

# *GC4NC*: A Benchmark Framework for Graph Condensation on Node Classification with New Insights

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Google DeepMind

# Background

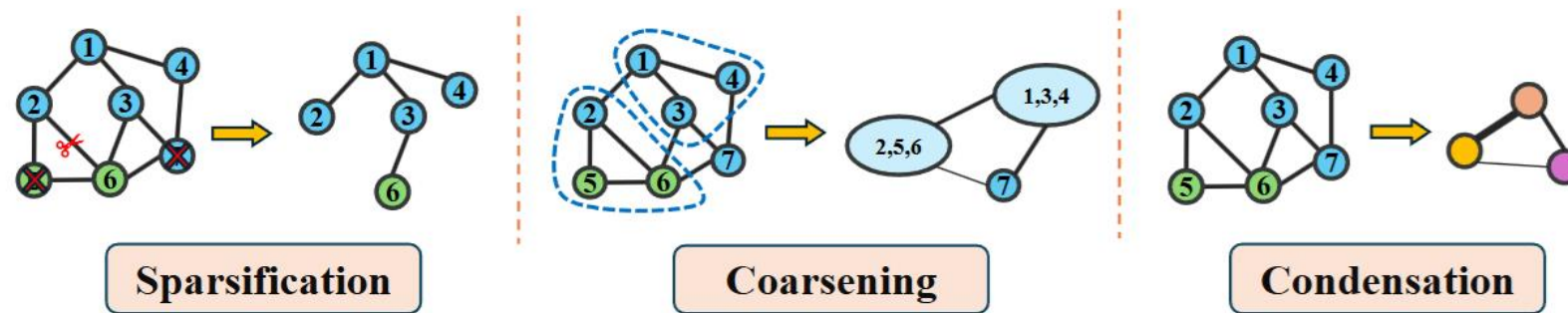


Figure 2: Illustration of key differences among three strategies of graph reduction: Graph sparsification selects significant nodes and edges while discarding others, graph coarsening groups and aggregates similar nodes and edges to construct a smaller graph, and graph condensation learns a synthetic graph from scratch.

- Large graph datasets are challenging. Graph condensation enables GNN to preserve the performance with a smaller graph.
- Many papers discussed the potential of robustness and privacy application but never verified.
- Unified protocols are needed.

# Benchmark design

- Focus on Node Classification task
  - as over 90% of GC papers work on it
- Three stages: initialization, training, evaluation
- Unified approach for fair comparison
  - fix the frequency of intermediate validation
  - fix the downstream GCN hyperparameters

# Benchmark design

- Comprehensive baselines
  - Trajectory-matching (TM)
  - Distribution-matching (DM)
  - Gradient-matching (GM)
- Multifaceted evaluation
  - Transferability
  - Initialization (connected to graph reduction methods)
  - NAS (Neural Architecture Search)
  - robustness, privacy, and graph property (new!)

# Observations: Performance and Efficiency

Condensation								Whole
TM		DM	GM					
GEOM	SFGC	GCDM	GCondX	GCond	DosCond	MSGC	SGDD	
67.61	66.27	70.65	67.79	70.05	69.41	60.24	71.87	72.6
70.70	70.27	71.27	69.69	69.15	70.83	72.08	70.52	
73.03	72.36	72.08	68.38	69.35	72.18	72.21	69.65	
78.14	75.11	79.21	79.74	80.17	80.65	80.54	80.15	81.5
82.29	79.55	80.26	78.67	80.81	80.85	80.98	80.29	
82.82	80.54	80.68	78.60	80.54	81.15	80.94	81.04	
69.64	67.61	77.62	72.03	77.36	58.13	75.25	78.11	78.6
76.21	66.89	76.63	72.05	78.05	52.70	78.26	78.07	
78.49	67.61	77.48	71.97	76.46	76.45	78.20	75.95	
64.91	64.91	60.04	59.40	60.49	55.70	57.66	58.50	71.4
68.78	66.58	60.59	62.46	63.88	57.39	64.85	59.18	
69.59	67.03	60.71	59.93	64.23	61.06	65.73	63.76	

