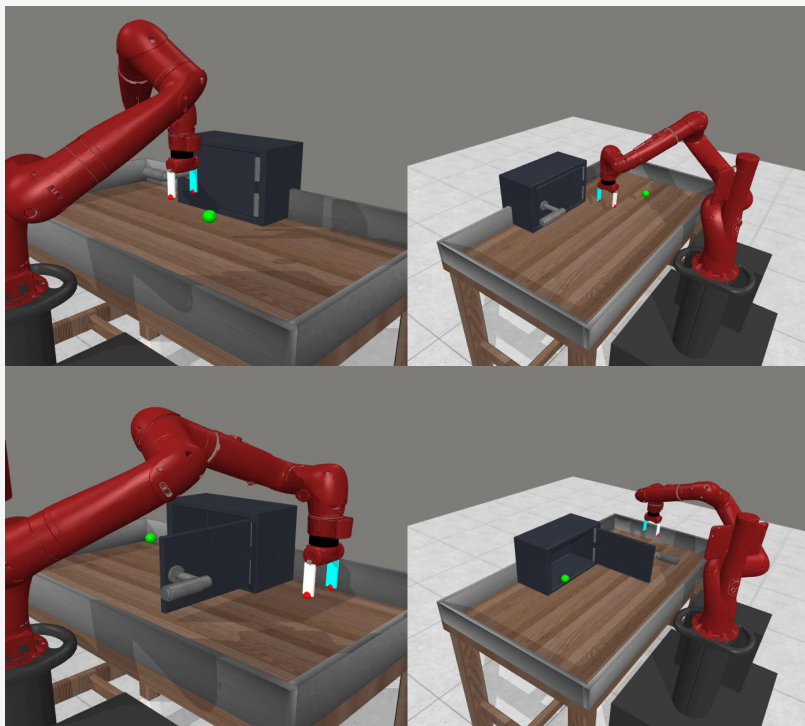


Reflection

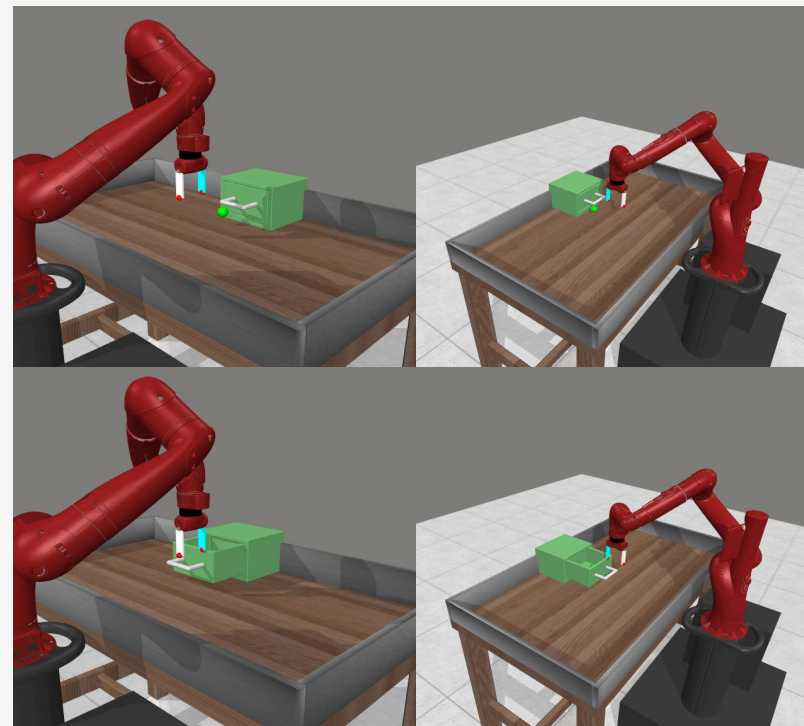
Given the effectiveness of spatial symmetry, can we leverage symmetry in time domain to boost the learning efficiency of deep RL?

Time Reversal Symmetry

- Observation: Tasks often exist as a pair.
- Examples: door opening/closing, drawer opening/closing.



door opening/closing



drawer opening/closing

Time Reversal Symmetry

- Observation: Tasks often exist as a pair.
- Examples: plate slide side (back), window opening/closing.

