Diffusion Tree Sampling: Scalable Inference-time alignment of diffusion models

Vineet Jain, Kusha Sareen, Mohammad Pedramfar, Siamak Ravanbakhsh

Goal: Sample from the reward-tilted distribution

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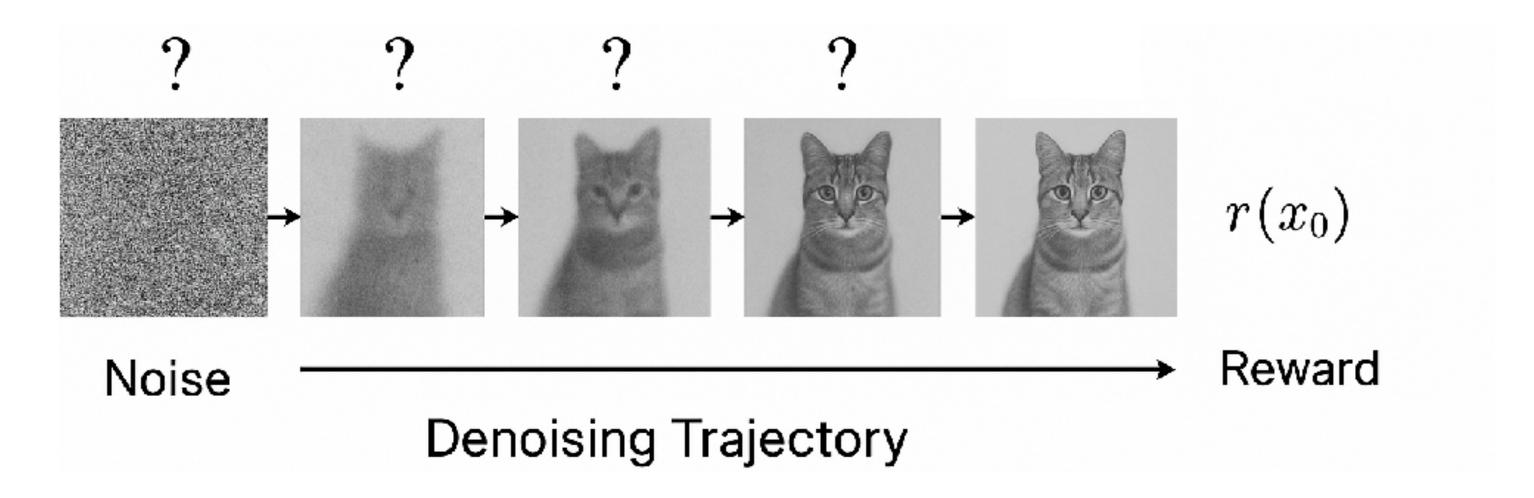
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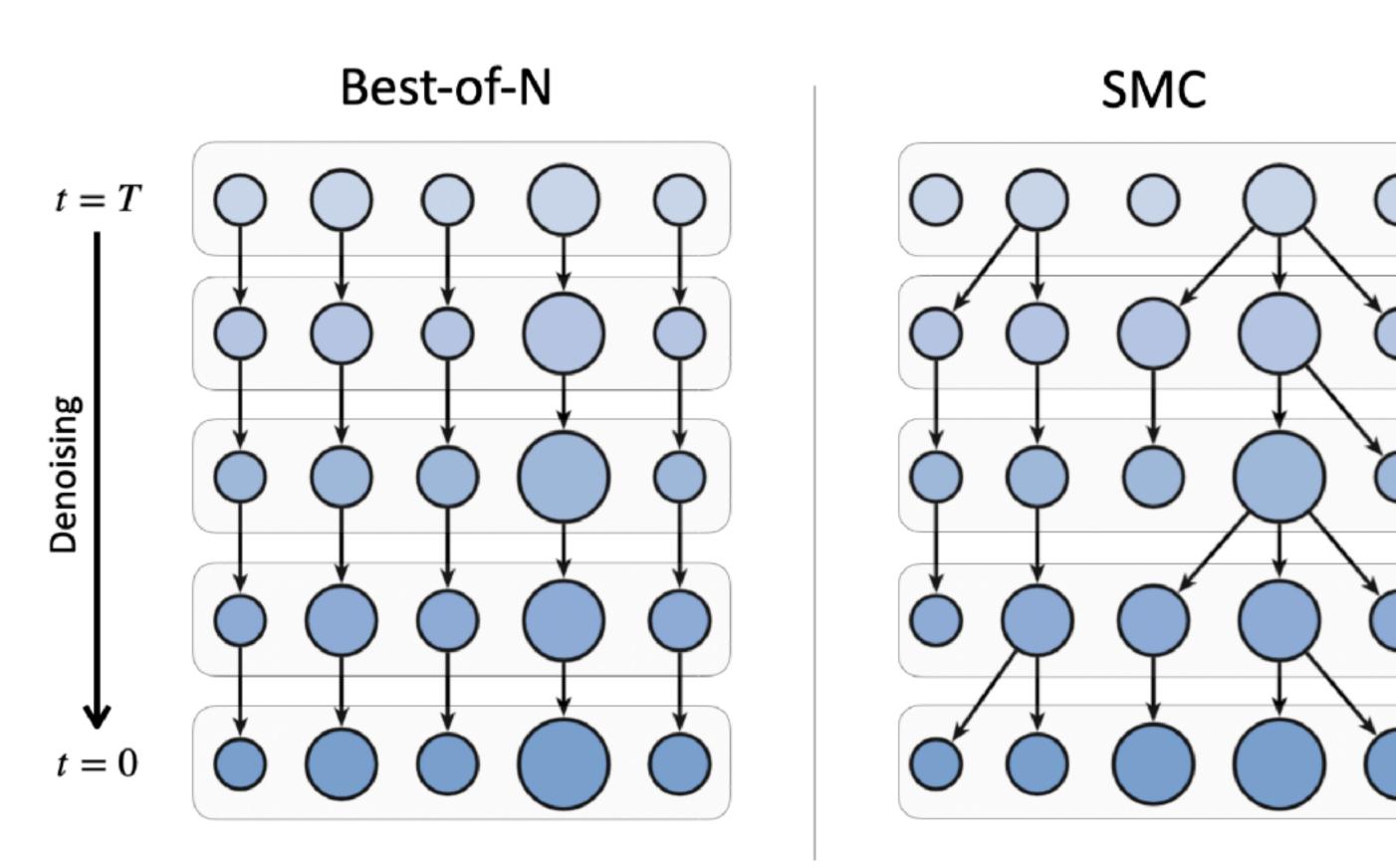
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But credit assignment is hard!