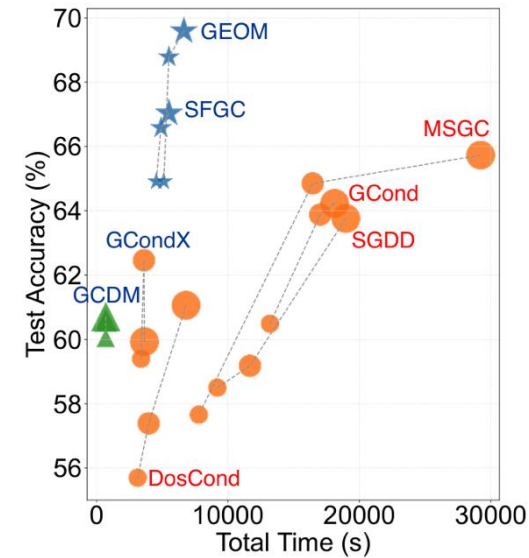


Figure 1: Test accuracy vs. total time for *structure-free* and *structure-based* condensation methods on *Arxiv*. TM is represented by ★, GM by ●, and DM by ▲. Marker sizes increase with reduction rates of 0.05%, 0.25%, and 0.50%.

- **TM-based** methods excel in condensation performance but lack efficiency.

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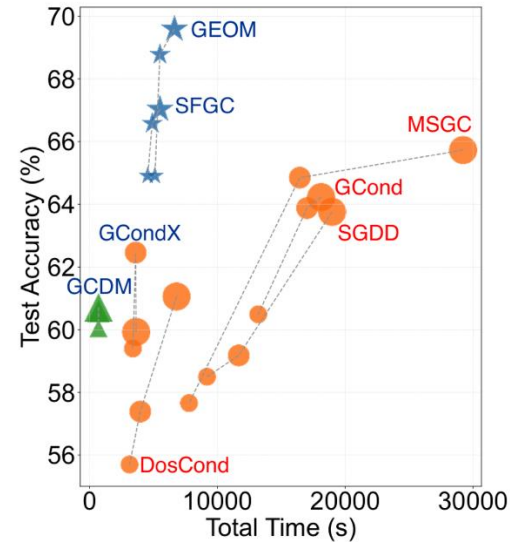
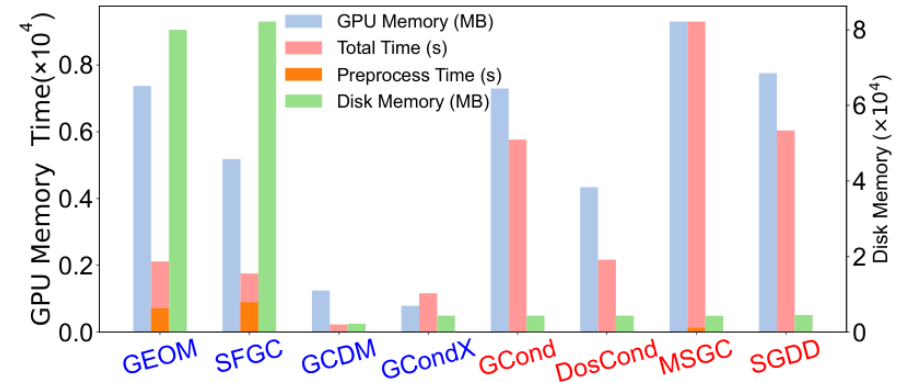


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- **Structure-free** methods are more efficient than structure-based ones.

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Figure 2: Comparison of GPU memory, disk memory, preprocess time, and total time on Arxiv ( $r = 0.5\%$ ).

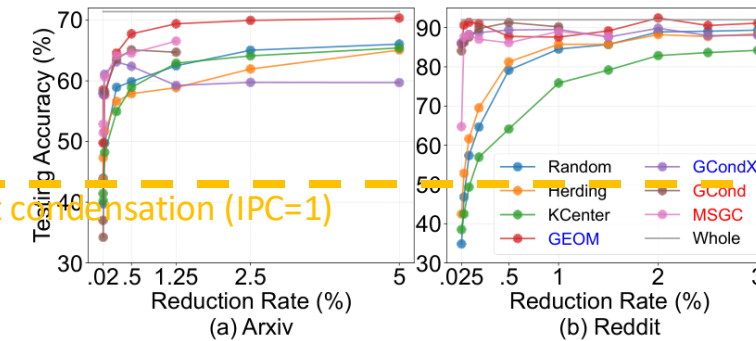


Figure 3: Varying reduction rates on Arxiv and Reddit. No mark represents OOM when the reduction rate is too large for a method.