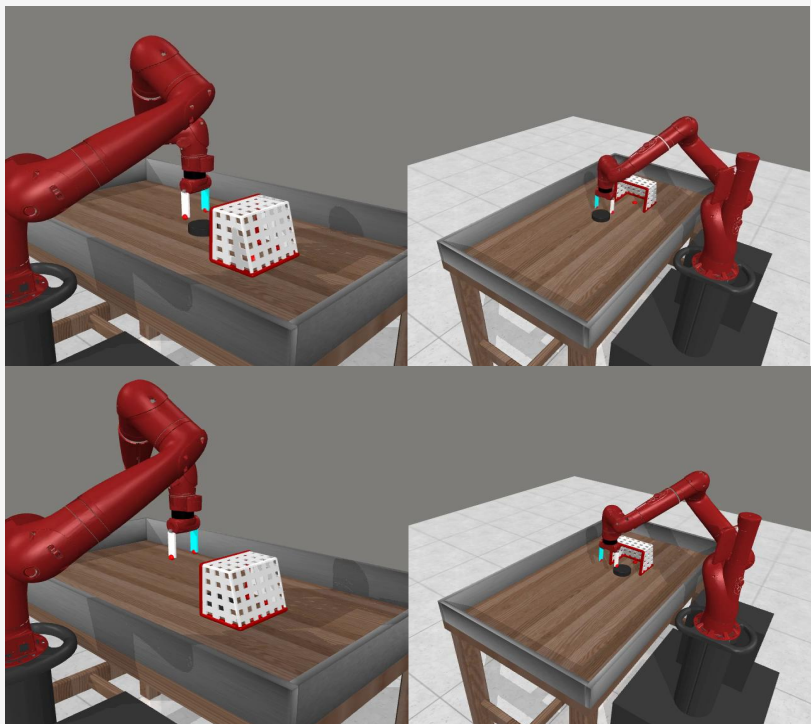
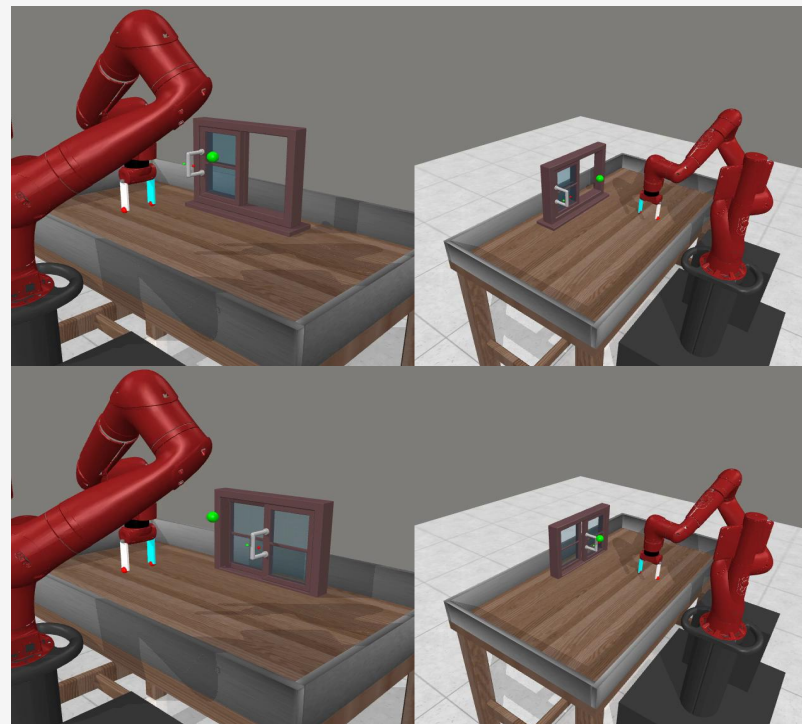
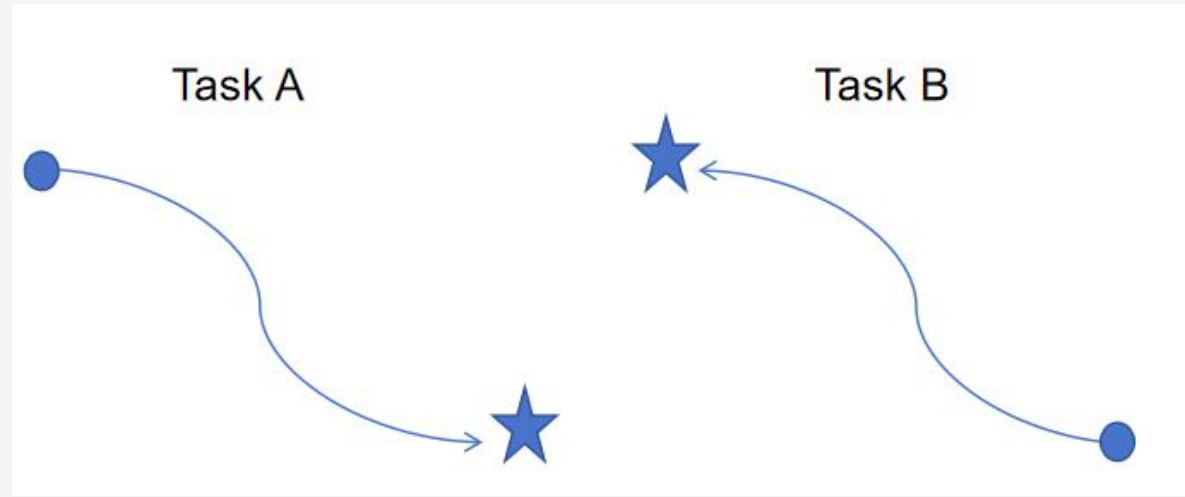