Existing methods

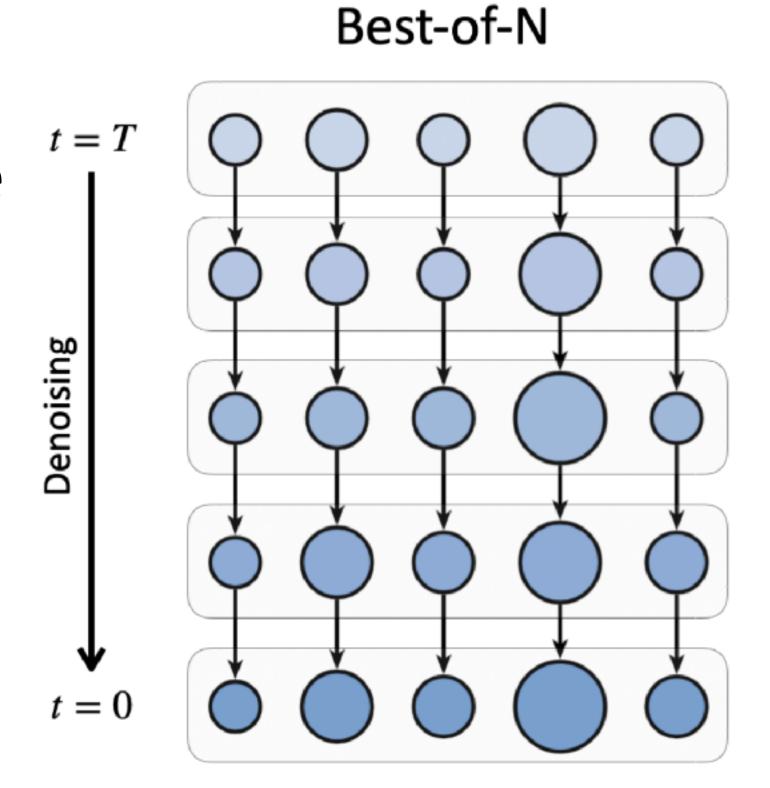
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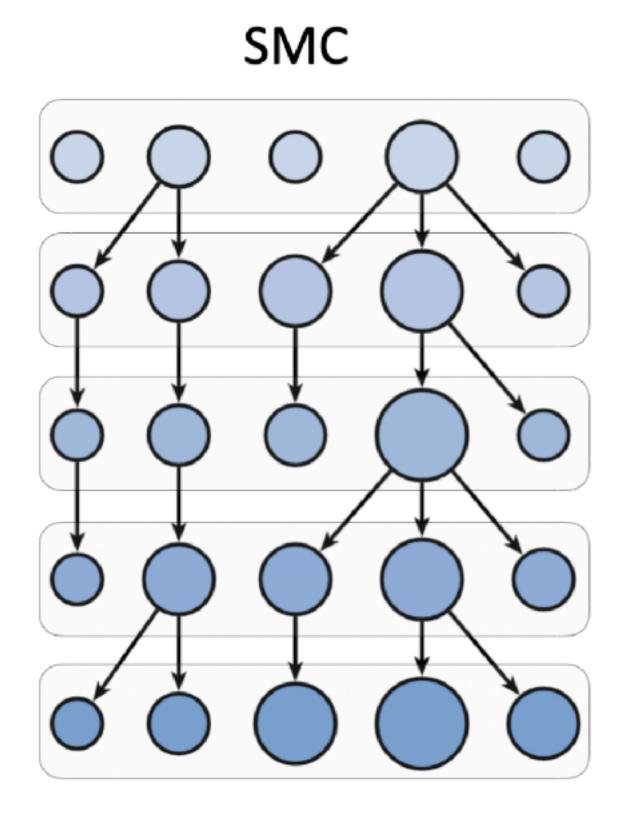


Existing methods

X Biased approximations of the value function at noisy states

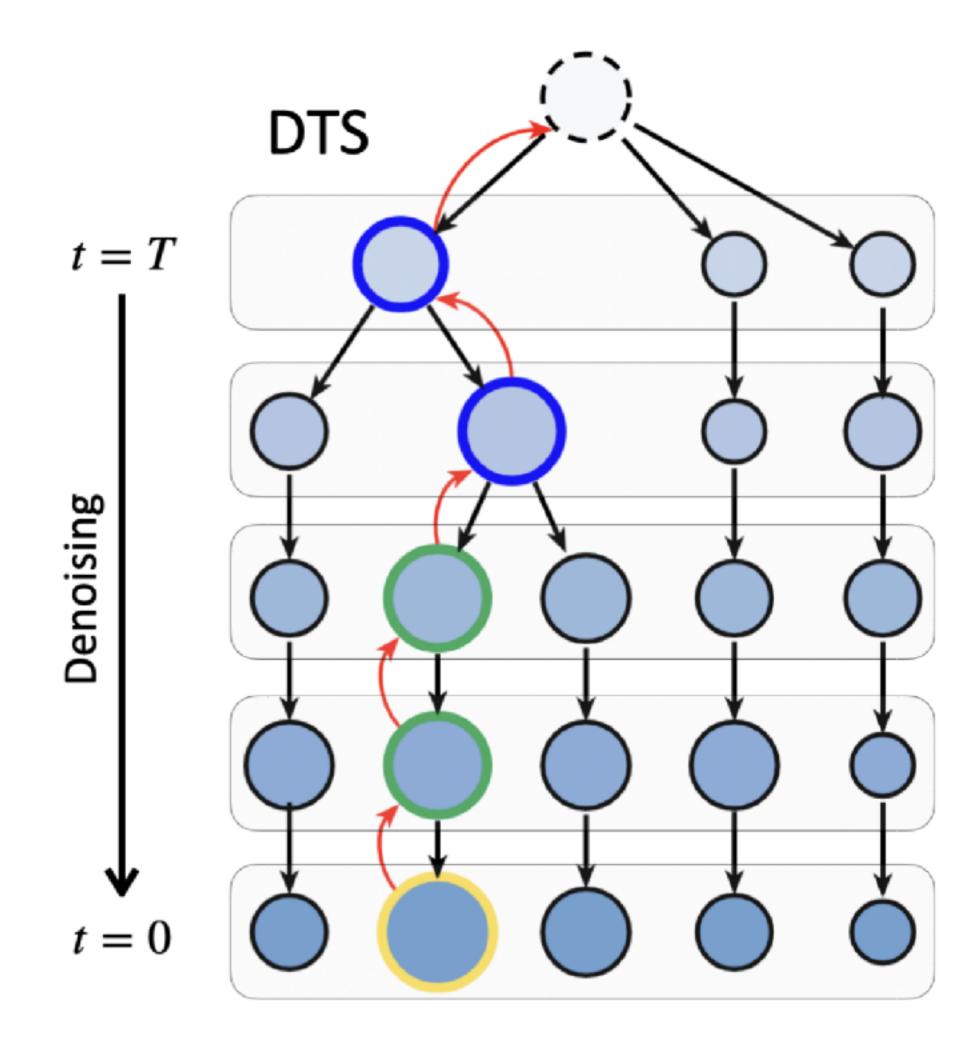
Only scale *in parallel* by increasing particle count