- GC outperforms image dataset condensation at the extremely low reduction rate.



# Observations: Privacy Protection

**MIA Acc:** Membership Inference Attack, MIA Acc reflects the probability that an adversary (confidence threshold) can correctly identify whether a node belongs to the training set.

Methods	<i>Cora, r = 2.6%</i>		<i>Citeseer, r = 1.8%</i>		<i>Arxiv, r = 0.5%</i>	
	MIA Acc ( $\downarrow$ )	Acc ( $\uparrow$ )	MIA Acc ( $\downarrow$ )	Acc ( $\uparrow$ )	MIA Acc ( $\downarrow$ )	Acc ( $\uparrow$ )
<b>Whole</b>	$74.87 \pm 1.16$	$81.50 \pm 0.50$	$81.76 \pm 1.01$	$72.61 \pm 0.27$	$54.26 \pm 0.11$	$71.43 \pm 0.11$
<b>GCond</b>	$72.10 \pm 0.96$	$80.54 \pm 0.67$	$74.11 \pm 0.61$	$69.35 \pm 0.82$	<b><math>53.04 \pm 0.18</math></b>	$64.23 \pm 0.16$
<b>GCondX</b>	$66.83 \pm 0.81$	$78.60 \pm 0.31$	$71.97 \pm 0.58$	$68.38 \pm 0.45$	$54.64 \pm 0.17$	$59.93 \pm 0.54$
<b>DosCond</b>	$69.70 \pm 0.50$	$81.15 \pm 0.50$	$74.33 \pm 0.34$	$72.18 \pm 0.61$	$54.04 \pm 0.79$	$61.06 \pm 0.59$
<b>SGDD</b>	$70.43 \pm 1.63$	$81.04 \pm 0.54$	$77.07 \pm 4.32$	$69.65 \pm 1.68$	$53.29 \pm 0.46$	$63.76 \pm 0.22$
<b>GDEM</b>	<b><math>60.66 \pm 1.26</math></b>	$81.76 \pm 0.53$	$70.01 \pm 2.94$	$71.74 \pm 0.90$	-	-
<b>GEOM</b>	$67.90 \pm 0.55$	<b><math>82.82 \pm 0.17</math></b>	<b><math>67.55 \pm 0.62</math></b>	<b><math>73.03 \pm 0.31</math></b>	$53.80 \pm 0.19$	<b><math>69.59 \pm 0.24</math></b>
<b>SFGC</b>	$67.29 \pm 1.02$	$80.54 \pm 0.45$	$72.12 \pm 0.44$	$72.36 \pm 0.53$	$54.49 \pm 0.53$	$67.03 \pm 0.48$

- TM and eigen-decomposition methods balance privacy and performance.



# Observations: Robustness and Denoising Ability

**Adversarial Structural Noise:** We employ PR-BCD, a scalable adversarial noise using Projected Gradient Descent.

Dataset	Method	Feature Noise		Structural Noise		Adversarial Structural Noise	
		Test Acc. ↑	Perf. Drop ↓	Test Acc. ↑	Perf. Drop ↓	Test Acc. ↑	Perf. Drop ↓
<i>Citeseer 1.8%</i>	Whole	64.07	11.75%	57.63	20.62%	53.90	25.76%
	<b>GCond</b>	<b>64.06</b>	<b>7.63%</b>	<b>65.64</b>	<b>5.35%</b>	<b>66.19</b>	<b>4.55%</b>
	<b>GCondX</b>	61.27	10.40%	<u>60.42</u>	11.65%	<u>60.75</u>	11.15%
	<b>GEOM</b>	58.77	19.53%	<u>51.41</u>	29.60%	<u>57.94</u>	20.67%
<i>Cora 2.6%</i>	Whole	74.77	8.26%	72.13	11.49%	66.63	18.24%
	<b>GCond</b>	67.62	16.04%	63.14	21.61%	<u>68.90</u>	14.45%
	<b>GCondX</b>	<b>67.72</b>	<b>13.85%</b>	<b>63.95</b>	<b>18.63%</b>	<b>69.24</b>	<b>11.91%</b>
	<b>GEOM</b>	49.68	40.01%	53.59	35.29%	<u>66.32</u>	19.93%
<i>Flickr 1%</i>	Whole	46.68	1.51%	42.60	10.13%	44.44	6.24%
	<b>GCond</b>	<b>46.29</b>	<b>1.49%</b>	<b>46.97</b>	<b>0.04%</b>	43.90	6.58%
	<b>GCondX</b>	45.60	2.11%	<u>46.19</u>	0.83%	42.00	9.83%
	<b>GEOM</b>	45.38	1.63%	<u>45.52</u>	1.32%	<b>44.72</b>	<b>3.06%</b>