plate slide side (back)



window opening/closing

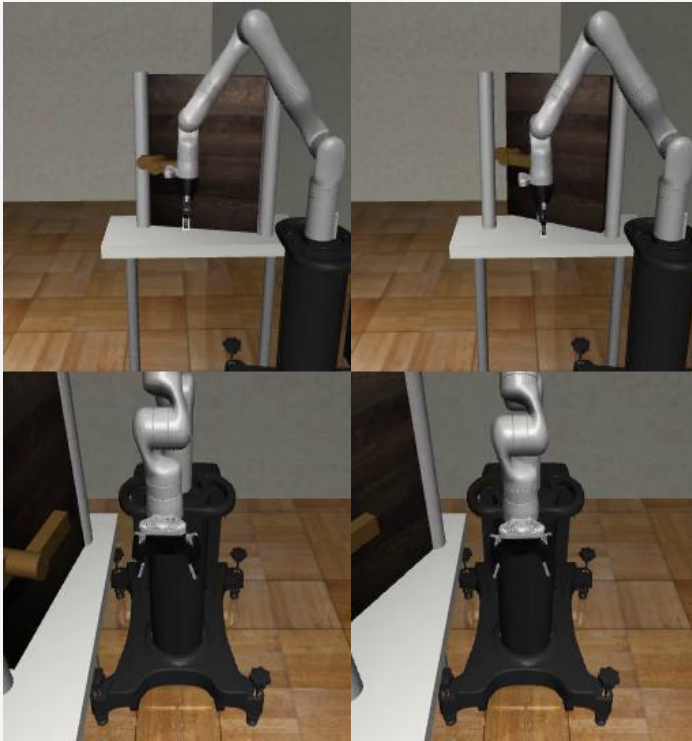
Time Reversal Symmetry



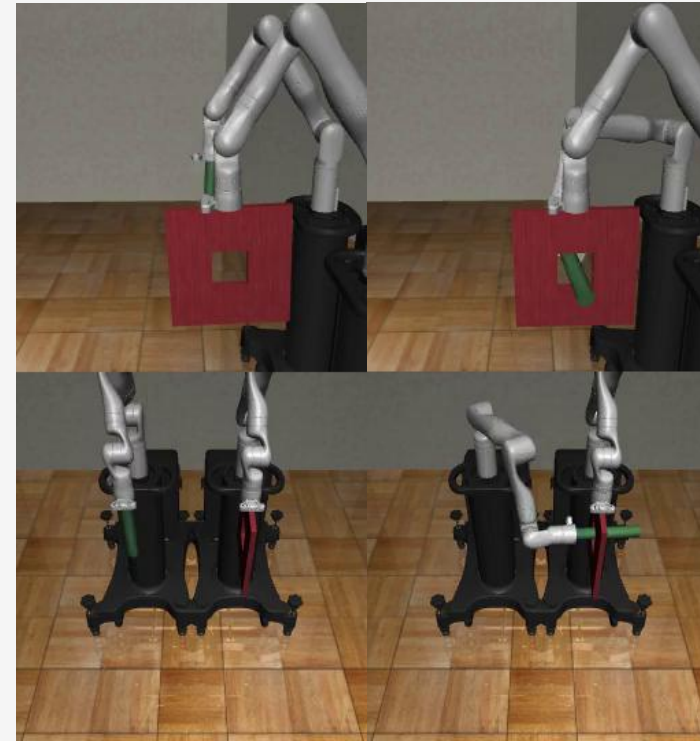
- Hypothesis: For some task pair (A, B), task A can be solved more quickly with reversed trajectories from task B.
- Objective of our work: Develop a method that enhances data efficiency of DRL agents with time reversal symmetry.
- Outcome: An agent that can solve two/multiple tasks simultaneously and much faster with the help of time reversal symmetry.