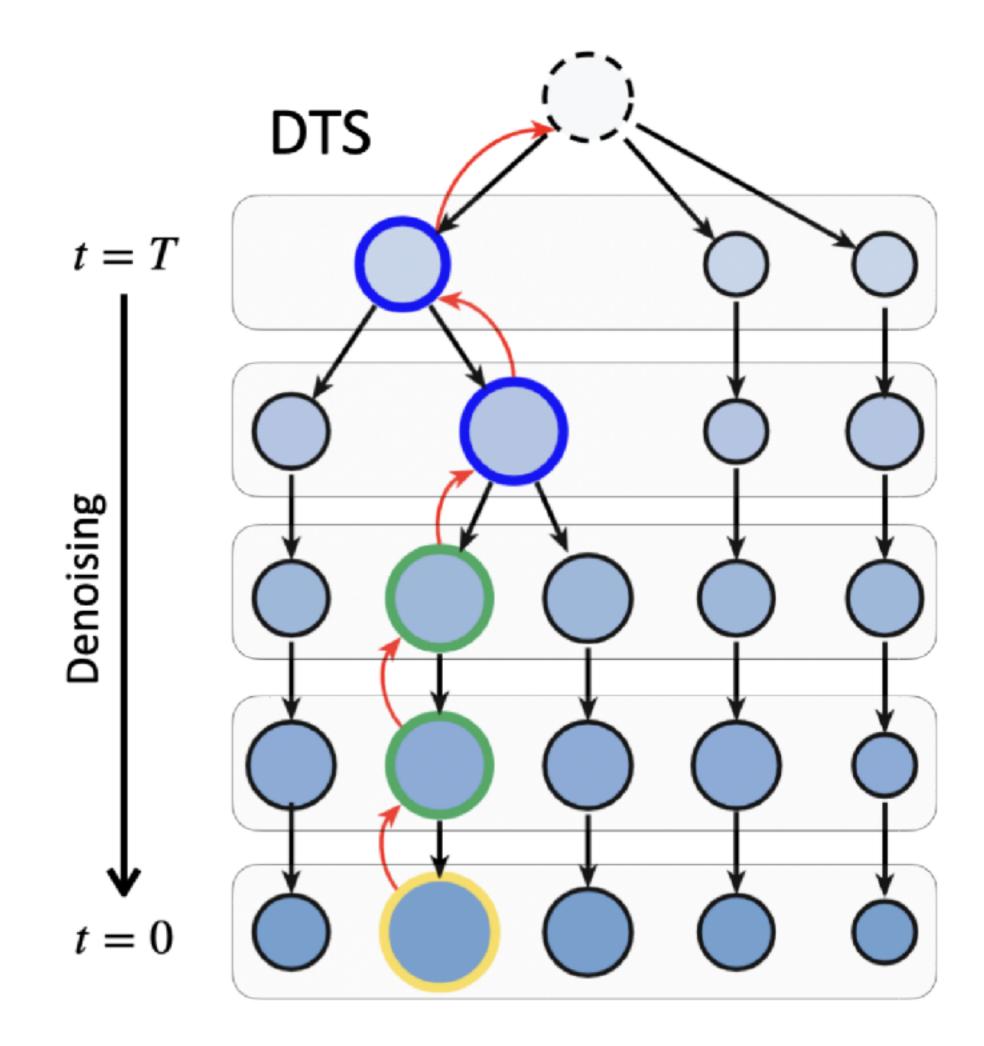
Core idea: Denoising as a tree + value backups

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Treat each noisy x_t as node; denoising as edges Maintain value estimates $\hat{v}(x_t)$ at each node

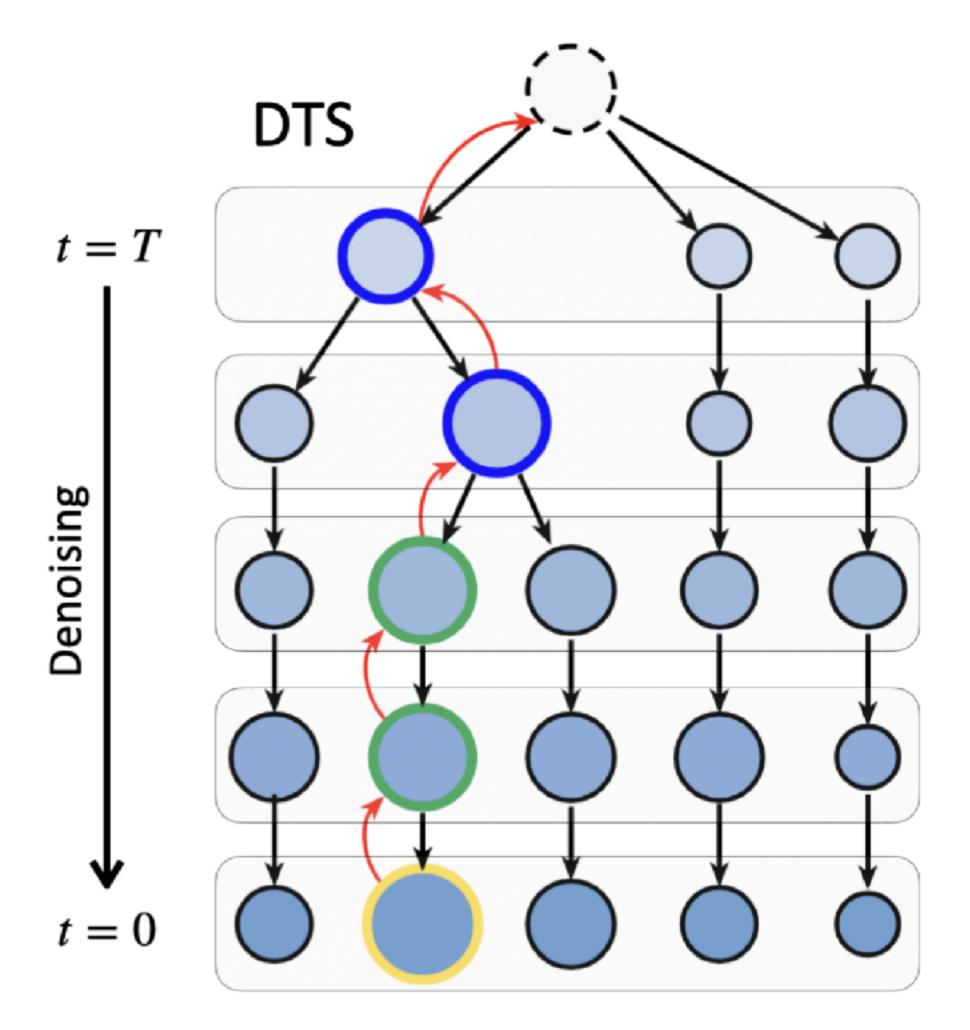


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Selection:

<u>DTS</u> sample $\propto \exp(\hat{v}(x_{t-1})) \rightarrow \text{asymptotically exact for } \pi^*$ <u>DTS*</u> greedy max $\hat{v}(x_{t-1}) \rightarrow \text{efficient high-reward search}$



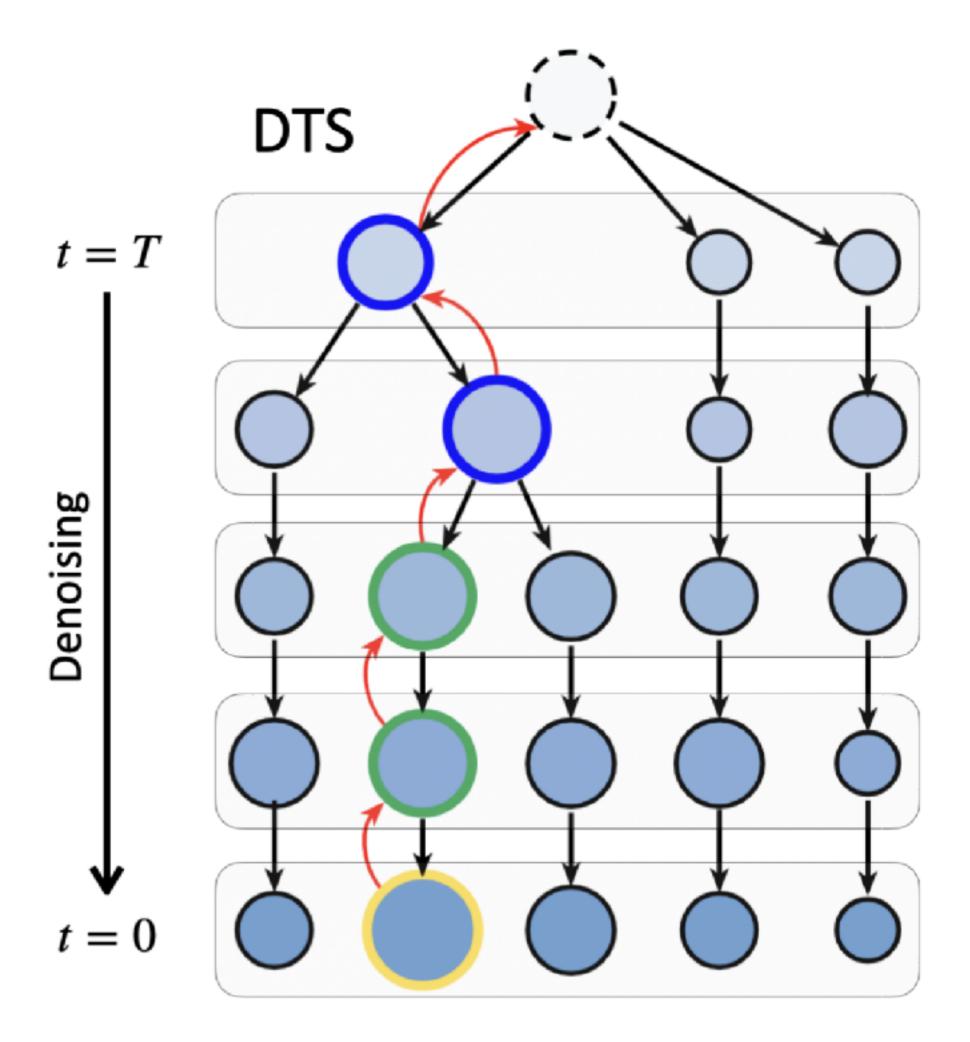
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Rollout: Use base model to create child x_{t-1} from node x_t