- **Structure-based** approaches offer superior robustness.

# Observations: Graph Properties Preservation

**Supervised DBI** (Davies-Bouldin Index) measures the quality of a **class** by evaluating the average similarity between each class and its most similar class

Graph Property		VNG	GCond	MSGC	SGDD	Avg.	Whole
Density% (Struc.)	<i>Cora</i> Corr.	52.17 -0.81	82.28 0.07	22.00 0.55	100.00 0.13	64.11 -0.02	0.14 -
Max Eigenvalue (Spectra)	<i>Cora</i> Corr.	3.73 0.85	34.90 0.25	1.69 0.95	14.09 0.28	13.60 0.58	169.01 -
DBI (Label & Feature)	<i>Cora</i> Corr.	3.69 0.81	1.84 0.93	0.70 0.94	4.34 0.97	2.64 <b>0.91</b>	9.28 -
DBI-AGG (Label & Feat. & Stru.)	<i>Cora</i> Corr.	3.59 0.99	0.38 0.93	0.57 0.95	0.18 0.89	1.18 <b>0.94</b>	4.67 -
Homophily (Label & Struc.)	<i>Cora</i> Corr.	0.14 -0.83	0.16 -0.68	0.19 -0.46	0.13 -0.80	0.16 -0.69	0.81 -

- **Node and aggregated features** are preserved in condensed graphs.

# Observations: Graph Properties Preservation

Table 17: Correlation between condensed graph properties and model performance.

	<b>VNG</b>	<b>GCond</b>	<b>MSGC</b>	<b>SGDD</b>	<b>Correlation</b>
Avg ACC	63.34	69.40	69.02	68.95	-
Density (%)	-0.81	0.07	0.55	0.13	0.91
Max Eigen	0.85	0.25	0.95	0.28	-0.51
DBI	0.81	0.93	0.94	0.97	0.96
DBI-AGG	0.99	0.93	0.95	0.89	-0.80
Homophily	-0.83	-0.68	-0.46	-0.80	0.54

- Preserving Density%, DBI tends to be beneficial for downstream tasks.

# Observations: Transferability and Initialization

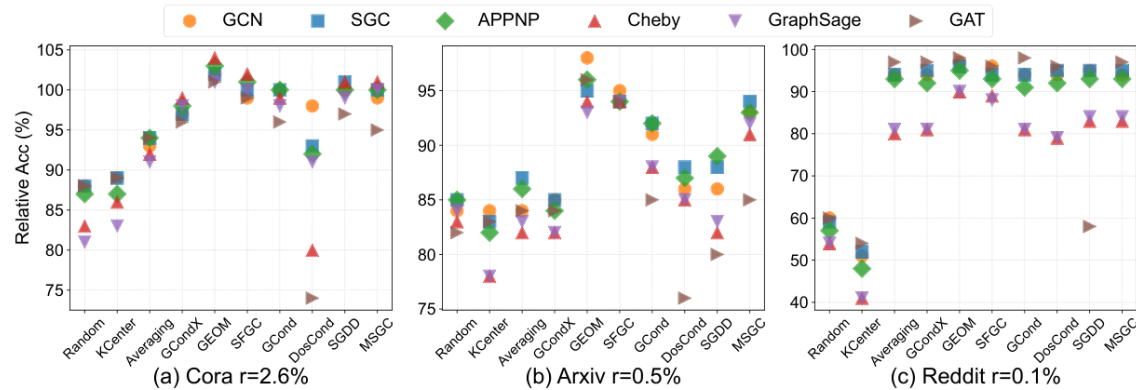


Figure 4: Condensed graph performance evaluated by different GNNs. The **relative accuracy** refers to the accuracy preserved compared to training on the whole dataset.