Full Time Reversal Symmetry

- For one transition (s_t, a_t, s_{t+1}) and the transition function T , if there exists $\overleftarrow{a_t}$ such that $T(s_{t+1}|s_t, a_t) = T(s_t|s_{t+1}, \overleftarrow{a_t})$, we say that the state pair (s_t, s_{t+1}) satisfies full time reversal symmetry.



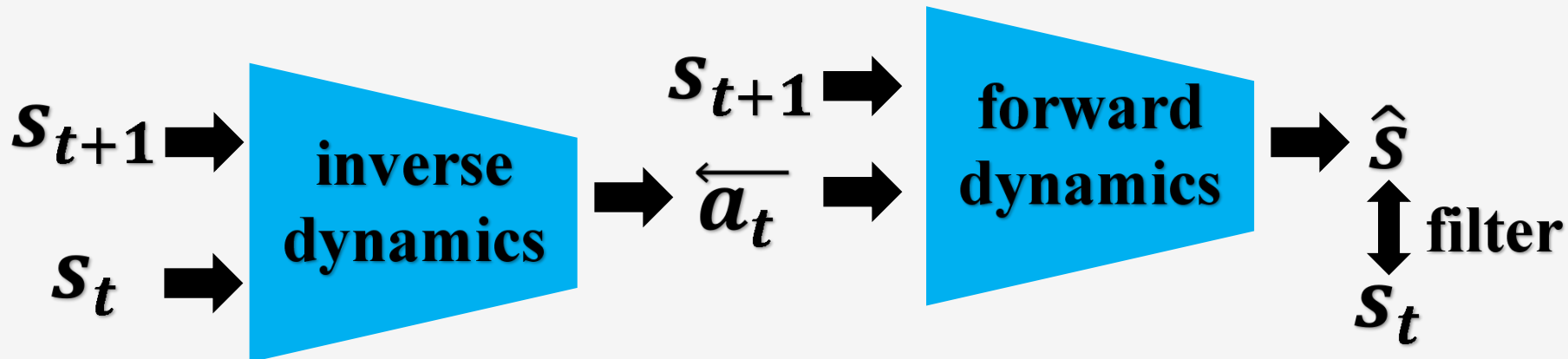
door opening/closing outward



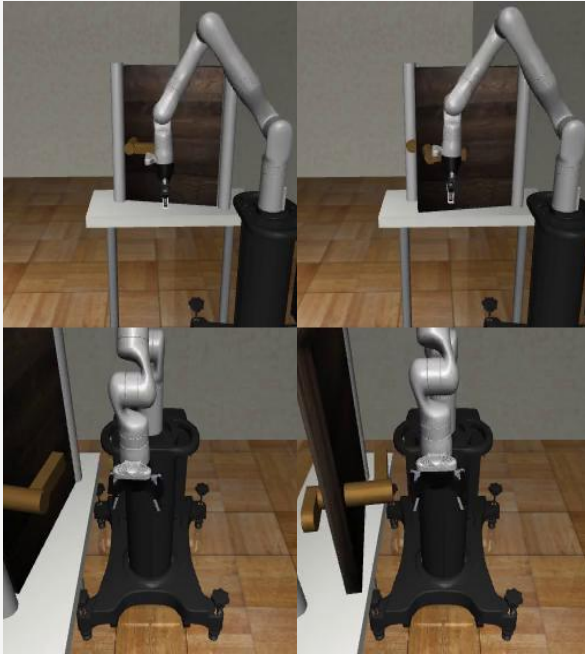
peg insertion/removal

Proposed Technique1: Trajectory Reversal Augmentation with Dynamics-Aware Filtering