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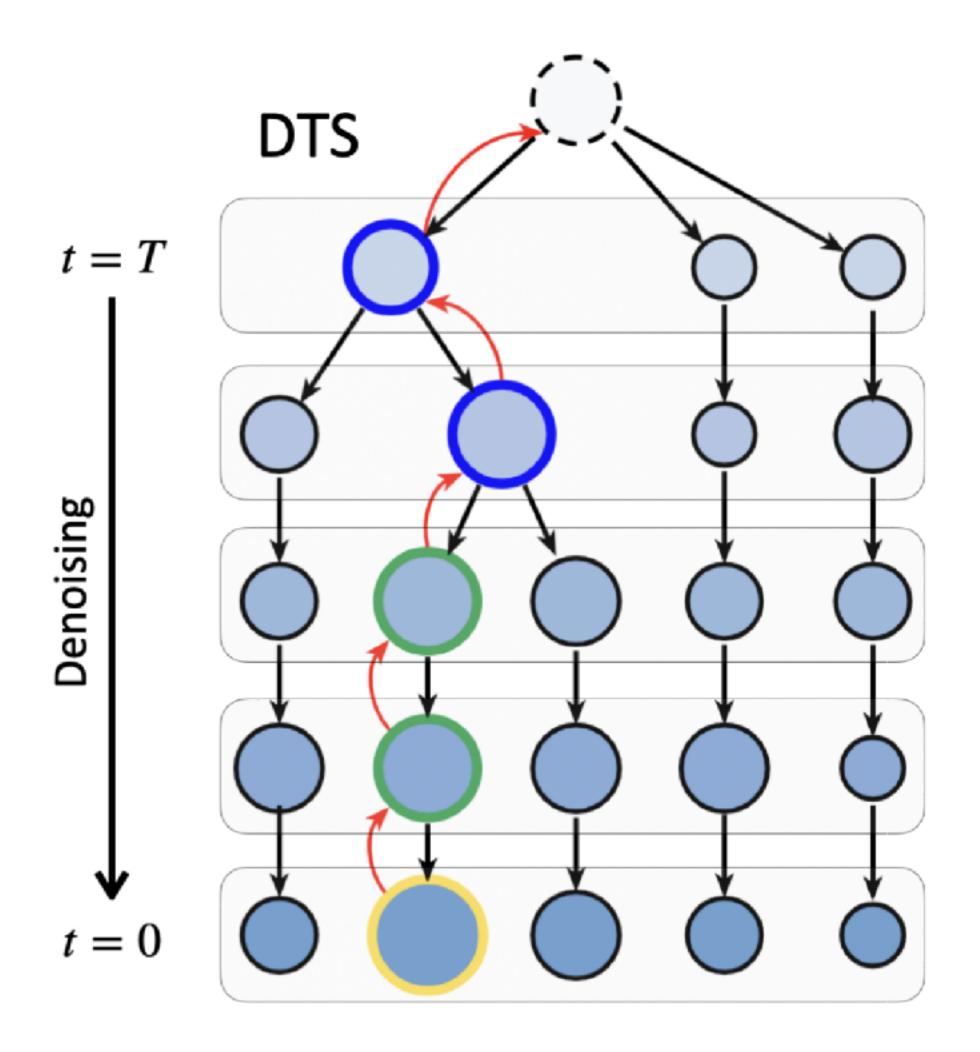
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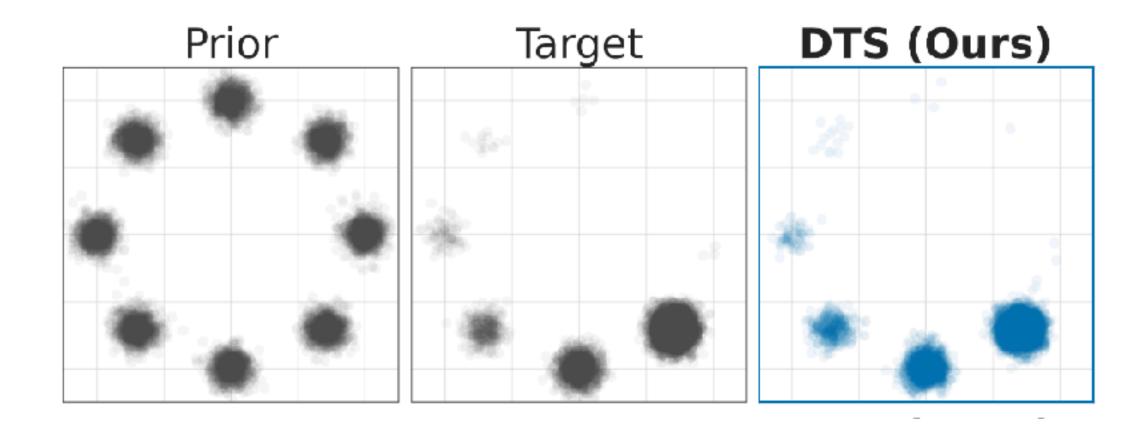
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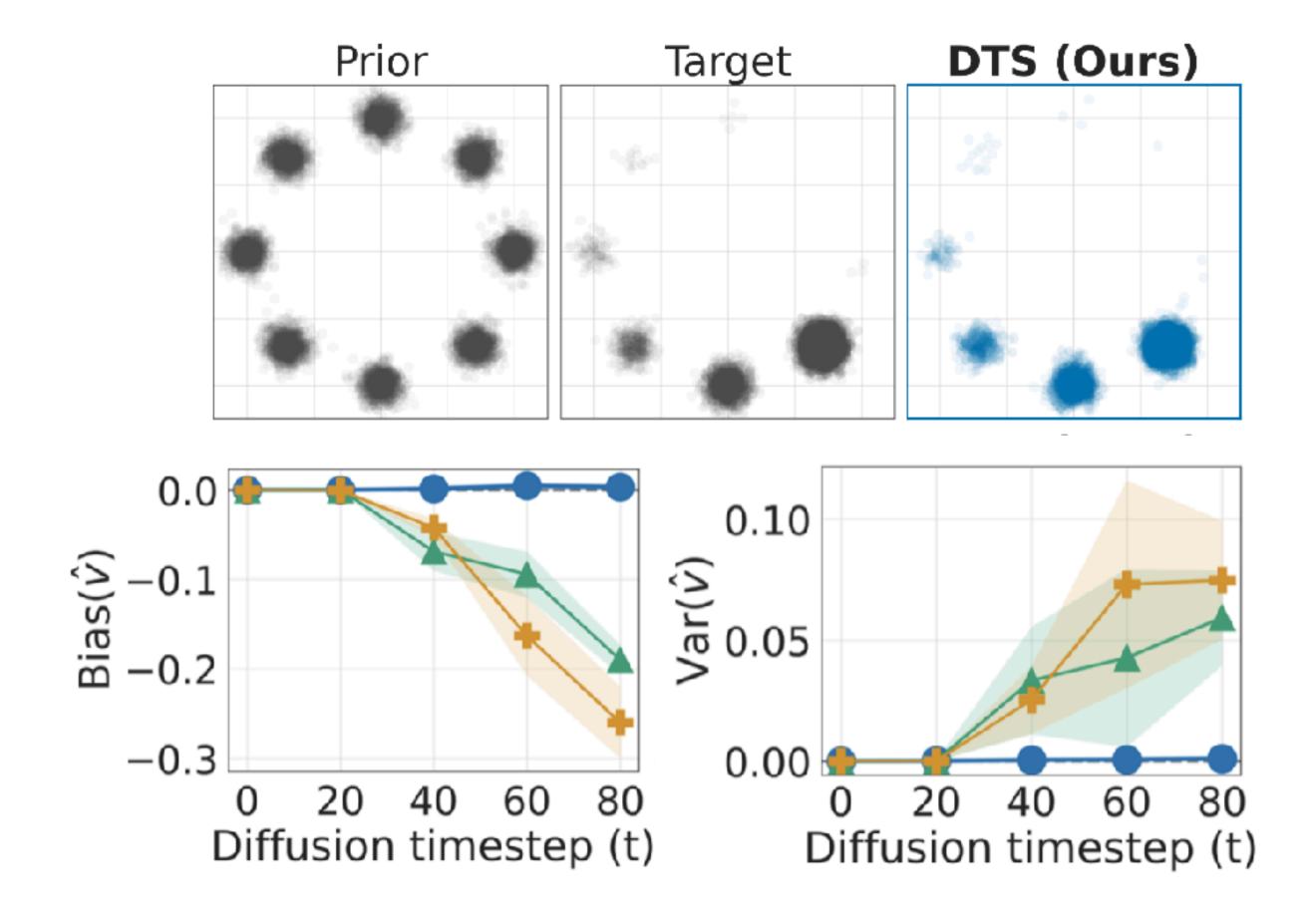
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Backup: Evaluate $r(x_0)$, backup soft (log-sum-exp) values