- GC methods vary in transferability across datasets.

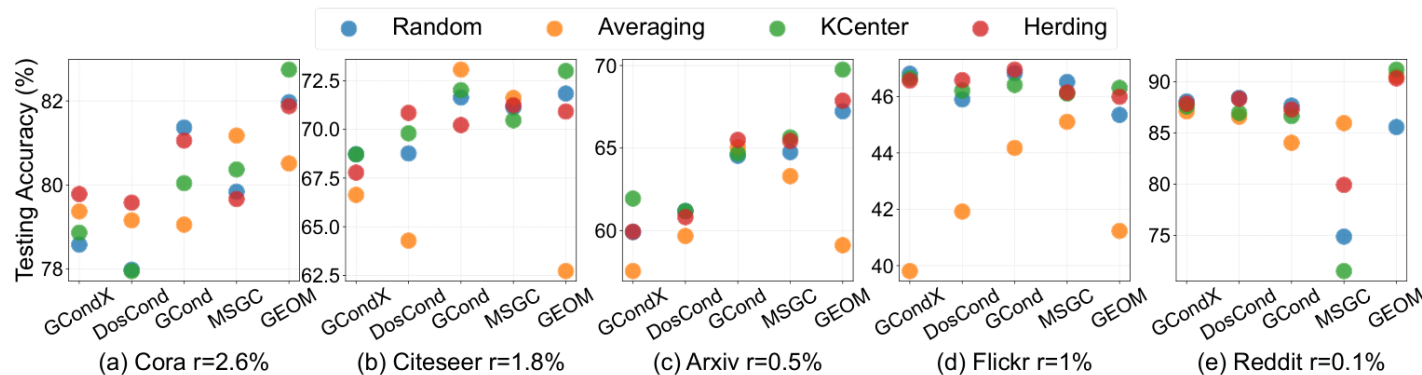


Figure 5: Test accuracy for different methods with different initialization.

- Current initialization strategies lack consistent impact.

# Observations: NAS

**Recall:** how many of the  $G$  top- $K$  architectures also appear in the top  $K$  on the  $G'$

**Top 1:** the performance of the  $G'$  top 1 architecture on the  $G$

Table 13: Recall@ $K$  of top- $K$  architectures evaluated on Cora with  $r = 0.5$ .

	Random	K-Center	GCondX	SFGC	GEOM	GCond	DosCond	MSGC
Recall@5	0.0	0.0	0.2	0.0	0.2	0.0	0.0	0.0
Recall@10	0.0	0.0	0.2	0.1	0.2	0.2	0.1	0.1
Recall@20	0.4	0.35	0.5	0.45	0.4	0.45	0.25	0.4

	Random	K-Center	GCondX	SFGC	GEOM	GCond	DosCond	MSGC	Whole
Top 1 (%)	81.88	81.74	81.49	82.42	82.19	81.82	81.91	82.40	82.51
Acc. Corr.	0.56	0.47	0.40	0.72	0.65	0.70	0.14	0.71	-
Rank Corr.	0.64	0.60	0.57	0.71	0.74	0.66	0.20	0.78	-

- TM or inner optimization (like GCondX, GCond) is key for NAS effectiveness.

# Conclusions

- First benchmark for GC methods with multi-dimension evaluation.
- Novel insights on privacy, robustness and graph properties.
- Inspires future directions for better performance and scalability.

# Toolkit

- Run Graph Condensation with 3 lines of code and evaluate with another 2!

```
from graphslim.dataset import *
from graphslim.evaluation import *
from graphslim.condensation import GCond
from graphslim.config import cli

args = cli(standalone_mode=False)
args.reduction_rate = 0.5
args.device = 'cuda:0'
graph = get_dataset('cora', args=args)
agent = GCond(setting='trans', data=graph, args=args)
reduced_graph = agent.reduce(graph, verbose=True)
evaluator = Evaluator(args)
res_mean, res_std = evaluator.evaluate(reduced_graph, model_type='GCN')
```



<https://github.com/Emory-Melody/GraphSlim>



# THANK YOU

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