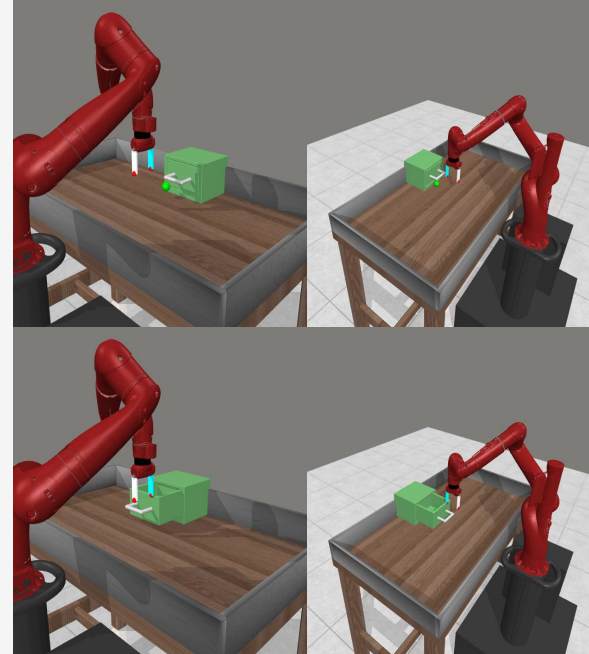
- Reverse transitions: $(s_t, a_t, s_{t+1}) \rightarrow (s_{t+1}, \overleftarrow{a}_t, s_t)$.
- Core idea: **data augmentation** using reversed transitions.
- Filter out fake (irreversible) transitions.
 1. Train an inverse dynamics model: output \overleftarrow{a}_t with s_{t+1} and s_t as inputs.
 2. Train a forward dynamics model: output \hat{s} with s_{t+1} and \overleftarrow{a}_t as inputs.
 3. Filter based on the error between s_t and \hat{s} .



What if there are lots of irreversible transitions?



door opening/closing inward

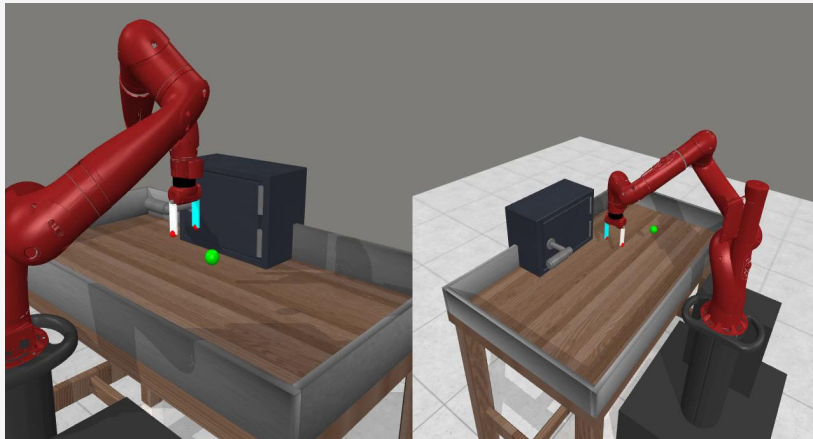


drawer opening/closing

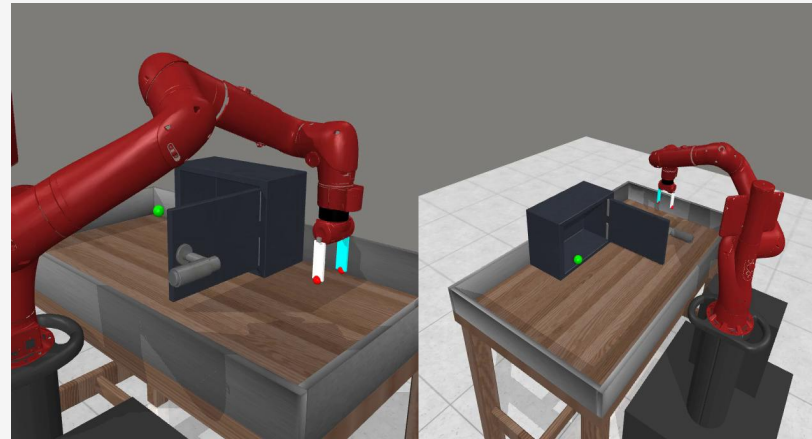
- The robotic arm is opening the door/drawer by **grasping and pulling** it while closing the door/drawer by **pushing** it, which creates irreversible transitions.
- However, we can observe that the trajectories of the objects are actually reversible.
- We need to find out how to leverage this property.

Partial Time Reversal Symmetry

- Assume that a state s can be decomposed into two parts (x, y) .
- For one state pair (s_t, s_{t+1}) and the transition function T , if there exist $(\overleftarrow{y}_t, \overleftarrow{y}_{t+1})$ and $(\overleftarrow{a}_t, \overleftarrow{a}_{t+1})$ such that $T(s_{t+1}|s_t, a_t) = T(\overleftarrow{s}_t|\overleftarrow{s}_{t+1}, \overleftarrow{a}_t)$, we say that the state pair (s_t, s_{t+1}) satisfies partial time reversal symmetry.
- Intuitively, x can be the part that is reversible (eg. containing object state information).