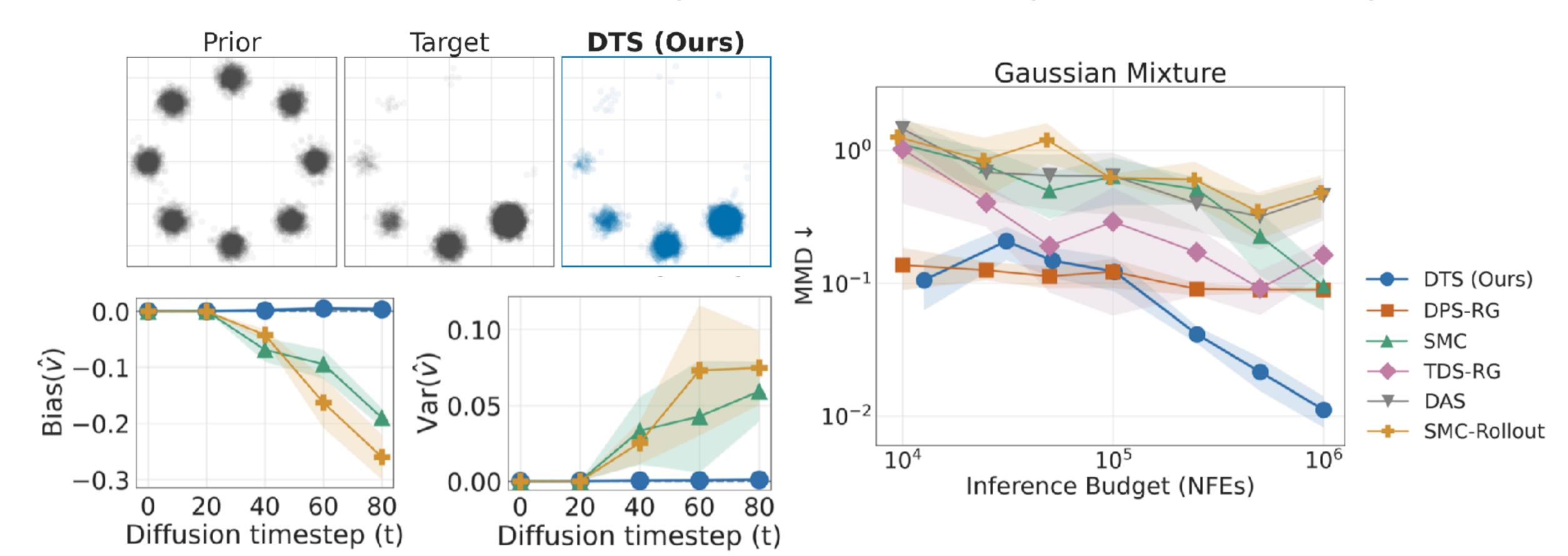




✓ Low-noise rewards back up to high-noise states → better credit assignment



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- Tree reuses estimates → more compute **sequentially** improves values & samples



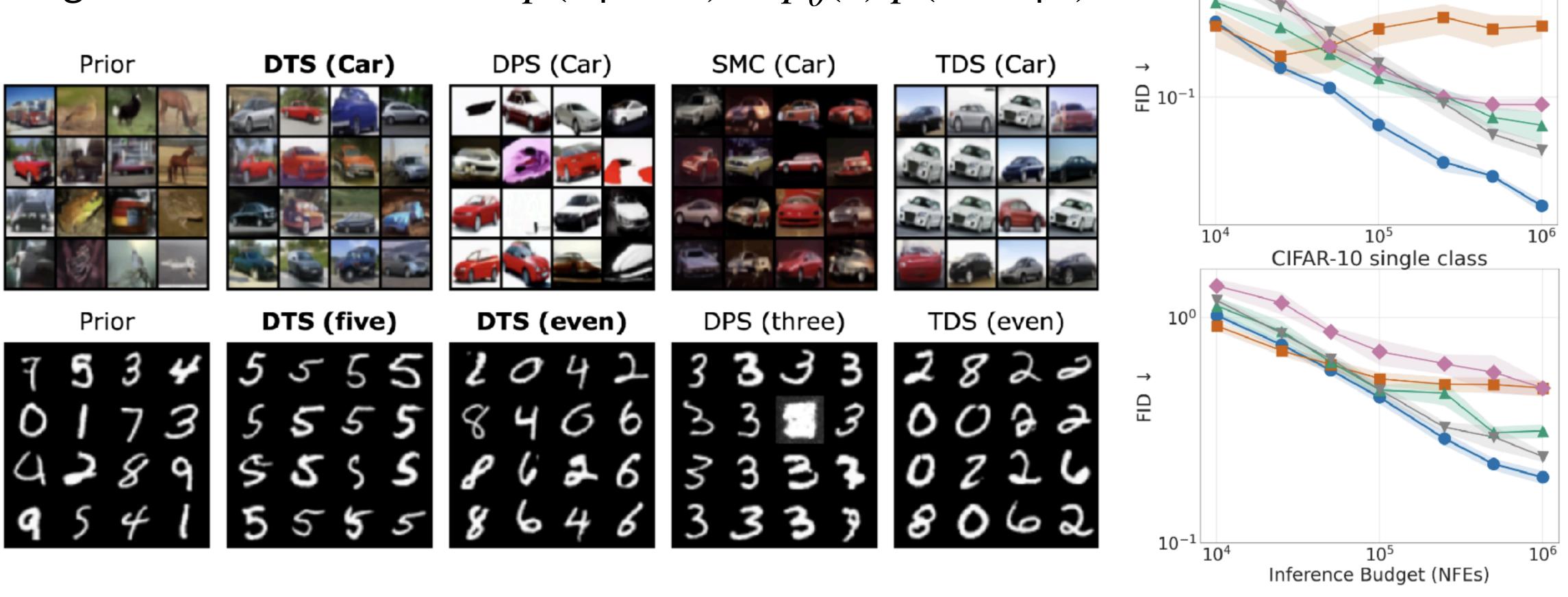
Class-conditional sampling

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Target distribution becomes $p(x \mid class) \propto p_{\theta}(x) p(class \mid x)$

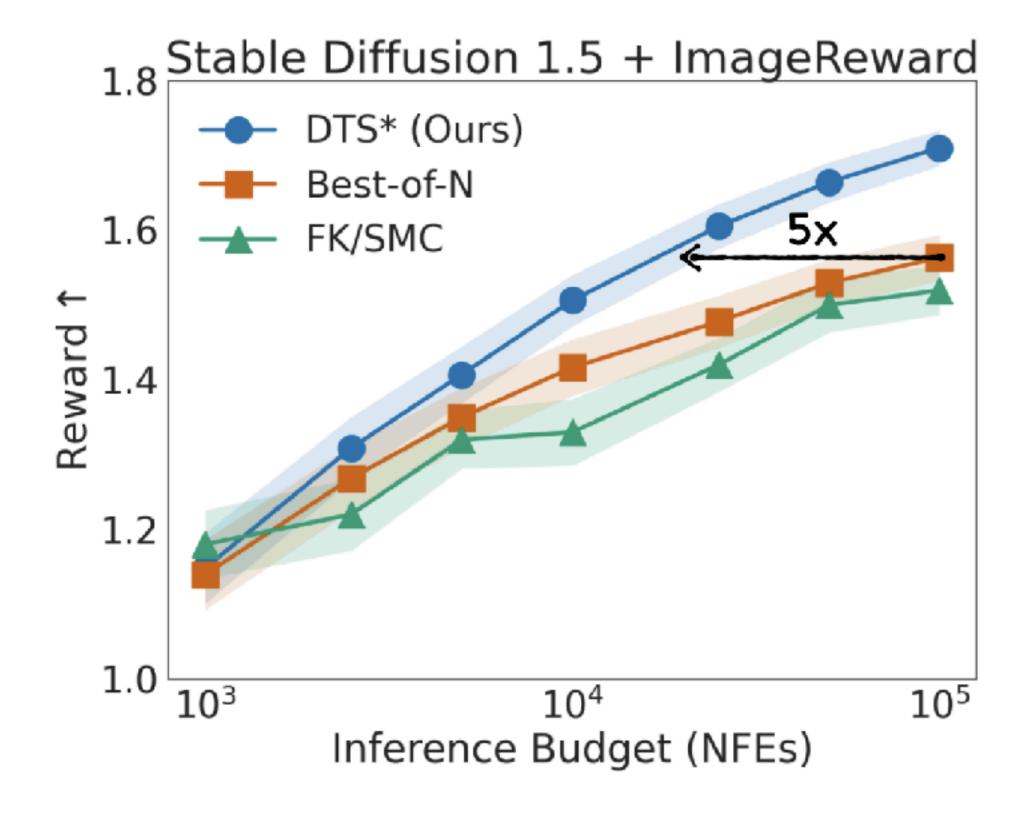
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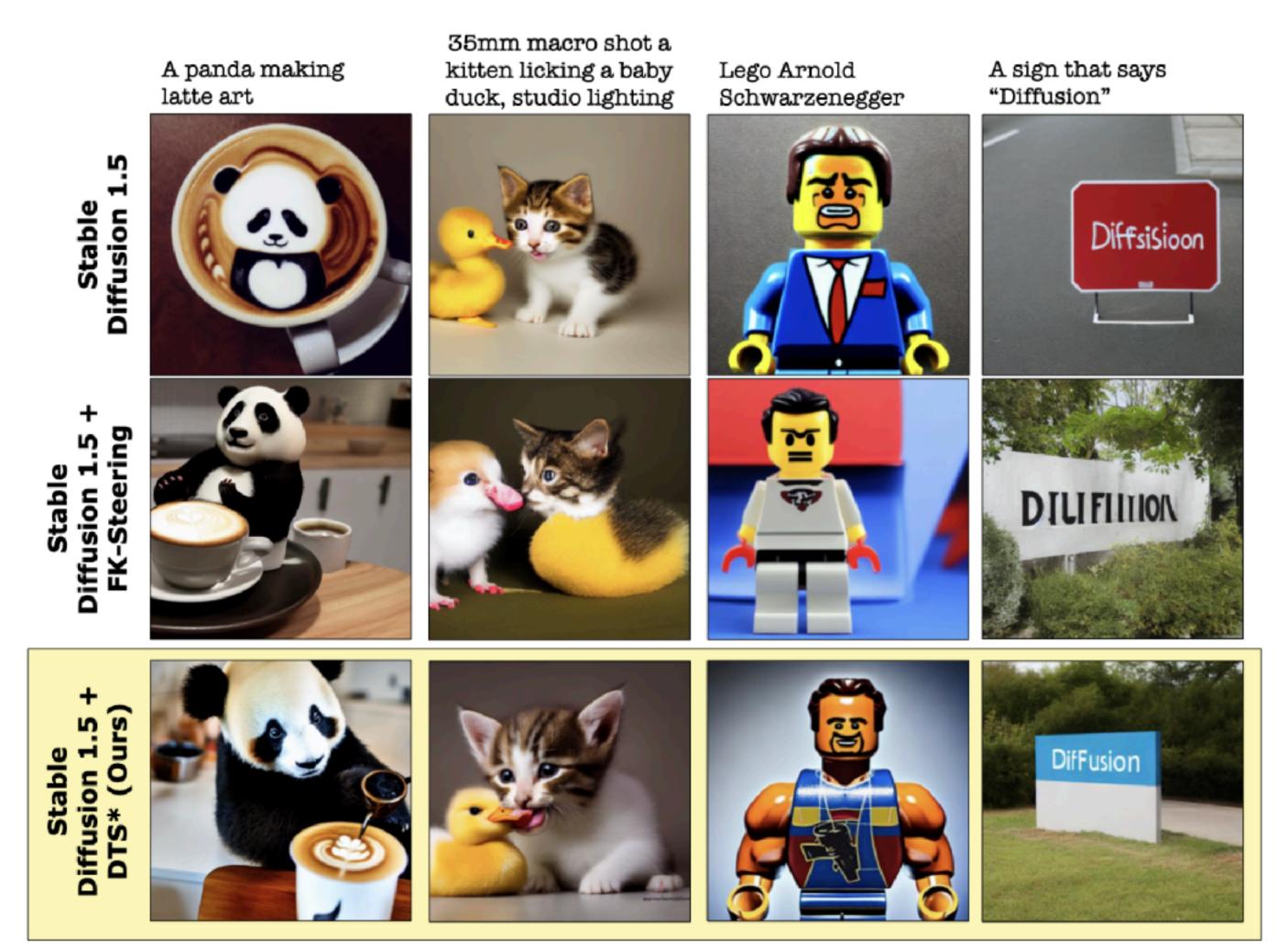
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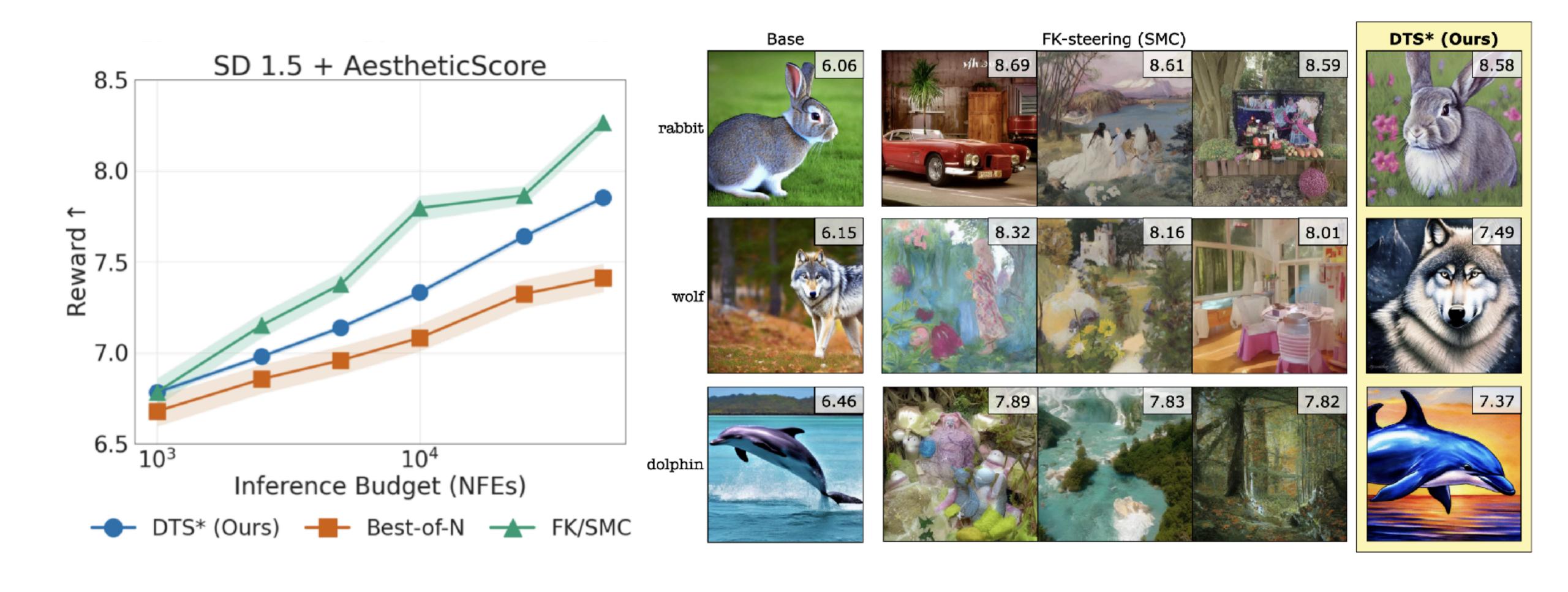
MNIST single class