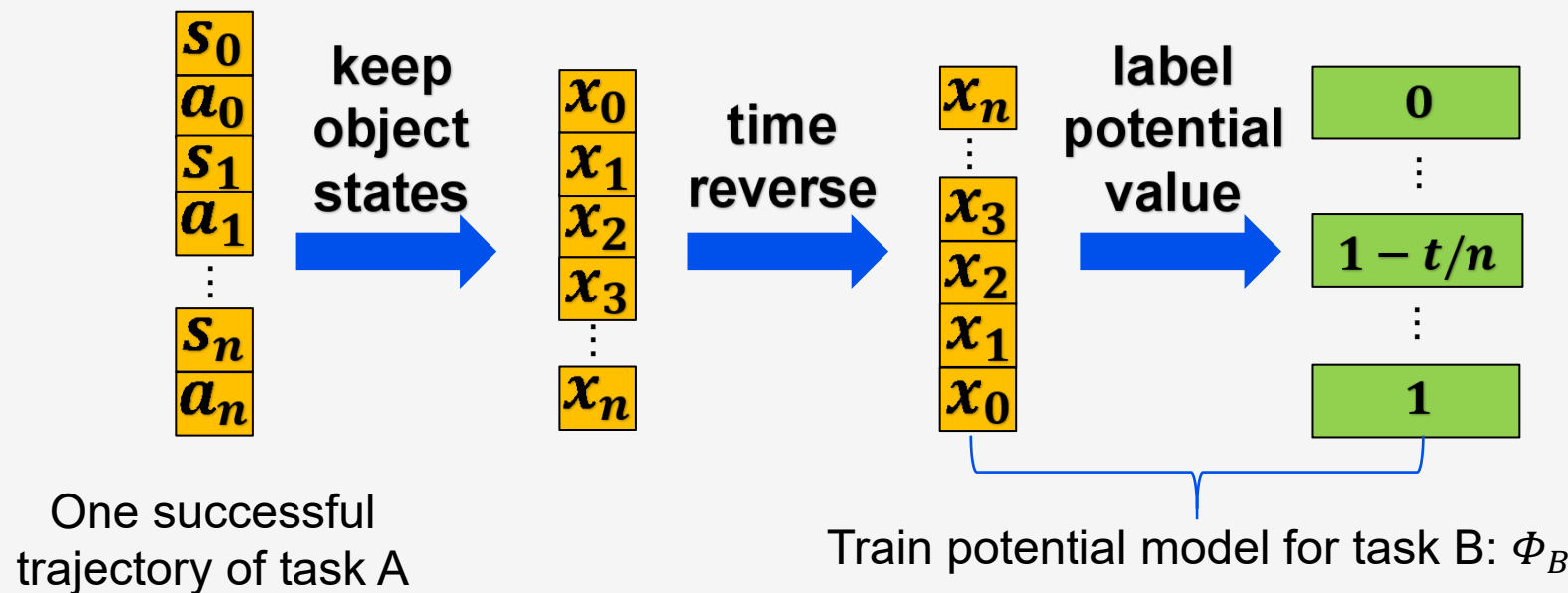
door opening



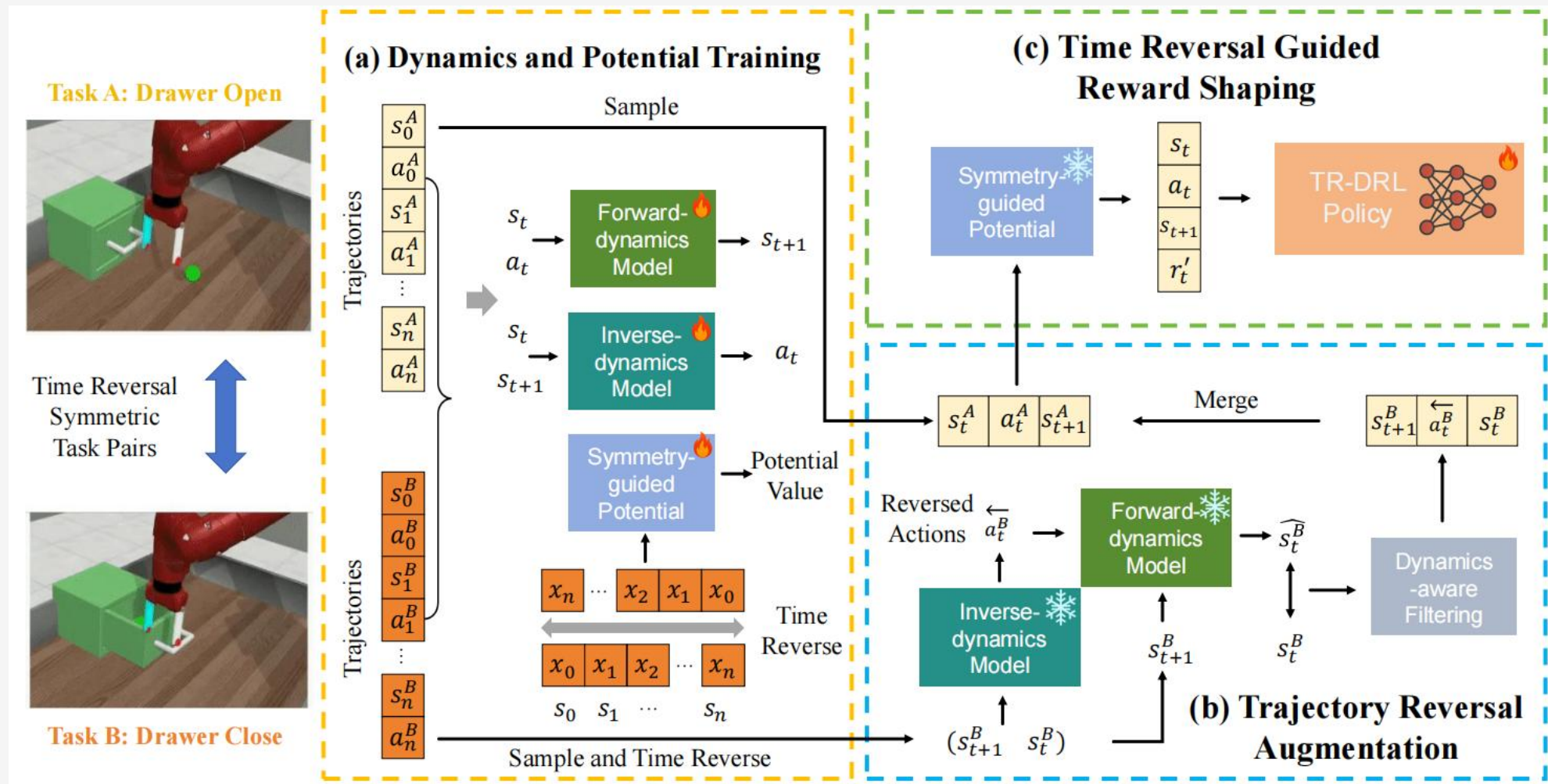
door closing

Proposed Technique2: Time Reversal Symmetry Guided Reward Shaping

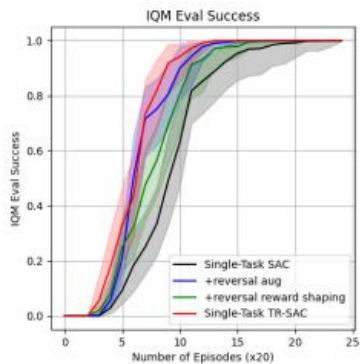
- Core idea: **reward shaping** using reversed trajectories.
 - Use reversed trajectories of object states (reversible part) to relabel the reward terms.
- Train a potential model: output potential value $\Phi(x_t)$ with x_t as input.
 - The reward of one transition (s_t, a_t, s_{t+1}) can be reshaped as $r_t + \Phi(x_{t+1}) - \Phi(x_t)$.



Method Diagram of TR-DRL



Experimental Results in Robosuite



| Method | Number of Environment Transitions | | | |
|---------------------------|-----------------------------------|-----------------|-----------------|-----------------|
| | 50k | 100k | 150k | 200k |
| Single-Task SAC | 0.11 ± 0.07 | 0.62 ± 0.16 | 0.93 ± 0.07 | 0.97 ± 0.03 |
| +reversal aug | 0.22 ± 0.10 | 0.88 ± 0.10 | 0.99 ± 0.01 | 1.00 ± 0.00 |
| +reversal reward shaping | 0.26 ± 0.10 | 0.79 ± 0.12 | 0.97 ± 0.03 | 1.00 ± 0.00 |
| Single-Task TR-SAC (Ours) | 0.33 ± 0.14 | 0.92 ± 0.07 | 1.00 ± 0.00 | 1.00 ± 0.00 |