Text-to-image models

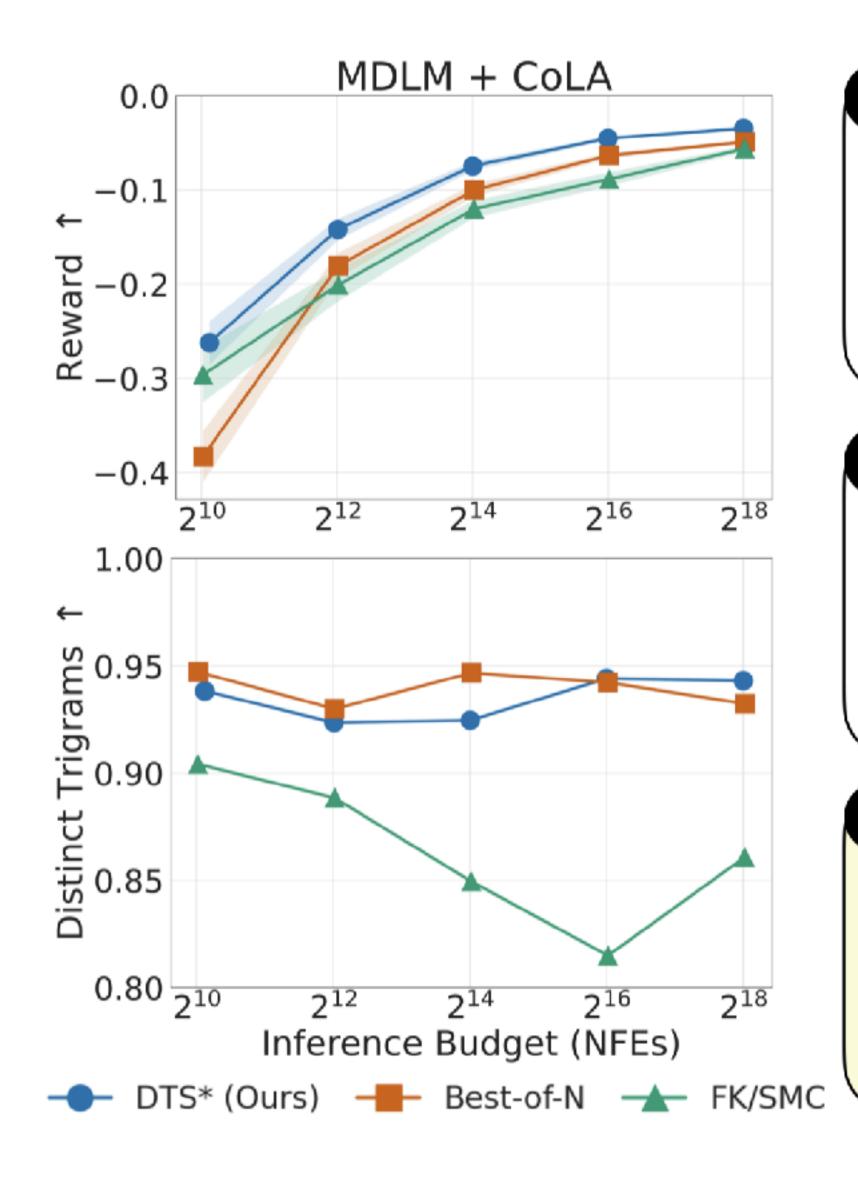




Text-to-image models



Diffusion language models



Base Reward = -1.454

The city centre workers are blamed criticised also for border management in recent years. It has involved taking millions of dollars (nominally Medicare Depenances) out of the US Treasury for months. The package was reduced to \$1.50 million, at the...

FK/SMC Reward = -0.059

The city is defended by the Royal Jamaican Squadron. The city is defended by the English Defence Squadron. The city is defended by the Continental Guards. The navy is defended by the Catalonian Squadron. The city is defended by the...

DTS* (Ours) Reward = -0.032

The city's Public Safety Committee has also promised to consider ways to discourage residents from buying private homes of their own. But tax-benefit analysts oppose such a step because they fear it would dramatically reduce the local tax base. Taxpayers...

Thank you!

Website arXiv