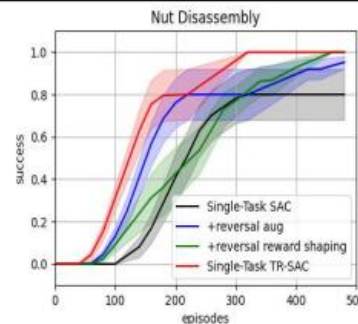
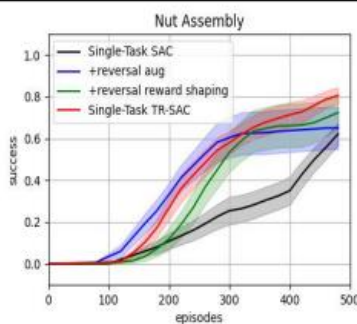
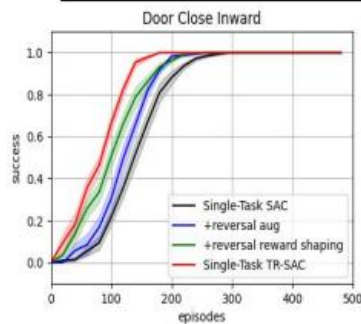
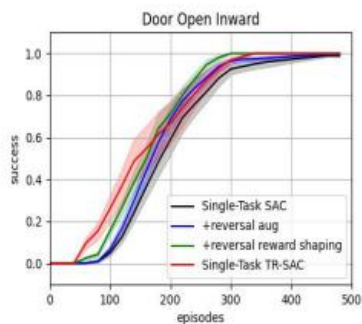


Figure 4: **Results for single-task setting in 10 environments from Robosuite.** Top: Plots and table for IQM of success rate. Bottom: Curves of success rate in two pair of reversible tasks. "Single-Task SAC": baseline; "+reversal aug": trajectory reversal augmentation with dynamics-aware filtering; "+reversal reward shaping": time reversal symmetry guided reward shaping.

Experimental Results in MetaWorld (MT50)

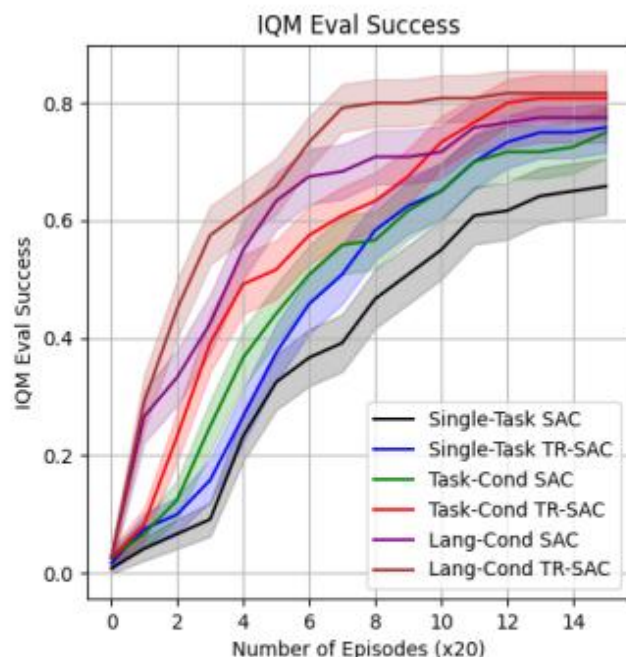


Figure 6: **IQM of success rate for multi-task settings in 12 pair of reversible tasks in MT50 of Meta-World.** "Task-Cond" and "Lang-Cond" are short for "task-conditioned" and "language-conditioned" respectively.

| Method | Number of Environment Transitions | | |
|---------------------------|-----------------------------------|-----------------------------------|-----------------------------------|
| | 50k | 100k | 150k |
| Single-Task SAC | 0.33 ± 0.05 | 0.55 ± 0.05 | 0.66 ± 0.05 |
| Task-Cond SAC | 0.44 ± 0.05 | 0.65 ± 0.05 | 0.75 ± 0.04 |
| Lang-Cond SAC | 0.63 ± 0.05 | 0.72 ± 0.05 | 0.78 ± 0.04 |
| Single-Task TR-SAC (Ours) | 0.38 ± 0.05 | 0.65 ± 0.05 | 0.76 ± 0.04 |
| Task-Cond TR-SAC (Ours) | 0.52 ± 0.05 | 0.73 ± 0.04 | 0.81 ± 0.04 |
| Lang-Cond TR-SAC (Ours) | 0.66 ± 0.05 | 0.81 ± 0.04 | 0.82 ± 0.04 |

Conclusion

- We propose TR-DRL, a framework leveraging time reversal symmetry to enhance sample efficiency of DRL algorithms.
- Key contributions include a novel notion of partial time reversal symmetry, trajectory reversal augmentation with dynamics-aware filtering, and symmetry-guided reward shaping.
- Experiments on Robosuite and Metaworld demonstrate improved agent performance and learning efficiency.

Thanks for watching

- If our work interests you, you may explore further with more video demonstrations on our project website and apply our method using our open-source code repository.



project website



code repository